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IIT JAM 2022 Question Paper (All Subjects)

IIT Joint Admission Test for Masters

Subjects	Page No.
Biotechnology (BT)	2 - 29
Chemistry (CY)	30 - 68
Economics (EN)	69 - 115
Geology (GG)	116 - 147
Mathematical Statistics (MS)	148 - 191
Mathematics (MA)	192 - 233
Physics (PH)	234 - 268

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Section A	a: Q.1 – Q.10 Carry ONE mark each.	
Q.1	Which of the following is involved in innate immune response in higher mammals?	ST.
(A)	T cell antigen receptor	ortes
(B)	B cell antigen receptor	A.
(C)	Toll-like receptor	
(D)	Major histocompatibility complex-II molecule	
	Proventing to the	
Q.2	Which among the following belongs to the family "Retroviridae"?	
(A)	Human Immunodeficiency virus	
(B)	Ebola virus	
(C)	Dengue virus	
(D)	Influenza virus	
Ry.		



Q.3	Which of the following is a glycolipid?
(A)	Cerebroside
(B)	Phosphatidylcholine
(C)	Phosphatidylserine
(D)	Cardiolipin
	22222 All AN INSTITUTE OF THE AND
Q.4	Which of the following bacterial component contains "dipicolinic acid"?
(A)	Endospore
(B)	Capsule
(C)	Flagella
(D)	Pili
20.00	



Q.5	The fossilization process in which mineral rich water penetrates through the pores of decomposed organic matter is known as	
(A)	Carbonization	all' e
(B)	Chemical fossilization	Porte of
(C)	Petrifaction	
(D)	Microfossilization	
	The dealer weather the state of	
Q.6	A random fluctuation in gene frequency is called	
(A)	Genetic drift	
(B)	Genetic load	
(C)	Panmixis	
(D)	Genetic shift	
Joint	AN I WE	
- Ales		



Q.7	The number of "Barr Bodies" present in a somatic cell of a woman suffering from Turner syndrome is	
(A)	0	elle e
(B)	1 3HUNGE	Loothe St.
(C)	2 Institute technology	
(D)	3 ganiting the office of the o	
	Charles and State	
	A MARTIN HOLE	
Q.8	Which of the following are produced by Mangrove trees to survive in the waterlogged swampy forests?	
(A)	Trichomes	
(B)	Pneumatophores	
(C)	Spermatophores	
(D)	Cambia	
20, 12		



Q.9	Indeterminate growth in plants is due to the presence of perpetually undifferentiated tissues, called as	
(A)	Tracheids	211th
(B)	Meristems	200The
(C)	Parenchyma	
(D)	Sclerenchyma	
	There are the search of the se	
Q.10	The osmotic potential (ψ) of pure water is MPa.	
(A)	-1	
(B)	0 For Mar UR	
(C)		
(D)	1050	
Joint		
A.		
<u></u>		



Section A	Section A: Q.11 – Q.30 Carry TWO marks each.			
Q.11	Bacteria containing a tuft of flagella that comes out from one pole is called			
	1			
(A)	Lophotrichous			
	3112			
(B)	Peritrichous			
	India tes at			
(C)	Monotrichous			
	A BOLL MALL TON			
(D)	Amphitrichous			
	A CONTRACTOR OF THE CONTRACTOR OF TO C			
Q.12	Which of the following activity is associated with <i>Klenow</i> fragment?			
2.12	which of the following derivity is associated with Richow Hughlent.			
(A)	5'-3' exonuclease activity			
	2 tel ⁹			
(B)	5'-3' endonuclease activity			
	to i fai			
(C)	Polymerase activity			
(D)	3'-5' endonuclease activity			
2	M. S.			
ath	ALC .			
0. K				
As				



Q.13	A frameshift mutation is caused by	
(A)	5-Bromouracil	A.
(B)	Acridine	oone St.
(C)	Glutathione	S.
(D)	Hypoxanthine	
	Ordantian Institution of the second s	
Q.14	The zone of a pond system where respiration is more than production is called as	
(A)	Limnetic zone	
(B)	Littoral zone	
(C)	Epilimnion zone	
(D)	Benthic zone	
Joint	AN I WE WANTED	
12.0		



Q.15	An organism that causes obstruction of lymphatic system in humans is	
(A)	Borrelia burgdorferi	L.
(B)	Brucella abortus	200 Hee
(C)	Yersinia pestis	Le la
(D)	Wuchereria bancrofti	
	Organing the Alexandree of the	
Q.16	A man having a dominant genetic trait (TT genotype) can taste phenylthiocarbamide (PTC), marries a woman who cannot taste PTC. The PTC tasting ability of their biological son and daughter is	
(A)	Son taster; Daughter non-taster	
(B)	Daughter taster; Son non-taster	
(C)	Both are non-tasters	
(D)	Both are tasters	
201.14		

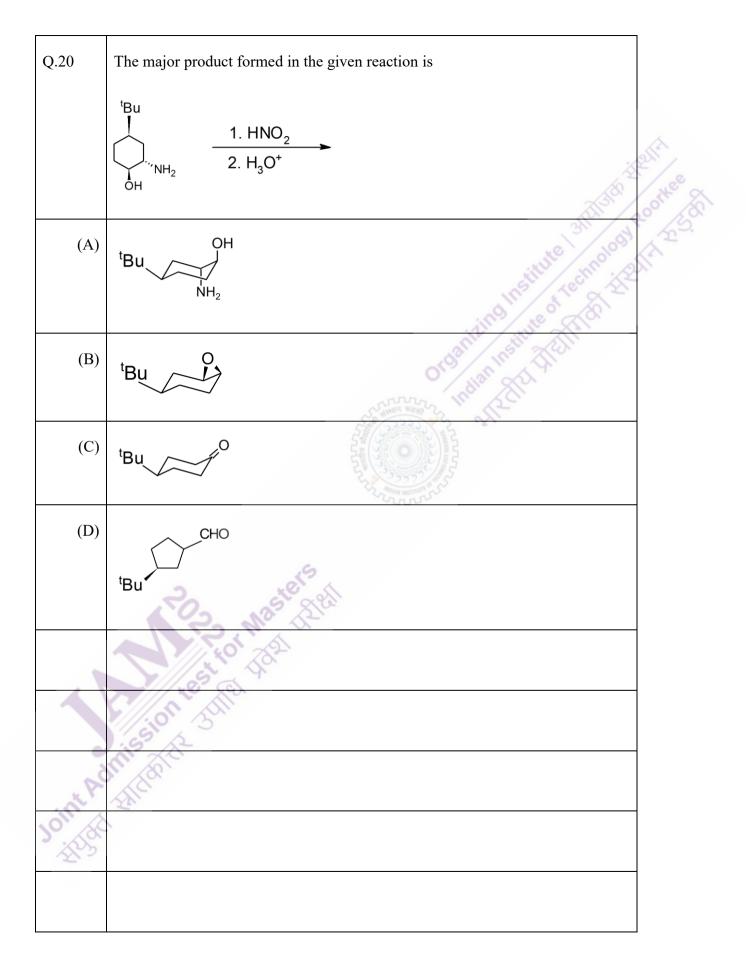


Q.17	Which of the following enzymes is absent in a person suffering from Alkaptonuria?	
(A)	Tyrosinase	elle e
(B)	Homogentisic acid oxidase	Loother St.
(C)	Catechol dioxygenase	
(D)	Phenylalanine hydroxylase	
	The search of th	
Q.18	The bacterium that can tolerate high concentrations of salt and also ferment mannitol is	
(A)	Staphylococcus aureus	
(B)	Staphylococcus epidermis	
(C)	Streptococcus pyogenes	
(D)	Serratia marcescens	
201.19		



Q.19	Match the following	
	Group I	Group II
	P) Streptomycin	1) Inhibits beta-subunit of RNA polymerase
	Q) Cycloheximide	 2) Inhibits peptidyl transferase activity of 50S subunit 2) I hibits period to the formula of (0S phone) in the fo
	R) Rifamycin	3) Inhibits peptidyl transferase activity of 60S subunit
	S) Chloramphenicol	4) Inhibits binding of formyl methionine tRNA to ribosome
(A)	P-1, Q-3, R-4, S-2	
(B)	P-4, Q-3, R-1, S-2	
(C)	P-2, Q-3, R-1, S-4	naster 28
(D)	P-3, Q-4, R-1, S-2	Can and a second
	Sion Juli	
ALAN	Man Ball	
John		







Q.21	DNA gyrase can	
(A)	cut single-stranded DNA	alla.
(B)	relax supercoiled DNA	and the constant
(C)	introduce negative supercoiling in DNA	S.
(D)	not utilize ATP	
	Organian Institution of the Alter Al	
Q.22	The stationary phase of cation-exchange chromatography can be	
(A)	DEAE-cellulose	
(B)	CM-cellulose	
(C)	Sephadex G-50	
(D)	Heparin-Sepharose	
inth	I LOO	
20.10		



Q.23	Components of a Transmission Electron Microscope are
(A)	Electron gun, objective lens, positron beam, projector lens
(B)	Neutron beam, projector lens, objective lens, evacuated tube
(C)	Electron beam, projector lens, objective lens, condenser lens
(D)	X-ray beam, projector lens, objective lens, condenser lens
	Organita Institution organitation
Q.24	In a honey bee population, the workers are infertile but protect the queen from
	intruders and help in reproduction. This is an example of
(A)	K selection
(B)	Sexual selection
(C)	Kin selection
(D)	Disruptive selection
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Q.25	For an enzyme following Michaelis-Menten kinetics, when [S]=K _M then, the velocity v is	
	([S] is substrate concentration, K_M is Michaelis constant, V_{max} is maximal velocity)	ellin ee ~
(A)	$[S] \times V_{max}$	oor So
(B)	$0.75 \times V_{max}$	2
(C)	$0.5 imes V_{max}$	
(D)	$K_M \times V_{max}$	
Q.26	The net equation for aerobic glycolysis is	
(A)	Glucose+2ATP \longrightarrow 2 lactate+2ADP+2P _i	
(B)	Glucose+2ADP+2P _i +2NAD ⁺ \longrightarrow 2 pyruvate+2ATP+2NADH+2H ₂ O+4H ⁺	
(C)	Glucose+2ADP+2P _i \longrightarrow 2 pyruvate+2ATP+2H ₂ O	
(D)	$Glucose+2ADP+2P_i+2NAD^+ \longrightarrow 2 lactate+2ATP+2NADH+2H_2O+4H^+$	
Joint	Xe	
Ĵ.		



	Γ
Q. 27	In the electron transport chain, flavin mononucleotide (FMN) can adopt as the highest oxidation state and is capable of accepting or donating electrons, respectively.
(A)	2; 2 or 3
(B)	2; 1 or 2
(C)	3; 2 or 3
(D)	3; 1 or 2
	STATUS AND A STATUS
Q.28	In bacteria, the σ factor that plays a major role in transcription during the stationary phase is
(A)	
(B)	σ ⁵⁴
(C)	σ^{28}
(D)	σ^{32}
公う	



Q.29	A rise in cytosolic calcium ion concentration just after fertilization in a sea urchin egg leads to	
(A)	Formation of fertilization envelope	ell's
(B)	Acrosomal reaction	200the Sci
(C)	Formation of vegetal pole	<u> </u>
(D)	Formation of animal pole	
	Change of the state of the stat	
	A STATUTION AND A STATUTION AN	
Q.30	In a nephron, follows the ascending limb of the "loop of Henle".	
(A)	Descending limb	
(B)	Distal tubule	
(C)	Collecting tubule	
(D)	Proximal tubule	
Jointh		



Section B	: Q.31 – Q.40 Carry TWO marks each.
Q.31	Transpirational pull that extends down to the roots in plants can be interrupted by
(A)	Process of cavitation
(B)	Process of gravitation
(C)	Formation of water vapor pockets
(D)	Positive pressure in xylem sap
2.32	Transfer of plasmids into animal cells can be achieved by
(A)	Electroporation
(B)	Liposome-mediated process
(C)	Calcium chloride treatment
(D)	Sucrose treatment



Q.33	Archaeal cell membranes contain lipids that are	
(A)	Ether linked	A.
(B)	Ester linked	oorhee a
(C)	Branched alkyl chain	15. A
(D)	Linear alkyl chain	
	Ordan Institut ACIT	
Q.34	Which of the following are producers in an ecological system?	
(A)	Macrophytes	
(B)	Phytoplanktons	
(C)	Zooplanktons	
(D)	Cyanobacteria	
in you	M. Cal	
20.10		

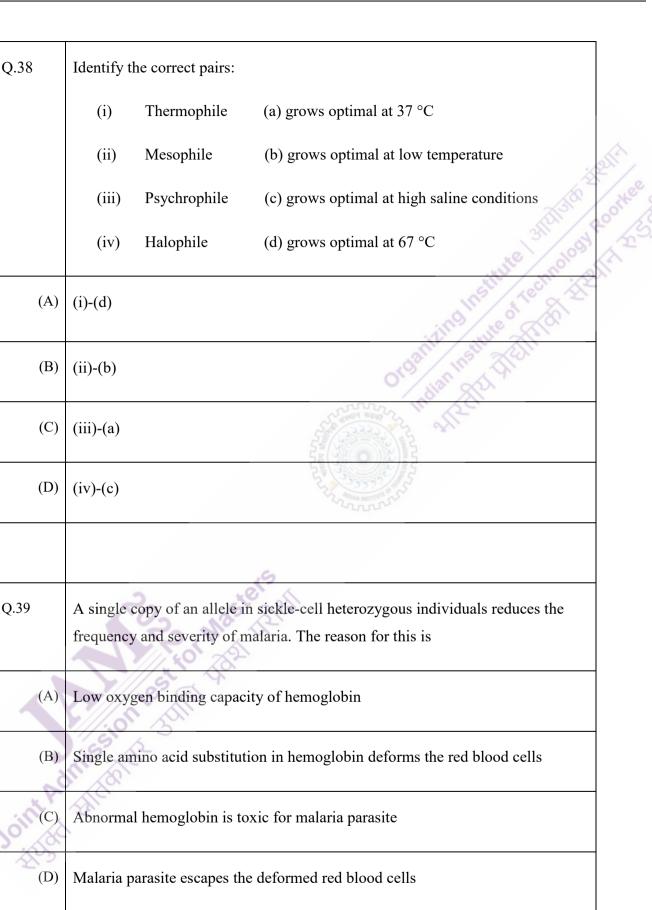


Q.35	Which of the following acts as wound hormones in plants?	
(A)	Ethylene	A.
(B)	Cytokinins	oothee a
(C)	Abscisic acid	15. 1
(D)	Dextrin	
	Organian Institution of the state of the sta	
Q.36	The enriched media used to facilitate the growth of fastidious microorganisms are	
(A)	Selenite F broth	
(B)	Blood agar	
(C)	Chocolate agar	
(D)	Loeffler's serum	
Joint	AN I WE	
20		

Q.37	Match the	e bacterial struct	ure to func	tion	
	(i)	Cell wall	(a)	Virulence factor	
	(ii)	Glycocalyx	(b)	Selective permeability	alla
			(c)	Attachment to surfaces	Loothee St
			(d)	Protection from osmotic lysis	12. 12.
(A)	(i)-(b), (ii	i)-(d)		ing institute of Teening in	
(B)	(i)-(d), (ii	i)-(a)		organite institut ACI	
(C)	(i)-(c), (ii	i)-(b)		A REAL PROPERTY OF THE REAL PR	
(D)	(i)-(d), (ii	i)-(c)			
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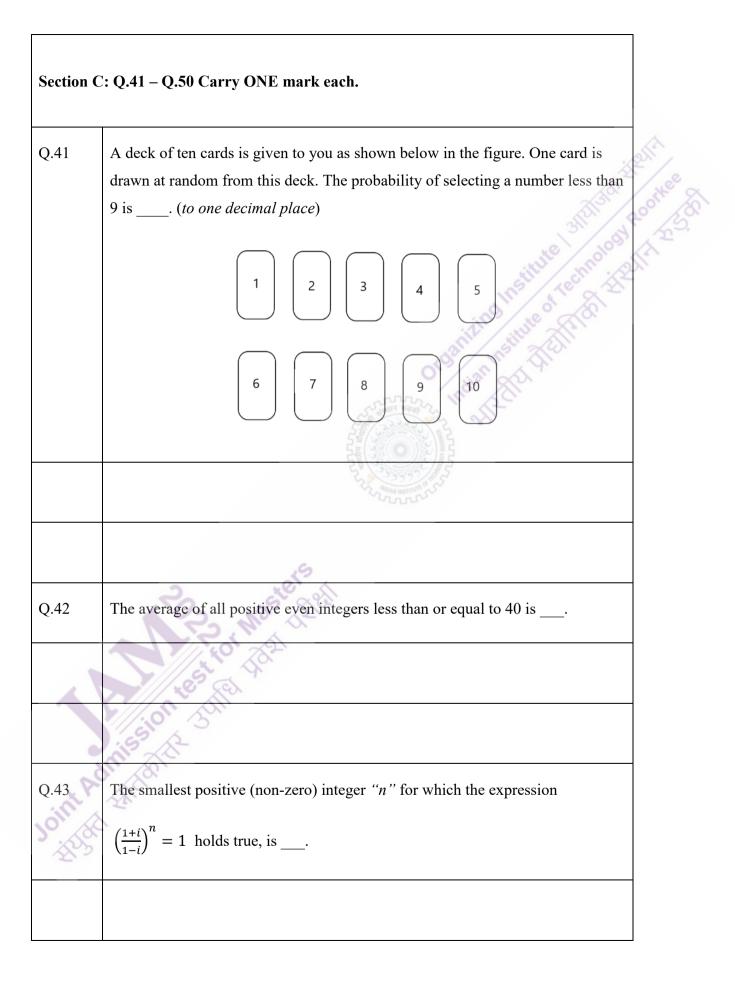
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BIOTECHNOLOGY - BT



Q.40	The correct statement/s for bimolecular nucleophilic substitution reactions is/are	
(A)	It goes through a carbocation formation	a fai
(B)	There is an inversion of configuration if the reacting center is chiral	orkee
(C)	Reaction is enhanced when carried out in polar solvents	S.
(D)	The reaction intermediate is trigonal bipyramidal	
	Ordan Institut ACAL	
	5	
	Res master Plail	
	10' 70' 70'	
	ission Juli	
inthe	R. ESC	
20. 14	Histon Julie	







Q.44	Given that
	$A = (sin\theta \cos\theta \tan\theta + sin\theta \cos\theta \cot\theta), \text{ the value of A is}$
	ALC: A
	20 200
	of the state of technic it?
Q.45	An object is placed at the principal focus of a concave lens of focal length 10
	cm. The image will be formed atcm, between the optical center and the
	focus of the lens on the same side of the object.
	MOBAN RESTRICTION
0.46	What is the maximum number of hydrogen bonds that a water molecule can
Q.46	make in the liquid state?
	make in the right state.
	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
	Sol Shi
	il state
Q.47	How many pairs of autosomal chromosomes are there in normal humans?
oin	
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Q.48	Calculate the temperature (in K) at which the resistance of a metal becomes
	20% more than its resistance at 300 K. The value of the temperature coefficient
	of resistance for this metal is 2.0×10^{-4} /K.
	2
	12 AS
	A Contraction of the second seco
	suite 3 notosy
Q.49	In the ¹ H NMR spectrum of ethanol at 400 MHz, the methyl group splits into
	number of peaks.
	Call Her Tak
	O' dian git
	The second se
	Martin Second X 2
0.50	In a denaturing polyacrylamide gel electrophoresis experiment, pure intact adult
Q.50	In a denaturing polyacrylamide gel electrophoresis experiment, pure intact adult human hemoglobin will yield (number) bands.
Q.50	In a denaturing polyacrylamide gel electrophoresis experiment, pure intact adult human hemoglobin will yield(number) bands.
Q.50	



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Section C	2: Q.51 – Q.60 Carry TWO marks each.	
Q.51	A man throws a ball vertically up in the air with an initial velocity v_1 such that it	
	reaches a height of 12 m with a speed of 12 m/s. If he throws the same ball	A.
	vertically up with an initial velocity v_2 such that it reaches a maximum height of	2/20
	12 m. Calculate v ₁ /v ₂ . (<i>up to 2 decimal places</i>)	porte 20
	Stitute comology	
	aniting the of Fich	
Q.52	What is the acceleration due to gravity (m/s ²) on the surface of a planet if its	
	radius is 1/4 th that of earth and its mass is 1/80 th that of earth? Assume that the	
	gravity on the surface of the earth is 10 m/s^2 .	
	AND	
	ets all	
Q.53	In a randomly mating population, the frequency of 'A' allele is 0.7. What is the	
	frequency of 'Aa' genotype in the next generation according to Hardy-	
	Weinberg's law? (up to two decimal places)	
	NISSION SUL	
oint	THER.	
Q.54	The potential difference to accelerate an electron was quadrupled. By what	
	factor does the <i>de Broglie</i> wavelength of the electron beam change?	



best resolution (in nm) of this microscope? Q.56 Assuming the molecule shown below is aromatic, the value of "n" according	ie
best resolution (in nm) of this microscope? Q.56 Assuming the molecule shown below is aromatic, the value of "n" according	Ie
best resolution (in nm) of this microscope? Q.56 Assuming the molecule shown below is aromatic, the value of "n" according the molecule shown below is aromatic.	ne
best resolution (in nm) of this microscope? Q.56 Assuming the molecule shown below is aromatic, the value of "n" according the molecule shown below is aromatic.	ne
best resolution (in nm) of this microscope? Q.56 Assuming the molecule shown below is aromatic, the value of "n" according the molecule shown below is aromatic.	
Q.56 Assuming the molecule shown below is aromatic, the value of "n" according	og T
A A A A A A A A A A A A A A A A A A A	100
A A A A A A A A A A A A A A A A A A A	
A A A A A A A A A A A A A A A A A A A	2
The second second	
The second second	to
"Hückel's rule" is	
Ro sters gell	
B the the	
A COLORAD	
10 - CO	
Q.57 In an actively growing population from a single bacterium, 1,048,576 cells are	·e
present after 20 th generation. How many cells were there in 5 th generation?	
A CAL	
oint 2n	
3 10-	
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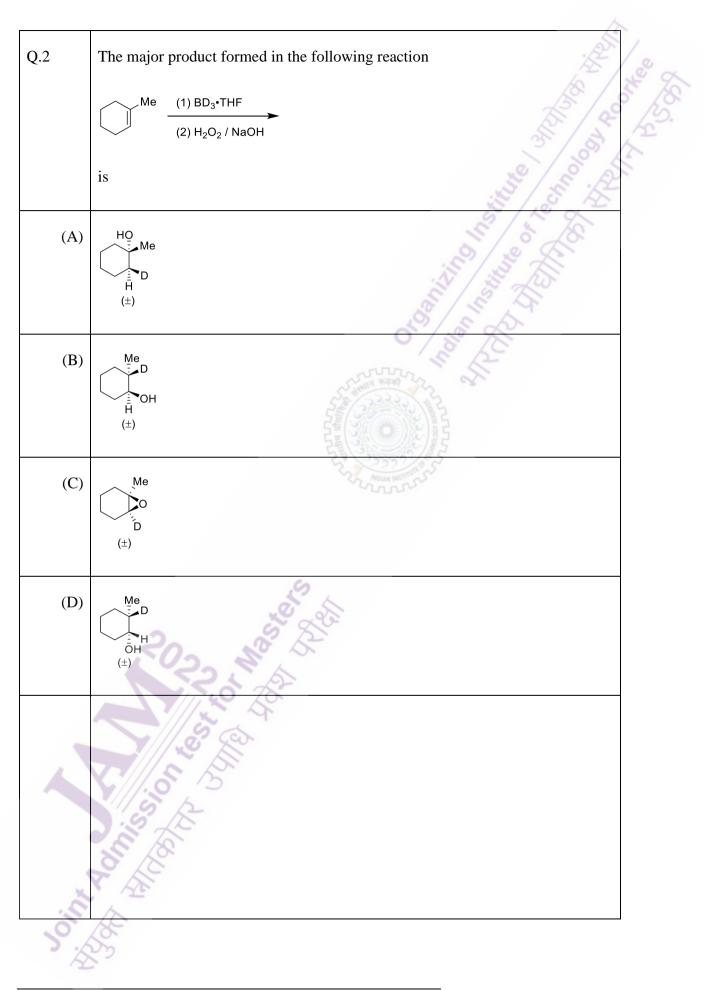


Q.58	A double stranded DNA molecule of total 5000 base pairs long, has a melting temperature of 85 °C. What will be the % AT base pairs in this sample? (<i>up to one decimal place</i>).	
	AS AS	atter 2
	stute 310 on	en fin
Q.59	How many GTP molecules are required for the translocation of tRNA from P site to E site during translation elongation process in bacteria?	
	OTON THE REAL PROPERTY OF THE	
Q.60	Amongst the molecules given below, the total number of molecules that have at least one sp^2 hybridized atom is	
	C ₆ H ₆ , NO ₂ , BF ₃ , H ₂ O ₂ , SO ₂ , C ₂ H ₂ , <i>L</i> -Tryptophan	
~	test for	
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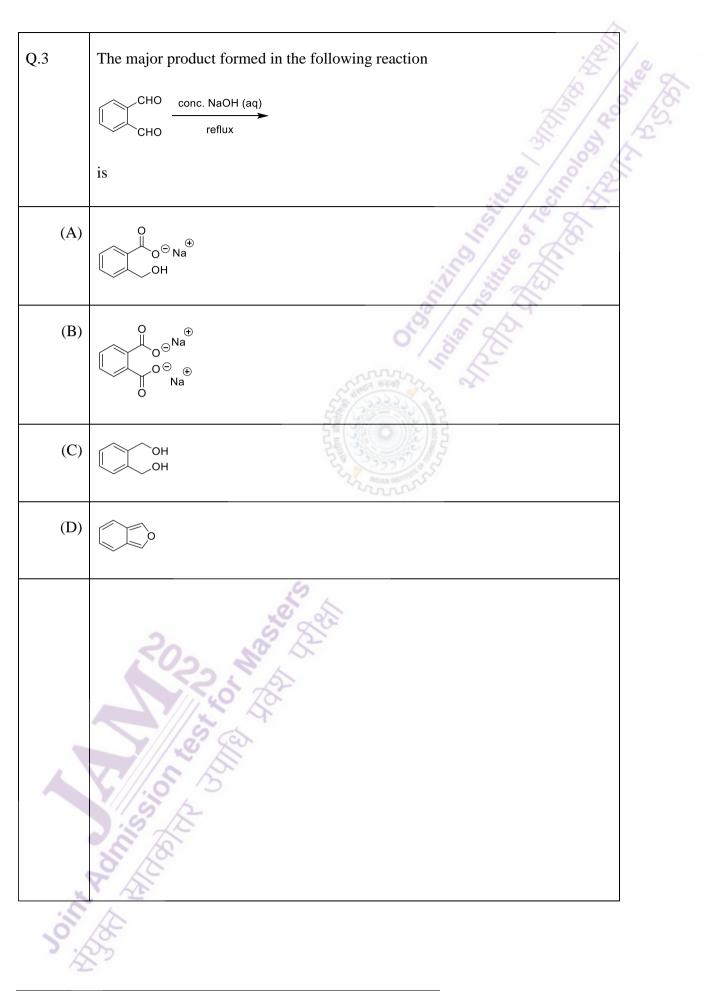


Section A	A: Q.1 – Q.10 Carry ONE mark each.	100 0
Q.1	The reagent required for the following transformation	165. AS.
		h.
	is a set of the set of	
(A)	NaBH ₄	
(B)	LiAlH ₄	
(C)	H ₃ B·THF	
(D)	Zn(Hg)/HCl	
doin.	2022 Master Aller 2022 Master Aller 2023 Master A	

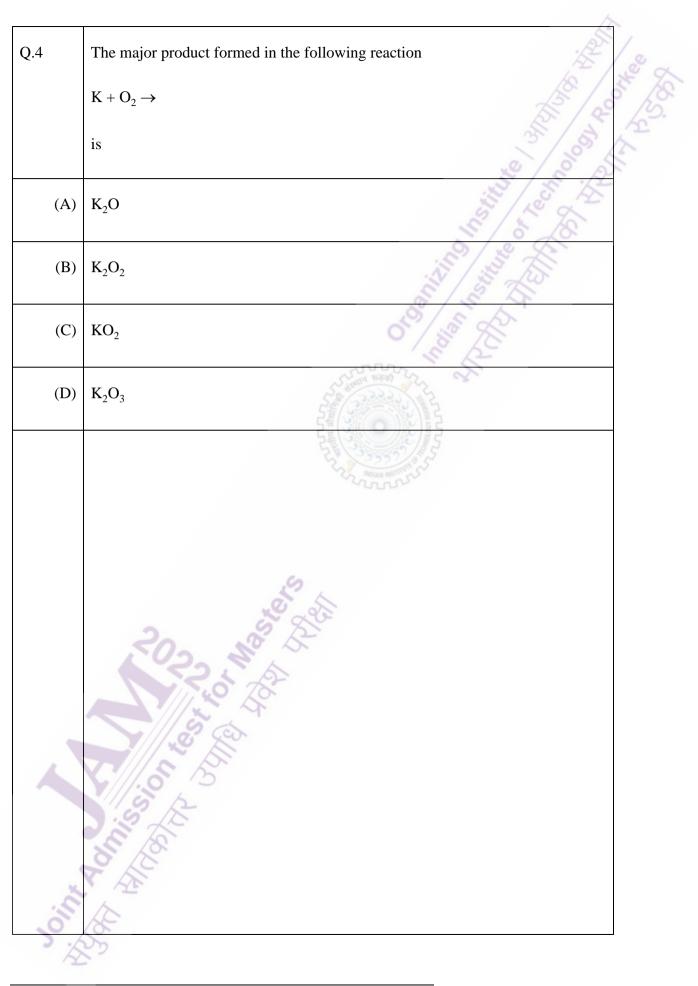




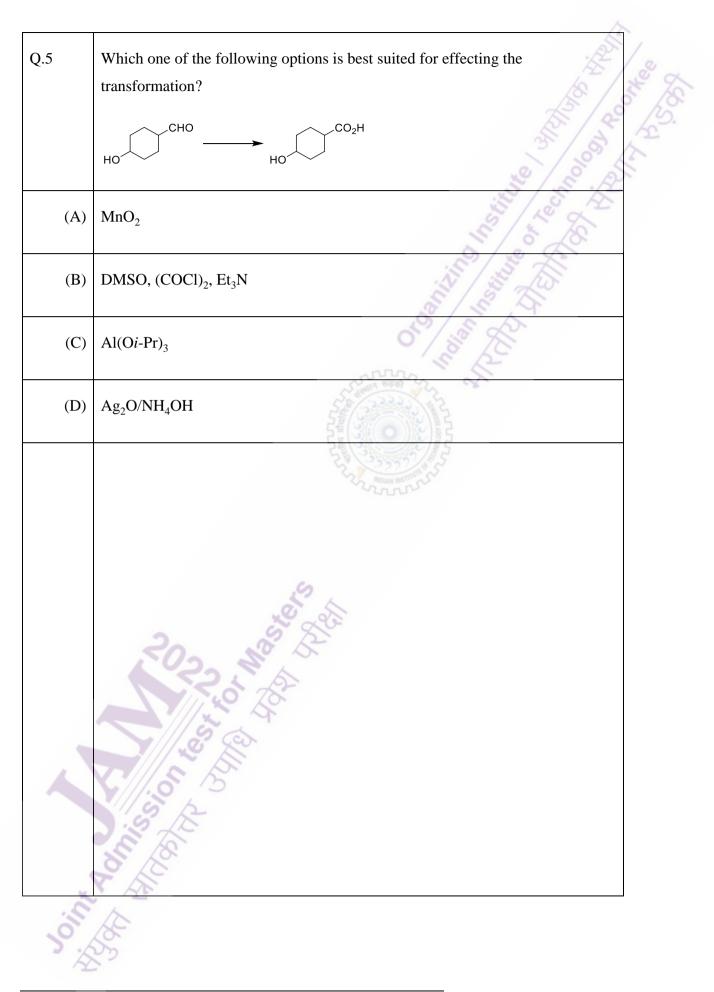














Q.6	The structure of $[XeF_8]^{2-}$ is
(A)	cubic
(B)	hexagonal bipyramid
(C)	square antiprism
(D)	octagonal
in o	Por to



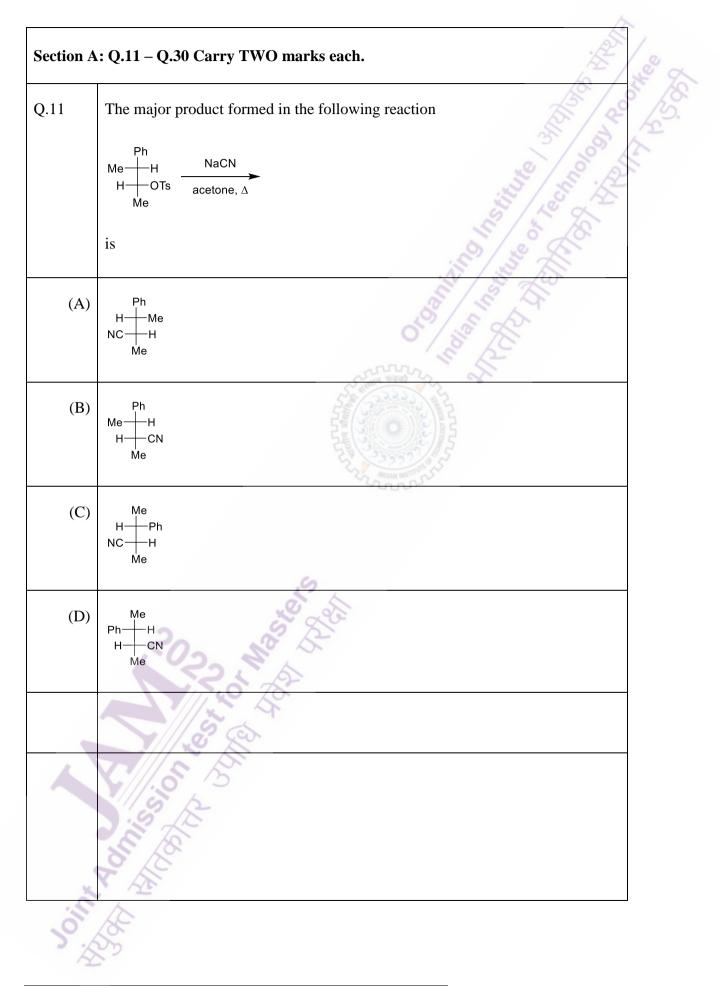
	L.
Q.7	Among the following, the compound that forms the strongest hydrogen bond is
(A)	HF
(B)	HCI
(C)	HBr
(D)	ні
	State and the state
	Matter and a second sec
Q.8	Among the following, the biomolecule with a direct metal-carbon bond is
(A)	coenzyme B ₁₂
(B)	nitrogenase
(C)	chlorophyll
(D)	hemoglobin
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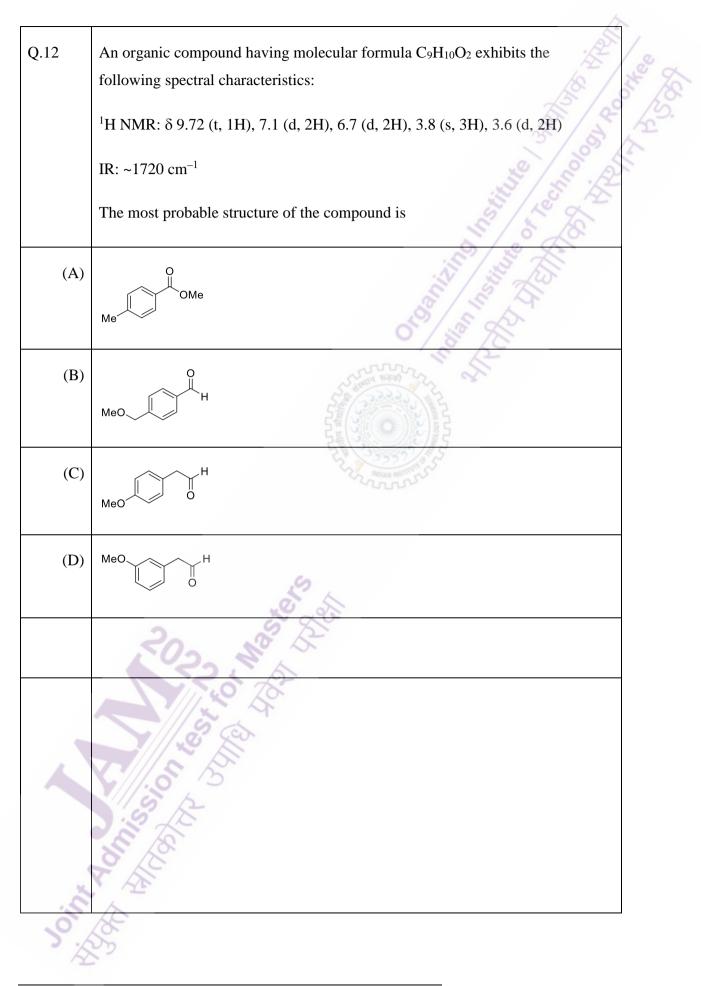


Q.9	For the reaction	e d
	$H_2PO_2^-(aq) + OH^-(aq) \rightarrow HPO_3^{2-}(aq) + H_2(g)$	18.
	the rate expression is $k[H_2PO_2^-][OH^-]^2$. If the concentration of $H_2PO_2^-$ is	2
	doubled, the rate is	
(A)	tripled	
(B)	halved	
(C)	doubled	
(D)	unchanged	
	ARDIAN RESTRICT	
Q.10	The nature of interaction involved at the gas-solid interface in physisorption is	
(A)	ionic	
(B)	van der Waals	
(C)	hydrogen bonding	
(D)	covalent	
	Sing Ba	
in	N AN	
5.4		





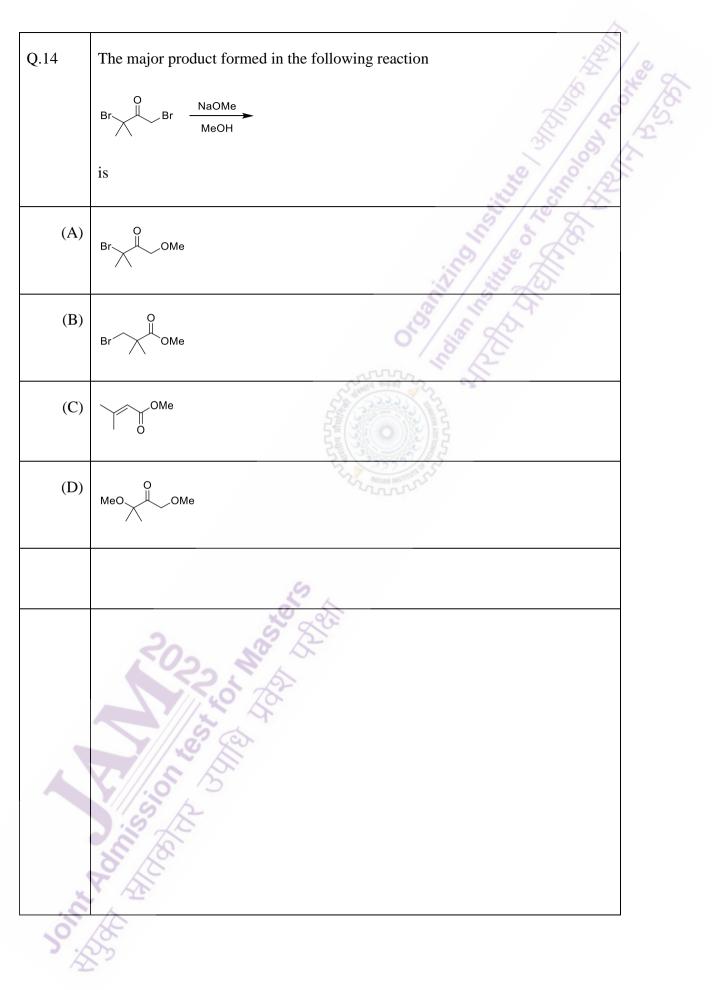


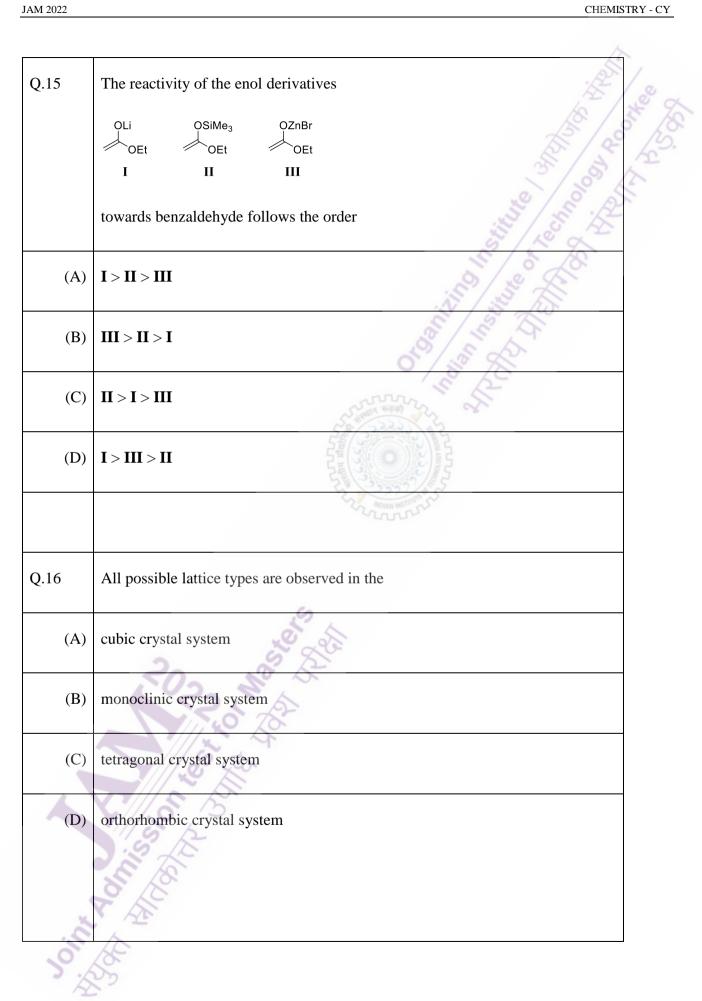




	A
Q.13	The major product formed in the reaction of $(2S,3R)$ -2-chloro-3-phenylbutane
	with NaOEt in EtOH is
(A)	(E)-2-phenyl-but-2-ene
(B)	(Z)-2-phenyl-but-2-ene
(-)	
(C)	3-phenyl-but-1-ene
	The second second
(D)	(2 <i>R</i> ,3 <i>R</i>)-2-ethoxy-3-phenylbutane
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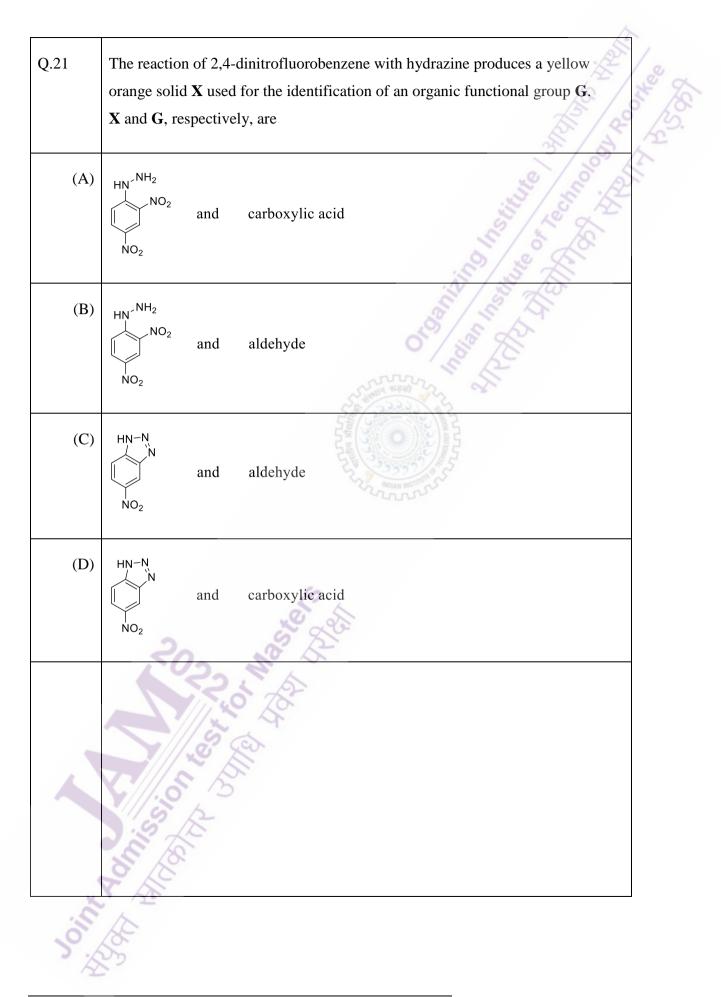


Q.17	The structure types of $B_{10}H_{10}^{2-}$ and $B_{10}H_{14}$, respectively, are	The of
(A)	closo and nido	15
(B)	nido and arachno	
(C)	nido and closo	
(D)	closo and arachno	
	STATUT SEE	
Q.18	The ground state and the maximum number of spin-allowed electronic	
	transitions possible in a Co ²⁺ tetrahedral complex, respectively, are	
(A)	⁴ A ₂ and 3	
(B)	⁴ T ₁ and 2	
(C)	⁴ A ₂ and 2	
(D)	⁴ T ₁ and 3	
	10,58,00 10,58,00 10,58,00	
Ŭ.		
5.4		



Q.19	The correct statement about the geometries of BH_2^+ and NH_2^+ based on valence
	shell electron pair repulsion (VSEPR) theory is
(A)	both BH_2^+ and NH_2^+ are trigonal planar
(B)	BH_2^+ is linear and NH_2^+ is trigonal planar
(C)	BH_2^+ is trigonal planar and NH_2^+ is linear
(D)	both BH_2^+ and NH_2^+ are linear
	MICIAN INSTITUTE
Q.20	The order of increasing CO stretching frequencies in $[Co(CO)_4]^-$, $[Cu(CO)_4]^+$, $[Fe(CO)_4]^{2-}$ and $[Ni(CO)_4]$ is
(A)	$[Cu(CO)_4]^+ < [Ni(CO)_4] < [Co(CO)_4]^- < [Fe(CO)_4]^{2-}$
(B)	$[Fe(CO)_4]^{2^-} < [Co(CO)_4]^- < [Ni(CO)_4] < [Cu(CO)_4]^+$
(C)	$[Co(CO)_4]^- < [Fe(CO)_4]^{2-} < [Cu(CO)_4]^+ < [Ni(CO)_4]$
(D)	$[Ni(CO)_4] < [Cu(CO)_4]^+ < [Co(CO)_4]^- < [Fe(CO)_4]^{2-1}$
14	No the
S	15°



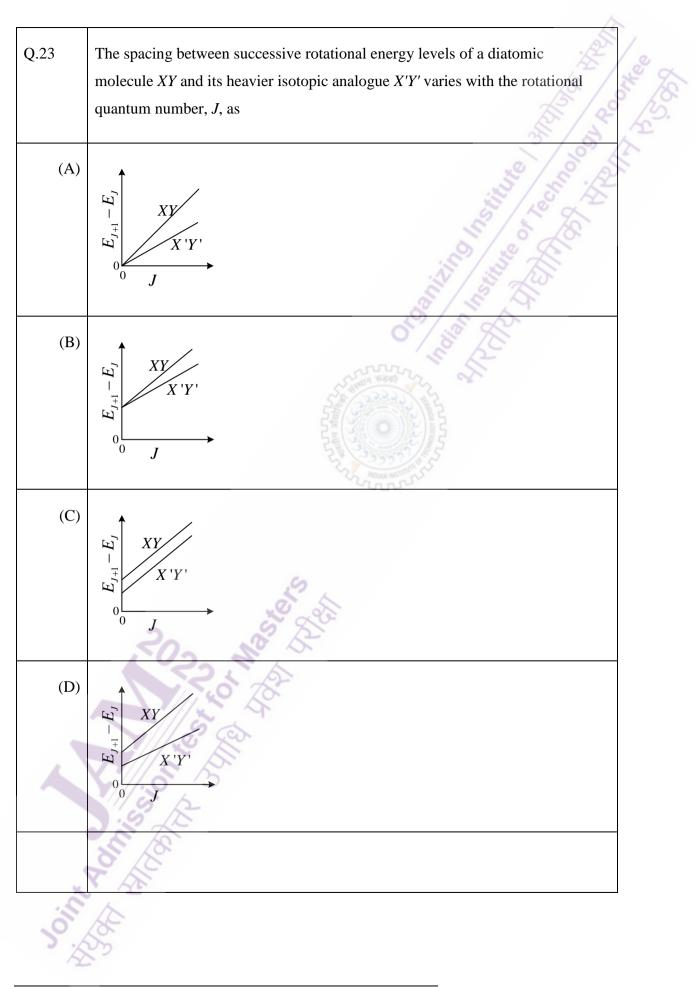


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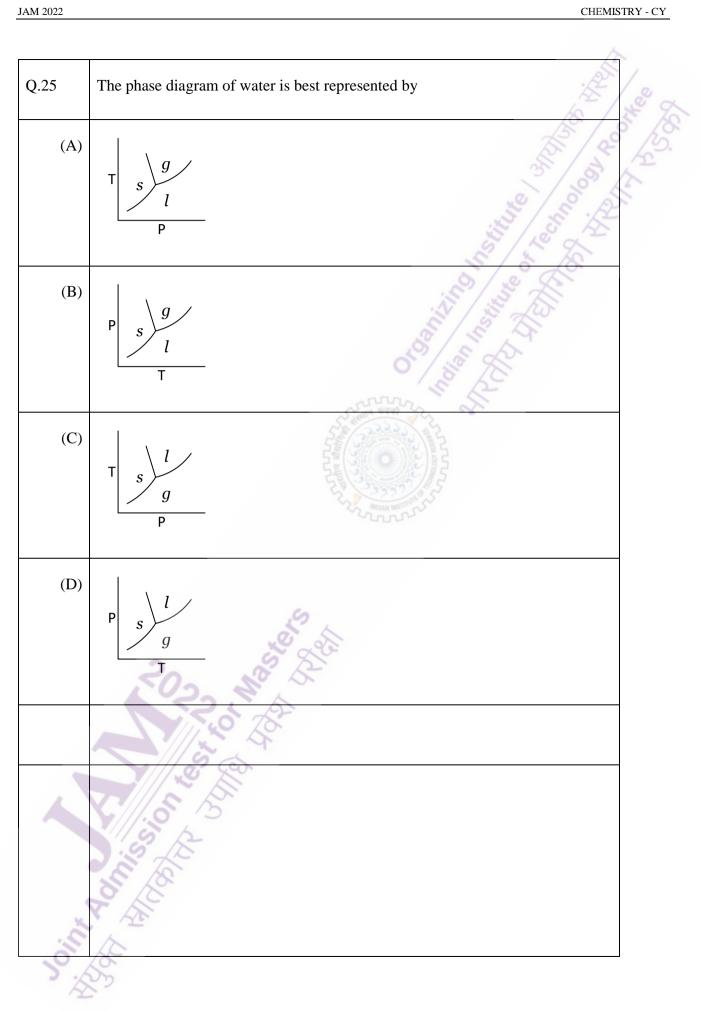
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Q.22	The stability of adducts $H_3B \cdot PF_3$, $H_3B \cdot NMe_3$, $H_3B \cdot CO$, $H_3B \cdot OMe_2$ follows the order
(A)	$H_{3}B \cdot OMe_{2} < H_{3}B \cdot CO < H_{3}B \cdot PF_{3} < H_{3}B \cdot NMe_{3}$
(B)	$H_{3}B \cdot PF_{3} < H_{3}B \cdot CO < H_{3}B \cdot NMe_{3} < H_{3}B \cdot OMe_{2}$
(C)	$H_{3}B \cdot CO < H_{3}B \cdot PF_{3} < H_{3}B \cdot NMe_{3} < H_{3}B \cdot OMe_{2}$
(D)	$H_{3}B \cdot PF_{3} < H_{3}B \cdot CO < H_{3}B \cdot OMe_{2} < H_{3}B \cdot NMe_{3}$
	2022 to the state
2*	Star Star
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	<u>A</u>
Q.24	The ratio of the $2p \rightarrow 1s$ transition energy in He ⁺ to that in the H atom is closest to
	15/00 15
(A)	
(B)	2
(C)	4
(D)	8
	Contraction of the second seco
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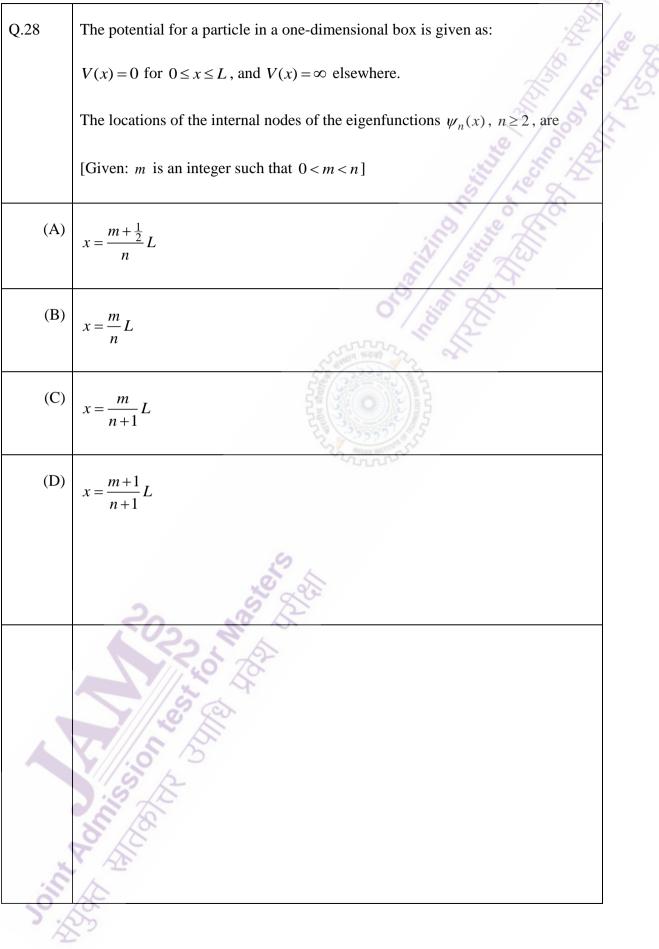
CHEMISTRY - CY

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Q.26	Capillary <i>W</i> contains water and capillary <i>M</i> contains mercury. The contact
	angles between the capillary wall and the edge of the meniscus at the air-liquid
	interface in W and M are θ_W and θ_M , respectively.
	The contact angles satisfy the conditions
	2 6 8
(A)	$\theta_W > 90^\circ$ and $\theta_M > 90^\circ$
	" " " " " " " " " " " " " " " " " " "
(B)	$\theta_W > 90^\circ$ and $\theta_M < 90^\circ$
(b)	$\sigma_W > 90$ and $\sigma_M < 90$
(C)	$\theta_W < 90^\circ \text{ and } \theta_M > 90^\circ$
	State and the
(D)	$\theta_W < 90^\circ$ and $\theta_M < 90^\circ$
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Q.27	The Maxwell-Boltzmann distribution $f(v_x)$ of one-dimensional velocities v_x
	at temperature T is
	[Given: A is a normalization constant such that $\int_{-\infty}^{\infty} f(v_x) dv_x = 1$, and k_B is the
	Boltzmann constant]
(A)	$A\exp(-mv_x^2/2k_BT)$
(B)	$A\exp(-mv_x^2/k_BT)$
(C)	$Av_x^2 \exp(-mv_x^2/2k_BT)$
(D)	$Av_x^2 \exp(-mv_x^2/k_BT)$
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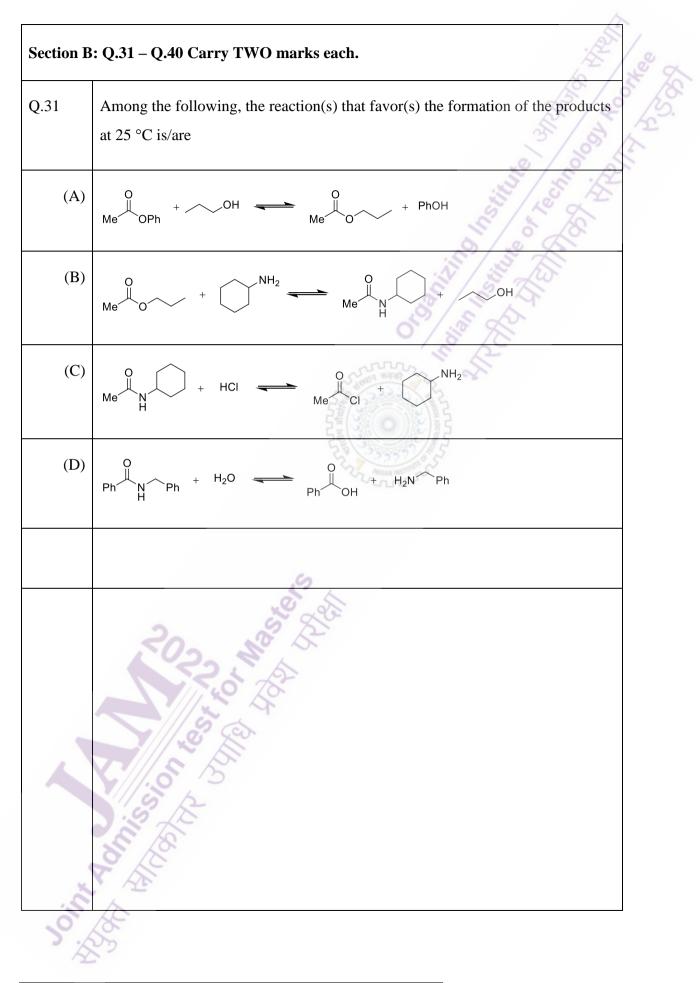


(A)	
(B)	2
(C)	3
(D)	
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Q.30	The standard Gibbs free energy change for the reaction
	$H_2O(g) \to H_2(g) + \frac{1}{2}O_2(g)$
	at 2500 K is +118 kJ mol ⁻¹ .
	The equilibrium constant for the reaction is
	[Given: $R = 8.314 \text{ J K}^{-1} \text{ mol}^{-1}$]
(A)	0.994
(B)	1.006
(C)	3.42×10^{-3}
(D)	292.12
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Q.32	Among the following, the correct statement(s) is/are:
(A)	The first pK_a of malonic acid is lower than the pK_a of acetic acid while its second pK_a is higher than the pK_a of acetic acid.
(B)	The first pK_a of malonic acid is higher than the pK_a of acetic acid while its second pK_a is lower than the pK_a of acetic acid.
(C)	Both the first and the second pK_a s of malonic acid are lower than the pK_a of acetic acid.
(D)	Both the first and the second pK_as of malonic acid are higher than the pK_a of acetic acid.
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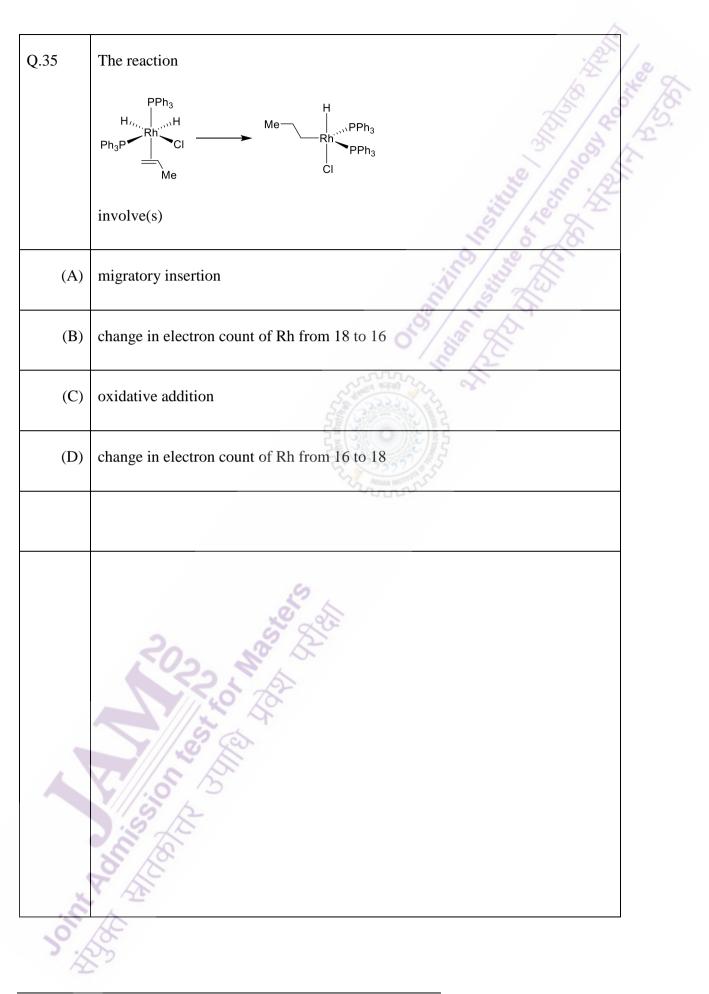






Q.34	Among the following, the suitable route(s) for the conversion of benzaldehyde to acetophenone is/are
(A)	CH ₃ COCl, anhydrous AlCl ₃
(B)	(i) $HS(CH_2)_3SH$, $F_3B \cdot OEt_2$; (ii) n-BuLi; (iii) MeI; (iv) $HgCl_2$, $CdCO_3$, H_2O
(C)	NaNH ₂ , MeI
(D)	(i) MeMgBr; (ii) aq. acid; (iii) pyridinium chlorochromate (PCC)
	and the second
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Q.36	The reason(s) for the lower stability of Si_2H_6 compared to C_2H_6 is/are	20
(A)	silicon is more electronegative than hydrogen	185.
(B)	Si–Si bond is weaker than C–C bond	
(C)	Si–H bond is weaker than C–H bond	
(D)	the presence of low-lying d-orbitals in silicon	
	ALL REAL PROPERTY AND	
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Q.37	For an <i>N</i> -atom nonlinear polyatomic gas, the constant volume molar heat
	capacity $C_{v,m}$ has the expected value of $3(N-1)R$, based on the principle of equipartition of energy. The correct statement(s) about the measured value of
	$C_{v,m}$ is/are
(A)	The measured $C_{v,m}$ is independent of temperature.
(B)	The measured $C_{v,m}$ is dependent on temperature.
(C)	The measured $C_{v,m}$ is typically lower than the expected value.
(D)	The measured $C_{v,m}$ is typically higher than the expected value.
	ADDIAN DISTUTION
Q.38	Zinc containing enzyme(s) is/are
(A)	carboxypeptidase
(B)	hydrogenase
(C)	carbonic anhydrase
(D)	urease
(D)	urease



Q.39	The conversion of ICl to ICl ⁺ involve(s)
(A)	the removal of an electron from a π^* molecular orbital of ICl
(B)	an increase in the bond order from 1 in ICl to 1.5 in ICl^+
(C)	the formation of a paramagnetic species
(D)	the removal of an electron from a molecular orbital localized predominantly on Cl
Q.40	The common point defect(s) in a solid is/are
(A)	Wadsley defect
(B)	Schottky defect
(C)	Suzuki defect
(D)	Frenkel defect
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Section C: Q.41 – Q.50 Carry ONE mark each.		
Q.41	Among the following	AS.
	the number of aromatic compounds is	
Q.42	The number of stereoisomers possible for the major product formed	
	in the reaction $\begin{array}{c} HBr\\ Ph \\ C \end{array} \xrightarrow{C+C+2} (1 \text{ equivalent})\\ H\end{array}$ is	
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Q.43	The number of signals observed in the ¹ H NMR spectrum of the compound	100
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	is	
	Or an Instant	
Q.44	The reaction of 122 g of benzaldehyde with 108 g of phenylhydrazine gave 157 g of the product $ \begin{array}{c} & & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ $	
	The yield of the product is%. (round off to the nearest integer)	
	Se de	
Q.45	The B–B bond order in B ₂ is	
Q.46	The number of unpaired electrons in $[Co(H_2O)_6]^{2+}$ is	
	Sur Contraction of the second se	
Q.47	The number of significant figures in 5.0820×10^2 is	
2	eres and a second se	



Q.48	The <i>d</i> spacing for the first-order X-ray ($\lambda = 1.54$ Å) diffraction event of metallic
	iron (fcc) at $2\theta = 20.2^{\circ}$ is Å. (round off to three decimal places)
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	10 20 20
Q.49	The volume fraction for an element in an <i>fcc</i> lattice is
	(round off to two decimal places)
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Q.50	A steady current of 1.25 A is passed through an electrochemical cell for
	1.5 h using a 12 V battery. The total charge, Q, drawn during this process
	is Coulombs. (round off to the nearest integer)
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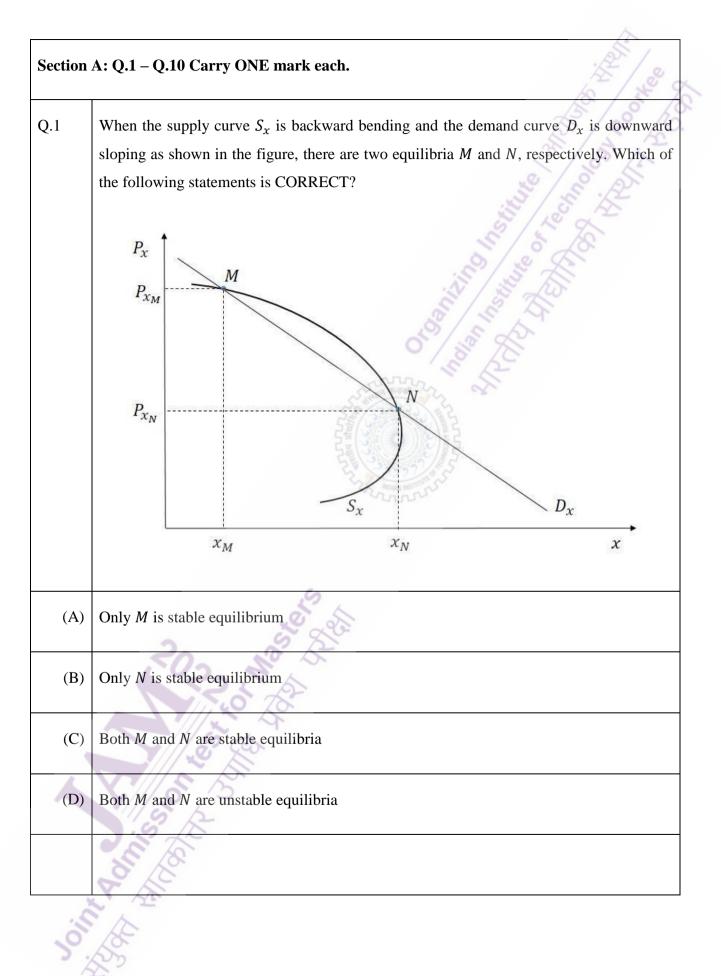
Section	C: Q.51 – Q.60 Carry TWO marks each.
Q.51	The specific rotation of optically pure (<i>R</i>)-1-phenylethylamine is +40 (neat, 20 °C). A synthetic sample of the same compound is shown to contain 4:1 mixture of (<i>S</i>)- and (<i>R</i>)-enantiomers. The specific rotation of the neat sample at 20 °C is (<i>round off to the nearest integer</i>)
	All and
Q.52	The number of β particles emitted in the nuclear reaction $^{238}_{92}U \rightarrow ^{206}_{82}Pb$ is
	C and the second s
Q.53	Iron is extracted from its ore via the reaction $Fe_2O_3 + 3 CO \rightarrow 2 Fe + 3 CO_2$ The volume of CO (at STP) required to produce 1 kg of iron is liters. (round off to the nearest integer)
-	[Given: Atomic wt. of Fe = 56; assume STP to be 0 °C and 1 atm]
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	Total degeneracy (number of microstates) for a Ti ³⁺ ion in
	spherical symmetry is
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	2 2 2
Q.55	A galvanic electrochemical cell made of Zn ²⁺ /Zn and Cu ²⁺ /Cu half-cells
	produces 1.10 V at 25 °C. The ratio of $[Zn^{2+}]$ to $[Cu^{2+}]$ is maintained at 1.0.
	The ΔG° for the reaction when 1.0 mol of Zn gets dissolved is kJ.
	(round off to the nearest integer)
	[Given: Faraday's constant = 96485 C mol ^{-1}]
	L'étenne ceses
Q.56	At constant volume, 1.0 kJ of heat is transferred to 2 moles of an ideal gas at
	1 atm and 298 K. The final temperature of the ideal gas is K.
	(round off to one decimal place)
	[Given: $R = 8.314 \text{ J K}^{-1} \text{ mol}^{-1}$]
	5
	30 20 200
Q.57	Two close lying bands in a UV spectrum occur at 274 nm and 269 nm. The
	magnitude of the energy gap between the two bands is $___ cm^{-1}$.
	(round off to the nearest integer)
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Q.58	The pH of an aqueous buffer prepared using CH_3COOH and $CH_3COO^-Na^+$
	is 4.80.
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	The quantity $\frac{[CH_3COO^-] - [CH_3COOH]}{[CH_3COOH]}$ is
	(round off to three decimal places)
	1 2 2
	[Given: pK_a of CH_3COOH in water is 4.75]
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Q.59	At constant temperature, 6.40 g of a substance dissolved in 78 g of benzene
	decreases the vapor pressure of benzene from 0.125 atm to 0.119 atm.
	The molar mass of the substance is $\ g \text{ mol}^{-1}$.
	(round off to one decimal place)
	[Given: Mol. wt. of benzene = 78 g mol^{-1}]
	and
	20 22
Q.60	For a van der Waals gas, the critical temperature is 150 K and the
	critical pressure is 5×10^6 Pa. The volume occupied by each gas
	molecule is $\Å^3$.
	(round off to two decimal places)
	[Given: $R = 8.314 \text{ J mol}^{-1} \text{ K}^{-1}$, $N_A = 6.023 \times 10^{23}$]
	[Orven: $K = 0.514$ 5 mor K , $N_A = 0.025 \times 10^{-5}$]
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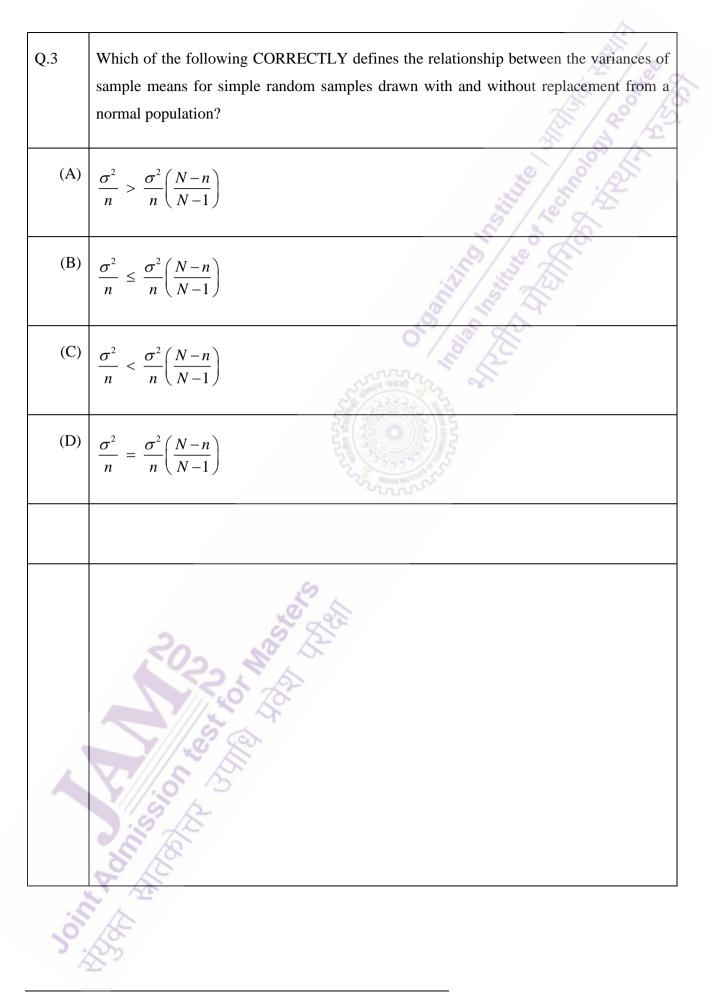




ECONOMICS - EN

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Q.2	Which of the following deficits indicates the true current fiscal position of the Indian Economy?
(A)	Revenue Deficit
(B)	Capital Deficit
(C)	Current Account Deficit
(D)	Primary Deficit
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Q.4	Suppose that one million unemployed persons in a country are receiving Rs. 6000 per
	month per person as an unemployment allowance. If the government, instead of paying
	unemployment allowance, hires all of them at the same amount (Rs. 6000 per month per
	person) and engages them in digging the pits and filling the same pits. What will be the
	effect on GDP?
(A)	No effect on GDP
(B)	GDP will rise.
(C)	GDP will fall.
(D)	The effect on GDP will be uncertain.
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Q.5	Which amendments to the constitution have provided constitutional status to the rural and urban local bodies in India?
(A)	80 th and 81 st Amendments
(B)	73 rd and 74 th Amendments
(C)	92 nd and 93 rd Amendments
(D)	71 st and 72 nd Amendments
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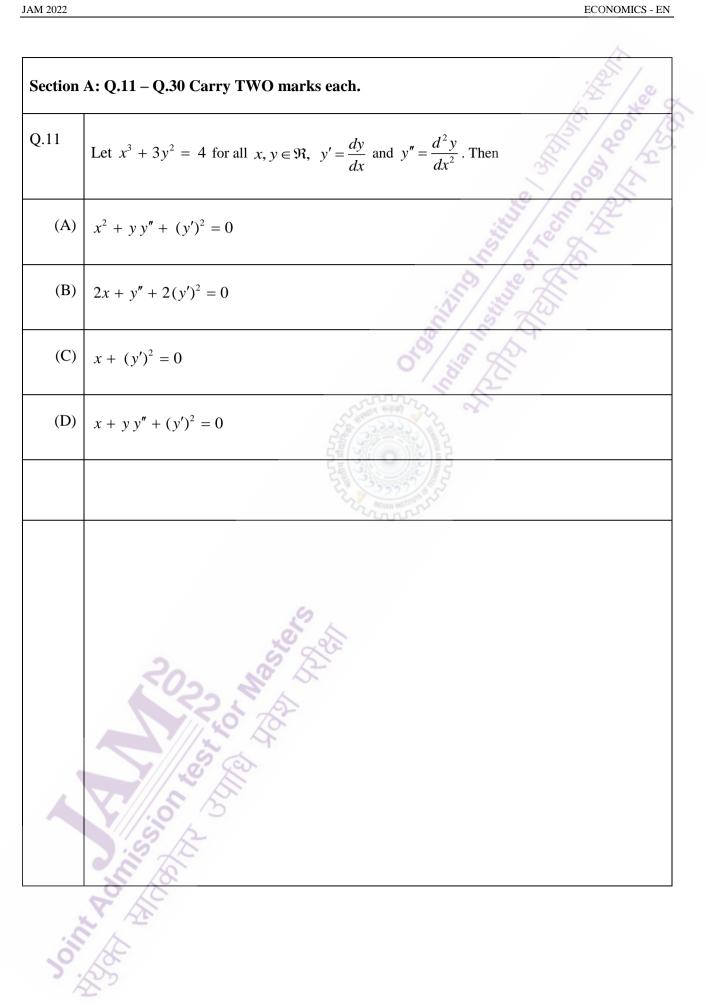
Q.6	Let W be a subspace of a vector space \Re^3 . Then, which of the following sets of vectors forms a basis of W?
(A)	(1, 2, 1) and (1, -2, 5)
(B)	(1, 3, 2), (1, -1, 0), (4, -1, 0) and (3, 1, -3)
(C)	(1, 1, 1), (1, 2, 3) and (2, -1, 1)
(D)	(1, -2, 1), (2, 1, -1) and (7, -4, 1)
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Q.7	From the following, who first examined the close negative relationship between the
	unemployment rate and the output ratio?
(A)	Alban W. Phillips
(B)	James Tobin
(2)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
(C)	Arthur M. Okun
	Set 12
(D)	Robert M. Solow
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Q.8	In the hypothesis testing, which of the following defines the size of power of the test?
(A)	1 – (Probability of accepting null hypothesis when it is true)
	2
(B)	1 – (Probability of rejecting null hypothesis when it is true)
	502 5
(C)	1 – (Probability of accepting null hypothesis when it is false)
(D)	1 + (Probability of rejecting null hypothesis when it is not true)
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Q.9	Which of the following is NOT a postulate of the Classical Model of full-employment equilibrium?
	2 00 10
(A)	Wage-Price flexibility
(B)	Perfect information about the market
(C)	Consumption and saving functions depend on income.
(D)	The price level moves proportionately with the quantity of money.
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Q.10	A long-run cost function for a product exhibits economies of scale if
(A)	average cost of production increases when the output increases.
(B)	the production function has decreasing returns to scale.
(C)	average cost of production falls as the output increases.
(D)	average cost of production remains constant as the output increases.
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		E.
Q.12	Match List I with List II and choose the CC	ORRECT option.
	List I	List II
	a. Second Five Year Plan (1956-61)	i. Towards Faster and More Inclusive Growth
	b. Fourth Five Year Plan (1969-74)	ii. Removal of Poverty and Attainment of Self-reliance
	c. Fifth Five Year Plan (1974-79)	iii. Rapid Industrialization–Heavy and Basic Industries
	d. Eleventh Five Year Plan (2007-12)	iv. Family Planning Programmes
		o list
(A)	(a, ii), (b, i), (c, iv), (d, iii)	AND COLOR
(B)	(a, iii), (b, iv), (c, i), (d, ii)	Contraction of the second seco
(C)	(a, iv), (b, iii), (c, ii), (d, i)	
(D)	(a, iii), (b, iv), (c, ii), (d, i)	
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~	(a, iii), (b, iv), (c, ii), (d, i)	
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Q.13	Let $f:[0,\infty) \to \Re$ be a function defined by $f(x) = \frac{x+1}{x+2}$ for all $x \in \Re$. Then f is
(A)	one-one and onto.
(B)	one-one but not onto.
(C)	onto but not one-one.
(D)	neither one-one nor onto.
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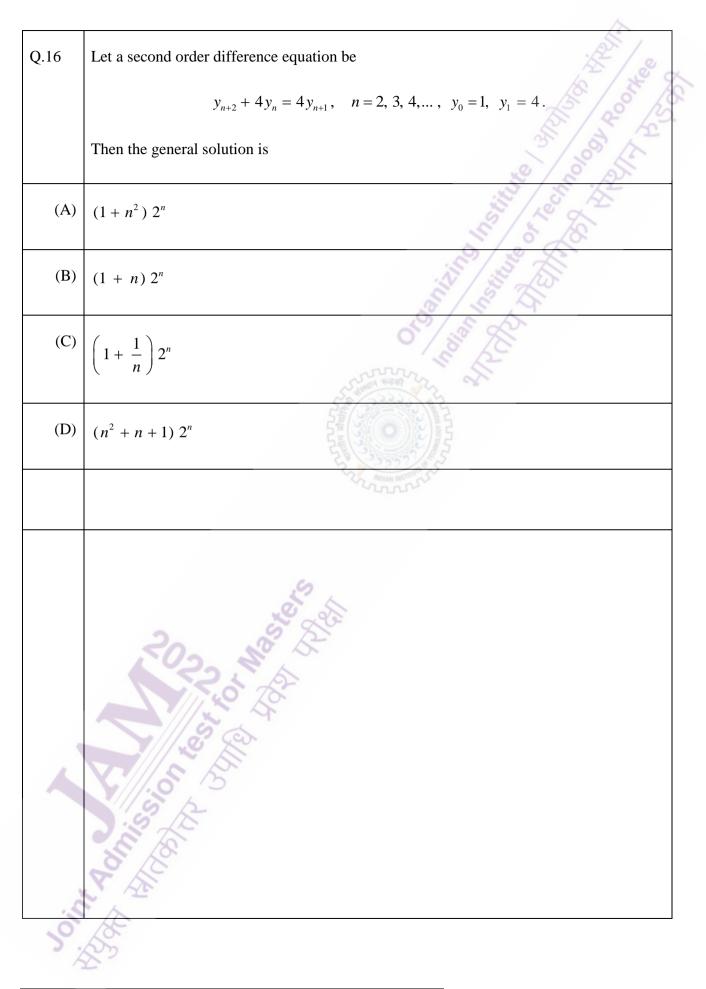


Q.14	An economy is characterized by the Solow model, with the production function $y = \sqrt{k}$,
	where y is output per worker and k is capital per worker. The steady-state level of output
	per worker is $y^{ss} = A^{1/(1-\alpha)} \left(\frac{\gamma}{\delta}\right)^{\alpha/(1-\alpha)}$, where A, γ, δ and α denote productivity,
	share of output invested (in %), depreciation rate (in %) and capital's share in income (in
	fraction), respectively. Suppose that $A = 1$, $k = 400$, $\gamma = 50\%$, $\delta = 5\%$ and $\alpha = 1/2$.
	Then the current output, using the above information, is
(A)	above the steady-state level of output per worker.
(B)	at the steady-state level of output per worker.
(C)	below the steady-state level of output per worker.
(D)	at the Golden Rule level.
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Q.15	Which of the following is NOT related to the structural adjustment programmes implemented in India after 1991?
(A)	Deregulation
(B)	Quantitative restrictions on trade
(C)	Fiscal austerity
(D)	Reduction of subsidies
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Q.17 Suppose that two random samples of sizes n_1 and n_2 are selected without replacement from two binomial populations with means $\mu_1 = n_1 p_1$, $\mu_2 = n_2 p_2$ and variances $\sigma_1^2 = n_1 p_1 q_1$, $\sigma_2^2 = n_2 p_2 q_2$, respectively. Let the difference of sample proportions \overline{P}_1 and \overline{P}_2 approximate a normal distribution with mean $(p_1 - p_2)$. Then the standard deviation of the difference of sample proportions \overline{P}_1 and \overline{P}_2 is (A) $\sqrt{\left(\frac{p_1 q_1}{n_1}\right) \left(\frac{N_1 - n_1}{N_1 - 1}\right) + \left(\frac{p_2 q_2}{n_2}\right) \left(\frac{N_2 - n_2}{N_2 - 1}\right)}$ (B) $\left(\frac{p_1 q_1}{n_1}\right) + \left(\frac{p_2 q_2}{n_2}\right)$ (C) $\frac{p_1 q_1 - p_2 q_2}{n_1 + n_2}$ (D) $\frac{p_1 q_1}{n_1 + n_2} \left(\frac{N_1 - n_1}{N_1 - 1} \right) + \left(\frac{p_2 q_2}{n_1 + n_2} \right) \left(\frac{N_2 - n_2}{N_2 - 1} \right)$



Q.18	Which of the following statements is NOT correct in the context of quantity theory of money?
(A)	The quantity of money available determines the price level in the economy.
(B)	The growth rate in the quantity of money available determines the inflation rate in the economy.
(C)	The velocity of money must rise with the increase in the quantity of money in the economy.
(D)	The economy's output is determined by factor supplies and technology, because money is neutral.
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Q.19	Let the function $f : \Re^2 \to \Re$ be $f(x, y) = \frac{xy^2}{x^3 + 2x^2y + y^3}$, $f(0, 0) = 0$. Then
(A)	f is differentiable at (0, 0).
(B)	f_x does not exist at (0, 0).
(C)	f_y does not exist at (0, 0).
(D)	f is not continuous at $(0, 0)$.
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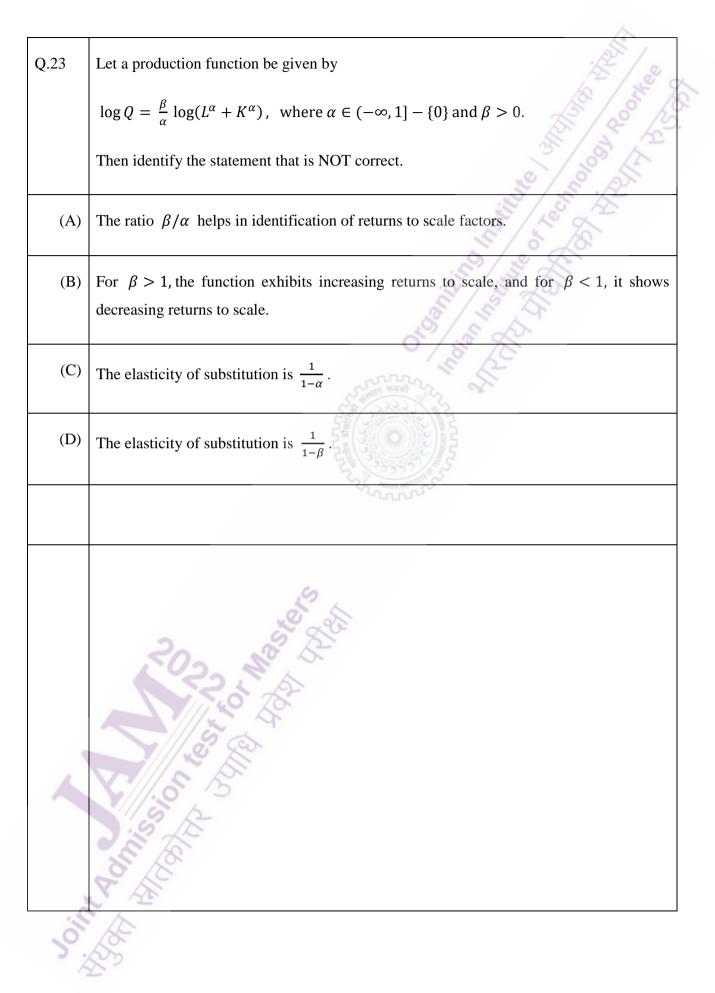
Q.20	Which of the following measures was announced by the Government of India in the year 1994?
(A)	Full convertibility on capital account
(B)	Full convertibility on current account
(C)	Constitution of the Narasimham Committee on banking sector reforms
(D)	Constitution of the Abid Hussain Committee on trade policies
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Q.21	An analyst at the Green Car Co. Ltd. estimated the following demand function for the electric vehicles it sells:
	$Q_E = 0.75 - 1.5P_E + 2.5P_F - 0.5P_B + 3.2I$
	where Q_E = Number of electric vehicles (in thousand per year), P_E = Unit price of electric vehicle (Rs. in Lakh), P_F = Average unit price of vehicle using fossil fuels (Rs. in Lakh), P_B = Unit price of battery used in electric vehicle (Rs. in Lakh), I = Personal disposable income (Rs. in Lakh).
	Let P_E = Rs. 6.5 Lakh, P_F = Rs. 4.5 Lakh, P_B = Rs. 0.5 Lakh and I = Rs. 10 Lakh. Then the income elasticity of demand (e_{Q_EI}) and the cross price elasticity of demand ($e_{Q_EP_F}$) satisfy
(A)	$0.98 \le e_{Q_E I} \le 0.99$ and $0.33 \le e_{Q_E P_F} \le 0.34$
(B)	$0.94 \le e_{Q_E I} \le 0.95$ and $0.45 \le e_{Q_E P_F} \le 0.46$
(C)	$0.98 \le e_{Q_E I} \le 0.99$ and $0.45 \le e_{Q_E P_F} \le 0.46$
(D)	$0.94 \le e_{Q_E I} \le 0.95$ and $0.33 \le e_{Q_E P_F} \le 0.34$
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Q.22 Choose the option that represents the original linear programming problem based on the initial simplex tableau given below, where S_i represents slack/surplus variables and A_i represents the artificial variables corresponding to the *i*th constraint: -M15 25 0 -M0 C_{i} S_3 X_b b S_1 A_1 A_2 х y 20 7 -M A_1 6 - 1 1 0 0 3 -21 -M A_2 18 0 0 0 30 8 0 0 0 0 S_3 5 1 38M -10M-4MZj M -MM0 15 + 10M25 + 4M $C_j - Z_j$ М 0 0 0 (A) Minimize Z=15x+25ysubject to $7x + 6y \ge 20$, $3x - 2y \le 18$, $8x + 5y \le 30$; $x, y \ge 0$. **(B)** Maximize Z = 15x + 25ysubject to $7x + 6y \ge 20, \ 3x - 2y = 18, \ 8x + 5y \le 30; \ x, y \ge 0.$ (C) Minimize Z=15x+25ysubject to $7x + 6y \ge 20$, 3x - 2y = 18, $8x + 5y \ge 30$; $x, y \ge 0$. Maximize Z = 15x + 25y(D) $7x + 6y = 20, \ 3x - 2y = 18, \ 8x + 5y \le 30; \ x, y \ge 0.$ subject to







Q.24	Which of the following statements is NOT correct under the IS-LM (Fixed Price) model?
(A)	The LM curve represents the combinations of income and interest rate, where money market is in equilibrium.
(B)	The IS curve represents the combinations of income and interest rate, where product market (goods and services) is in equilibrium.
(C)	An increase in money supply raises income and reduces interest rate when the IS curve has negative slope and the LM curve has positive slope.
(D)	Monetary policy has a relatively weak effect on income when the interest responsiveness of the demand for money is relatively low.
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Q.25	The probability of getting head in a toss of a biased coin is $\frac{2}{3}$. Let the coin be tossed three
	times independently. Then the probability of getting head in the first two tosses and tail in
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	the final toss is
(A)	4
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(B)	
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	5 5
(C)	2
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(D)	23
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Q.26 Consider a pure exchange economy with two goods x and y. Ravi and Suraj are two individuals with utility functions
$$U_R = \beta \log(xy)$$
 and $U_S = \left(\frac{x}{y}\right)^{\alpha}$, respectively. The endowments are x_R and y_R for Ravi and x_S and y_S for Suraj such that $x_R + x_S = A$ and $y_R + y_S = B$. Then their contract curve is
(A) $Ay_R - Bx_R = 0$
(B) $Ay_R + Bx_R - 2y_R x_R = 0$
(C) $Ay_R + Bx_R - y_R x_R = 0$
(D) $Ay_R - Bx_R + 2y_R x_R = 0$



Q.27	Which of the following is NOT correct regarding <i>R</i> -squared (R^2) and Adjusted <i>R</i> -squared (\overline{R}^2) ?
(A)	R^2 is a scale invariant statistic.
(B)	\overline{R}^2 is always positive.
(C)	R^2 tends to increase if we add an additional explanatory variable.
(D)	$\overline{R}^2 = 1 - (1 - R^2) \left(\frac{n - 1}{n - k}\right)$, where k is the number of parameters and n is the number of
	observations.
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Q.28	The technical change in the endogenous growth model is endogenized by
(A)	providing incentives to firms to innovate.
(B)	making the saving function dependent on income.
(C)	introducing constraints in capital accumulation.
(D)	assuming a perfectly competitive market structure.
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Q.29	Which of the following statements is COF	RECT for Game A and Game B?
	Game A: Mary wants to watch a movieand John is interested in watching afootball match. Both wish to betogether. The payoff matrix is:JohnMovieFootballMovieFootballMovieFootball(0,0)(1,2)	Game B: The Prisoner's dilemma problem is shown below: Convict 2 Do not confess Confess Do not confess Confess (-1,-1) (-9,0) (0,-9) (-5,-5)
		and the second second
(A)	In Game A , (Movie, Football) and (F In Game B , (Do not confess, Do not confe	Football, Movie) represent Nash equilibrium. ess) is the Nash Equilibrium.
(B)	In Game B , (Confess, Confess) is not a N Football) and (Football, Movie) represent	Vash equilibrium but in Game A , both (Movie, Nash equilibrium.
(C)	In Game B , the Nash equilibrium is (Do r	not confess, Do not confess).
(D)	In Game A, both (Movie, Movie) and (I In Game B, the Nash equilibrium is (Con	Football, Football) represent Nash equilibrium. fess, Confess).
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Q.30	The short-run production function of a firm is $Q = 200 + 0.2L^2 - 0.0004L^3$. If wage rate
	equals Rs. 140 and the number of labours (L) is 100, then the Marginal Cost and the
	Average Variable Cost, respectively, are
(A)	5 and 7.78
(B)	6 and 7.78
(C)	5 and 6.68
(D)	6 and 6.68
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Section	Section B: Q.31 – Q.40 Carry TWO marks each.	
Q.31	Let $X \sim N(\mu_X, \sigma_X^2)$ and $Y \sim N(\mu_Y, \sigma_Y^2)$. Which of the following is/are NOT correct?	
(A)	The area $F(X) = \frac{1}{\sigma_X \sqrt{2\pi}} \int_{-\infty}^{\mu_X} e^{-\frac{1}{2} \left(\frac{X-\mu_X}{\sigma_X}\right)^2} dx$ is 1.	
(B)	The areas under the normal probability curve between the ordinates at $\mu_x \pm 3\sigma_x$ and $\mu_y \pm 2\sigma_y$ are 0.9544 and 0.9973, respectively.	
(C)	For variable <i>X</i> ,	
	Quartile Deviation : Mean Absolute Deviation : Standard Deviation $\cong \frac{2}{3}\sigma_x:\frac{4}{5}\sigma_x:\sigma_x$	
(D)	If X and Y are independent, then $(X - Y) \sim N(\mu_X - \mu_Y, \sigma_X^2 + \sigma_Y^2)$.	
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	If X and Y are independent, then $(X - Y) - N(\mu_X - \mu_Y, \sigma_X + \sigma_Y)$.	
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Matching List I and List II, choose the CORRECT option(s). Q.32 List I List II Bombay Plan J. P. Narayan i. a. People's Plan b. ii. J. R. D. Tata Sarvodaya Plan iii. M. N. Roy c. (A) (a, i), (b, iii) **(B)** (a, ii), (b, iii) (C) (b, iii), (c, i) (D) (a, ii), (c, iii) all the set St Sold



Q.33 Suppose that the regression model is $Y_i = \beta_0 + \beta_1 X_{1i} + \beta_2 X_{2i} + \mu_i$, i = 1, 2, ..., n. Which of the following null hypotheses could be tested using the F-test? $\beta_1/\beta_2 = 0$ (A) $\beta_0 = 0$ (B) $\beta_1 \beta_2 = 0$ (C) $\beta_1 = \beta_2 = 0$ (D) o to to



Q.34 Let f be defined by
$$f(x) = |x| + \left| \cos\left(\frac{\pi}{2} - x\right) \right|, x \in \left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$$
. Then
(A) f is continuous on $\left(-\frac{\pi}{2}, 0\right) \cup \left(0, \frac{\pi}{2}\right)$.
(B) f is differentiable at $x = 0$.
(C) f is differentiable everywhere except $x = 0$.
(D) $\lim_{x \to 0} f(x) = 0$.



Q.35	The real exchange rate is given by $e = EP/P^*$, where <i>e</i> is the price of domestic goods in
	terms of foreign goods, E is the price of domestic currency in terms of foreign currency,
	P is the domestic price level, P^* is the foreign price level. If the Indian Rupee depreciates
	vis-à-vis the Japanese Yen, and the Marshall-Lerner condition holds, then
(A)	India's imports will increase.
(B)	India's trade balance will improve.
(C)	foreign demand for Indian goods will increase.
(D)	foreign demand for Indian goods will decrease.
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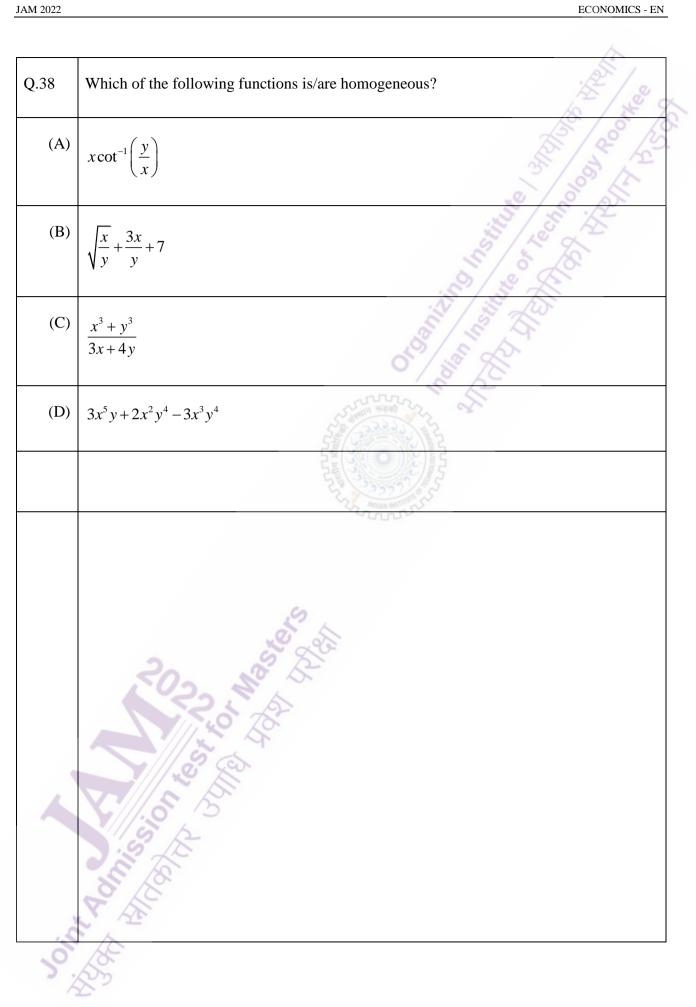


Q.36	The demand function (Q_x^D) and supply function (Q_x^S) are given as:
	$Q_x^D = f(P_x, I)$ and $Q_x^S = g(P_x, A)$
	where I (Income) and A (Advertisement expenses) are the exogenous factors affecting
	quantity demanded and supplied, respectively. Further, $\frac{\partial f}{\partial P_x} < 0$, $\frac{\partial g}{\partial P_x} > 0$ but $\frac{\partial f}{\partial I}$ and
	$\frac{\partial g}{\partial A}$ may have any sign. Considering that there exists an equilibrium $(Q_x^D = Q_x^S = Q)$,
	which of the following is/are CORRECT?
(A)	$e_{P_{\chi}A} = \left(\frac{\partial g}{\partial A} \frac{A}{Q}\right) / \left(\frac{\partial f}{\partial P_{\chi}} \frac{P_{\chi}}{Q} - \frac{\partial g}{\partial P_{\chi}} \frac{P_{\chi}}{Q}\right)$
(B)	$\frac{dP_x}{dA} = \left(\frac{\partial g}{\partial A}\right) / \left(\frac{\partial f}{\partial P_x} - \frac{\partial g}{\partial P_x}\right)$
(C)	$e_{P_{\chi}I} = \left(\frac{\partial g}{\partial I} \frac{I}{Q}\right) / \left(\frac{\partial f}{\partial P_{\chi}} \frac{P_{\chi}}{Q} - \frac{\partial g}{\partial P_{\chi}} \frac{P_{\chi}}{Q}\right)$
(D)	The sign of $\frac{dP_x}{dA}$ does not depend on $\frac{\partial g}{\partial A}$.
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	The sign of $\frac{d_1 x}{dA}$ does not depend on $\frac{d_2}{\partial A}$.
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Q.37	Which of the following statements is/are CORRECT under the Keynesian Cross (Fixed Price) Model?
(A)	The product market and factor market independently determine the full-employment level of output.
(B)	Output is determined in the product market by the aggregate expenditure.
(C)	Money market determines the price level, given the quantity of money and the level of output.
(D)	Employment is determined in the factor market by the output level determined in the product market.
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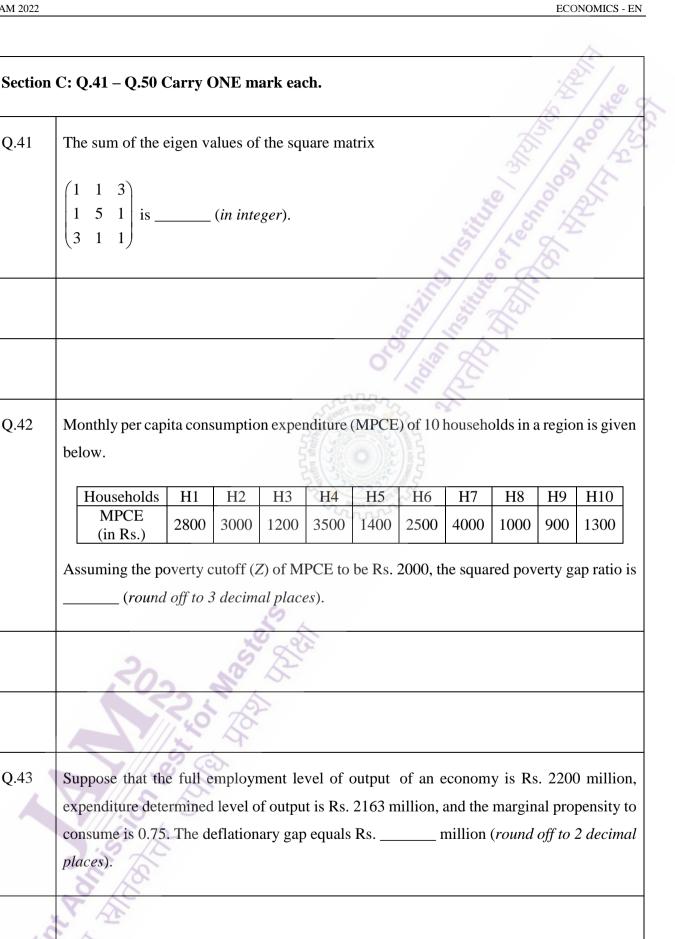
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Q.39	In the context of Indian agriculture, which of the following statements is/are CORRECT?
(A)	NABARD was established in 1982.
(B)	One of the objectives of setting up of the CACP was to ensure remunerative prices to farmers.
(C)	The APMC Act is related to institutional credit supply in agriculture.
(D)	The National Commission on Agriculture was chaired by V. M. Dandekar.
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Q.40	Let a monopolist demand curve be given by $Q = P^e$, where Q is output, P is price, e is
	the price elasticity of demand ($e < -1$), and Marginal Cost = Average Cost = α . If P_c and
	P_M represent the price under perfect competition and monopoly, respectively, then which
	of the following is/are NOT correct?
	000
	$(CS_M \text{ and } CS_C \text{ represent the consumer surplus under monopoly and perfect competition,}$
	respectively.)
(A)	$P_C = \alpha \left(\frac{e}{1+e}\right)$
(B)	$P_M = \alpha \left(\frac{e}{1+e}\right)$
(C)	For $e = -2$, $CS_M = CS_C$.
(D)	For <i>e</i> closer to -1 , the ratio CS_M/CS_C increases.
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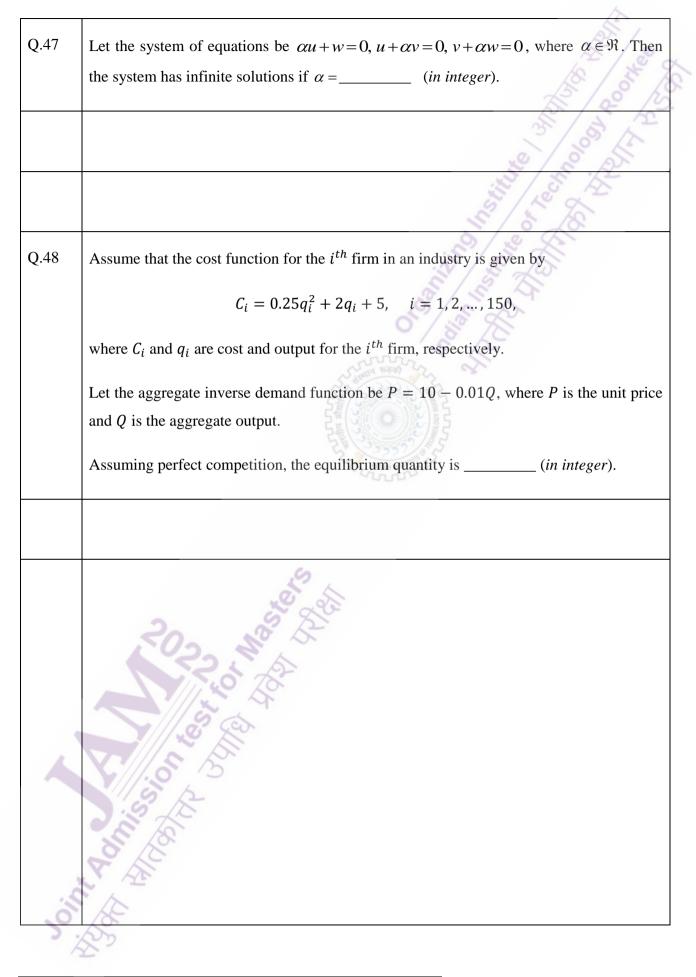
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Q.44	Let $a, b \in \Re$. If $f(x) = ax + b$ is such that
	$a+b=4$ and $f(x+y) = f(x)+f(y)-2$ for all $x, y \in \Re$,
	then $\sum_{n=1}^{50} f(n) = $ (in integer).
	$\lim_{n \to 1} \sum_{n=1}^{n} f(n) = \underline{\qquad} (n \text{ imager}).$
	Stitute Stitute
	all
Q.45	The Total Variable Cost (TVC) for a firm is given by $TVC = x^3 - bx^2$. The Total Fixed
	Cost is 848.
	The value of <i>b</i> for which the Marginal Cost is minimum at $x = 16$ is (<i>in integer</i>).
	"Vann"
	2
Q.46	Let the consumption function, tax function, and income identity be given by
	$C = C_0 + b(Y - T)$, $T = T_0 + tY$, and $Y = C + I_0 + G_0$, respectively, where C_0 , I_0 ,
	G_0 , and T_0 are autonomous consumption, investment, government expenditure, and tax,
	all and the addition of the ad
	respectively. If $b = 0.75$ and $t = 0.1$, then an increase in G_0 by Rs. 20 million will
-	respectively. If $b = 0.75$ and $t = 0.1$, then an increase in G_0 by Rs. 20 million will
	respectively. If $b = 0.75$ and $t = 0.1$, then an increase in G_0 by Rs. 20 million will
	respectively. If $b = 0.75$ and $t = 0.1$, then an increase in G_0 by Rs. 20 million will
	respectively. If $b = 0.75$ and $t = 0.1$, then an increase in G_0 by Rs. 20 million will



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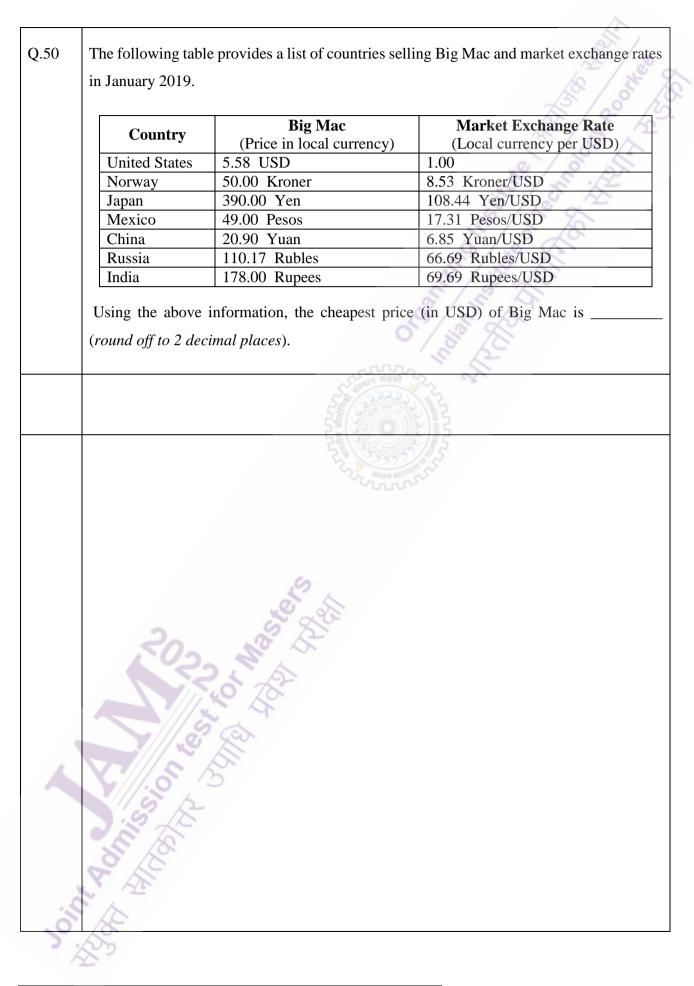




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the year 2		25/20
	National income related aggregates	Rs. Lakh Crores
Net	factor income earned abroad	1.S. 21
Priva	ate income	17.
GNF	P at factor cost	5 21
	P at factor cost	19
Reta	ined earnings of Nation's private sector	1
	borate tax	2.
	sehold direct tax	2
	onal income	14
Misc	cellaneous receipts of government administrative department	nts
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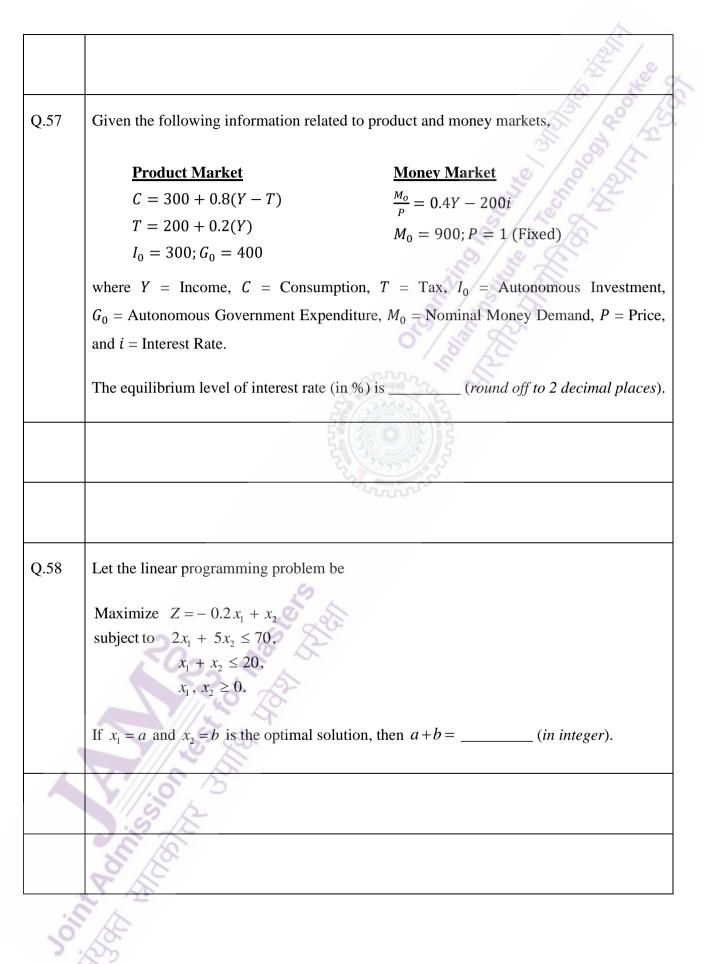


Section	C: Q.51 – Q.60 Carry TWO marks each.
Q.51	An individual faces an uncertain prospect, where wealth could be Rs. 10 Lakh with probability 0.75 and Rs. 7 Lakh with probability 0.25.
	Let the utility function be $U(w) = w^3$. Then the individual will buy full insurance by paying a premium of Rs Lakh (<i>round off to 2 decimal places</i>).
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Q.52	Suppose that per capita GDP of India and USA are growing at annual average rates of 8.8% and 1.8%, respectively. Further, consider that in 2019-20, per capita GDP of USA was USD 41099 and per capita GDP of India was USD 1570. Assuming that the two countries continue to grow at the above rates, India's per capita GDP will be equal to the per capita GDP of USA in years (<i>round off to 2 decimal places</i>).
	Sec.
Q.53	If $\int t \log\left(1 + \frac{2}{t}\right) dt = g(t)\left(\frac{t^2}{2} - 2\right) + f(t)\frac{t^2}{2} + Kt + C$, where <i>C</i> is an arbitrary constant, then 2 <i>K</i> is(<i>in integer</i>).
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Q.54 ACD Bank holds a total deposit of Rs. 256412. To expand the money supply in the economy during the COVID-19 pandemic period, the Reserve Bank of India reduces the cash reserve ratio (CRR) from 4.5% to 3.5%. Due to this policy change, the additional money supply generated by ACD Bank is Rs. _____ (*in integer*). regression model is $Y_{n \times 1} = X_{n \times 3} \beta_{3 \times 1} + U_{n \times 1}$ Q.55 Suppose that the with $\beta_{3\times 1} = \begin{bmatrix} \beta_1 & \beta_2 & \beta_3 \end{bmatrix}^T$. A random sample of size n = 23 on Y and X is drawn from the normal population. Using the data, if a researcher obtains $(X^T X)^{-1} = \begin{bmatrix} 0.3 & 0.5 & 0.8 \\ 0.4 & -0.6 & 0.2 \\ 0.4 & 0.5 & 0.3 \end{bmatrix}, \quad X^T Y = \begin{bmatrix} 0.3 & 0.2 & 0.1 \end{bmatrix}^T \text{ and } e^T e = 0.7,$ where e denotes the vector of estimated residuals, then the t-statistic to test the null hypothesis $\beta_3 = 0$ is _____ (round off to 2 decimal places). Given the production function $Q = 6\sqrt{L}$ and the supply of labour $L = \sqrt{w}$, where L and w Q.56 denote the number of labours and wage rate, respectively. If the unit price of the product is Rs. 243, then the profit maximizing value of w is Rs. _____ (*in integer*).







Q.59	Let the production function be $Q = \sqrt{L^2 + K^2}$, the unit price of labour (<i>L</i>) and capital (<i>K</i>) be Rs. 30 and Rs. 40, respectively, and the total cost be Rs. 580. Then the
	maximum value of Q subject to the cost constraint is (round off to 2 decimal
	places).
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Q.60	In a market, two firms F_1 and F_2 are producing homogenous products. The inverse demand function is given by $p = 120 - 0.5(q_1 + q_2)$, where p is the unit price of the product, and q_1 and q_2 are the outputs from F_1 and F_2 , respectively. Suppose the cost functions of
	F_1 and F_2 are $C_1 = 20q_1$ and $C_2 = 10 + 0.5q_2^2$, respectively. Then the total profit earned by both the firms assuming a competitive situation is (<i>in integer</i>).
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Section A: Q.1 – Q.10 Carry ONE mark each.		
	E S	a
Q.1	Which one of the following is a geochronologic unit?	185.
(A)	System	
(B)	Period	
(C)	Member	
(D)	Formation	
	ADIAN RECTITIVE AND	
Q.2	Which one of the following must have thickness less than 1 cm?	
(A)	Lamina	
(B)	Bed Cost and Cost	
(C)	Stratum	
(D)	Layer	
	Sing and a second	
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Q.3		became extinct during the Cretaceous-
	Tertiary mass extinction event?	12
(A)	Trilobite	5 3
		9 0 6
(B)	Ammonite	in the
(D)	Ammonite	12 12 25
		5/200
(C)	Brachiopod	IN IN THE
		the life
(D)	Echinoderm	5º 5 2
		2000
		State and the state
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	2.5×	33335
	Match the geomorphic features in Gro	up I with the related processes in
Q.4	Group II.	
	Group I	Group II
	P. Cirque	1. Fluvial
	Q. Ventifact	2. Glacial
	R. Point bar	3. Volcanic
	S. Tephra	4. Aeolian
(A)	P-2, Q-4, R-1, S-3	
(A)	1-2, Q-4, K-1, S-3	
(B)	P-2, Q-3, R-1, S-4	
	1 5 B	
(C)	P-4, Q-2, R-3, S-1	
	8 8	
(D)	P-1, Q-2, R-3, S-4	
(D)	1 -1, Q-2, N-3, S-4	
0	AS .	



Which one of the given textural features results from exsolution? Q.5 Ophitic (A) (B) Perthitic Graphic (C) Glomeroporphyritic (D) Q.6 In the holosymmetric class of the Cubic System, how many more faces does the {110} form have compared to the {111} form? 2 (A) (B) 4 (C) 6 8 (D)



	1	
Q.7	Which one of the following seismic waves involves compression and rarefaction (but not rotation) of the material that it passes through?	Solo Colo
(A)	P-waves	A.
(B)	S-waves	
(C)	Rayleigh waves	
(D)	Love waves	
	Contraction of the second seco	
Q.8	Realgar and orpiment are both minerals of arsenic (As) and have the same	
X .0	chemical composition. Which one of the following properties can be used to	
	distinguish between the two minerals in hand specimen?	
(A)	Lustre	
(B)	Hardness	
(C)	Colour	
(D)	Fracture	
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Q.9	Buckle folds result from
(A)	layer parallel shortening
(B)	layer perpendicular slip
(C)	layer parallel shearing
(D)	layer perpendicular shortening
	NUMBER OF THE OF
Q.10	Sandstone beds above a magmatic body are domal in shape, while the beds below are horizontal. The magmatic body is a
(A)	Batholith
(B)	Laccolith
(C)	Lopolith
(D)	Sill
	2. S. J.
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.11	Match the morphological features in Group I with the corresponding fossil		
	groups in Group II.	The second secon	
	Group I	Group II	
	P. Pedicle Foramen	1. Trilobita	
	Q. Pallial Sinus	2. Cephalopoda	
	R. Pygidium	3. Pelecypoda	
	S. Siphuncle	4. Brachiopoda	
(A)	P-4, Q-3, R-1, S-2	Croan Instant	
(B)	P-4, Q-1, R-2, S-3	A COSCINGT	
(C)	P-3, Q-4, R-1, S-2		
(D)	P-2, Q-1, R-4, S-3	ADDIAN INSTITUTE	
.12	The Triassic-Jurassic boundary lies wi stratigraphic units?	thin which one of the following	
(A)	Panchet Formation		
(B)	Dharmaram Formation		
(C)	Pachmarhi Formation		
(D)	Denwa Formation		



Q.13 Which one is the correct order of stability of the minerals (arranged from the most stable to the least stable) during chemical weathering? (A) Muscovite > Amphibole > Quartz > Olivine **(B)** Quartz > Amphibole > Olivine > Muscovite (C) Quartz > Muscovite > Amphibole > Olivine (D) Muscovite > Olivine > Quartz > Amphibole Match the following sedimentary rocks in Group I with their compositions in Q.14 Group II. Group I Group II P. Packstone 1. <15% matrix, > 25% rock fragments Q. Grainstone 2. >15% matrix, >25% feldspar R. Lithic arenite 3. Grain supported, contains no mud S. Arkosic wacke 4. Grain supported, contains mud P-4, Q-3, R-1, S-2 (A) (B) P-3, Q-4, R-2, S-1 P-3, Q-1, R-4, S-2 (C) P-2, Q-4, R-1, S-3 (D)



Q.15	Match the para Group II.	ameters in Group I with the	ir corresponding di	mensions in
		Group I	Group II	ALL AND
		P. Shear modulus	1. $M^{0}L^{0}T^{0}$	11000 Miles
		Q. Hydraulic conductivity	2. $M^{1}L^{-3}T^{0}$	the second
		R. Volumetric strain	3. $M^0L^1T^{-1}$	and the
		S. Dry density	4. $M^{1}L^{-1}T^{-2}$	The second
(A)	P-4, Q-3, R-1,	.S-2	A HOLE	
(B)	P-3, Q-1, R-2,	S-4		
(C)	P-2, Q-3, R-4,	S-1	ADIAN RETING	
(D)				
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Q.16	Match the countries in Group I with the plate tectonic features in Group II that cause seismic activity in them.		
	cause seisnine activity in them.	15 00	
	Group I	Group II	
	P. Iceland	1. Subduction Zone	
	Q. Indonesia	2. Transform Fault	
	R. Nepal	3. Mid-Oceanic Ridge	
	S. New Zealand	4. Continental Collision	
		o list for	
		and and the state	
(A)	P-3, Q-1, R-4, S-2		
(B)	P-3, Q-1, R-2, S-4	ADIAN INSTITUTE	
(C)	P-1, Q-3, R-4, S-2		
(D)	P-2, Q-1, R-4, S-3		
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	P-2, Q-1, R-4, S-3		
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Q.17	Which one of the magnitude scales given below DOES NOT saturate while estimating size of earthquakes?
	5
(A)	Local magnitude scale (M _L)
(B)	Body wave magnitude scale (M _b)
(C)	Surface wave magnitude scale (M _S)
(D)	Moment magnitude scale (M _W)
	States and
0.19	
Q.18	What is the minimum number of forms that an actual crystal must contain in Class 1 (Pedial) of the Triclinic System?
(A)	1
(B)	2 3023 10 2
(C)	3
(D)	4
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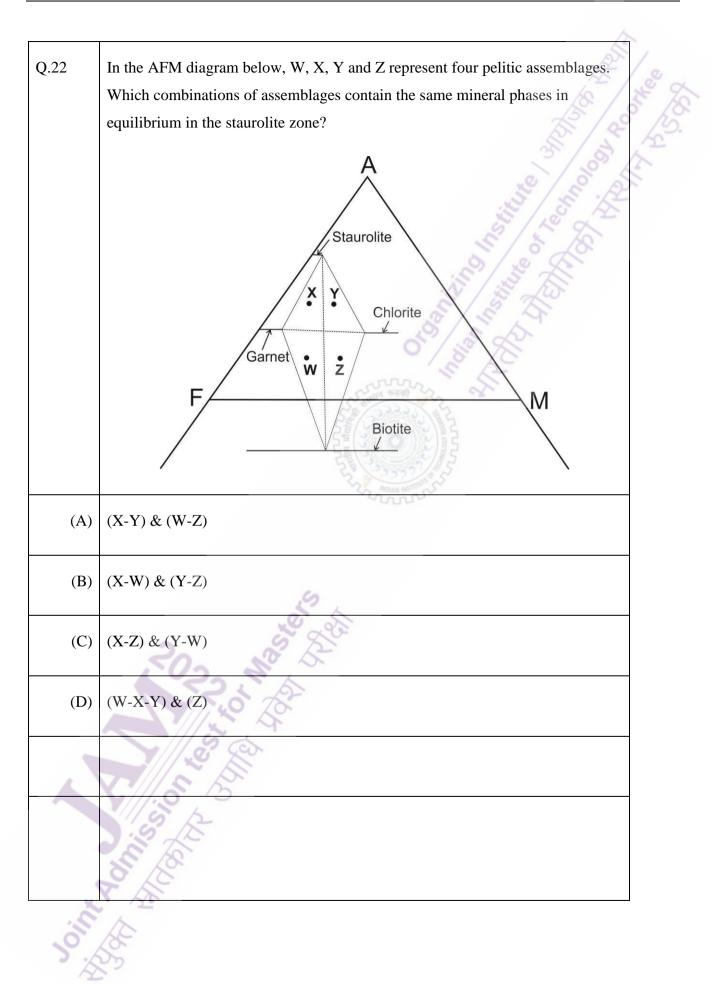


Q.19 The apparent dip of a plane is measured to be 45° towards NE. The true dip of the plane is 55° towards SSW (A) **(B)** 40° towards NNE (C) 48° towards ENE 40° towards E (D) Q.20 A horizontal upright fold will have a vertical fold axis and horizontal axial plane (A) horizontal fold axis and vertical axial plane (B) horizontal fold axis and axial plane with any dip (C) plunging fold axis on a vertical axial plane (D)



Q.21	The displacement of the bed shown in the figure below is caused by a single movement along fault XYZ. Of the options given below, which fault-type can
	explain the observed displacement?
	z
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	x
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(A)	Strike-slip
(B)	Reverse
	SE STORES
(C)	Normal
(D)	Trace-slip
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2	A C
55	SS SS

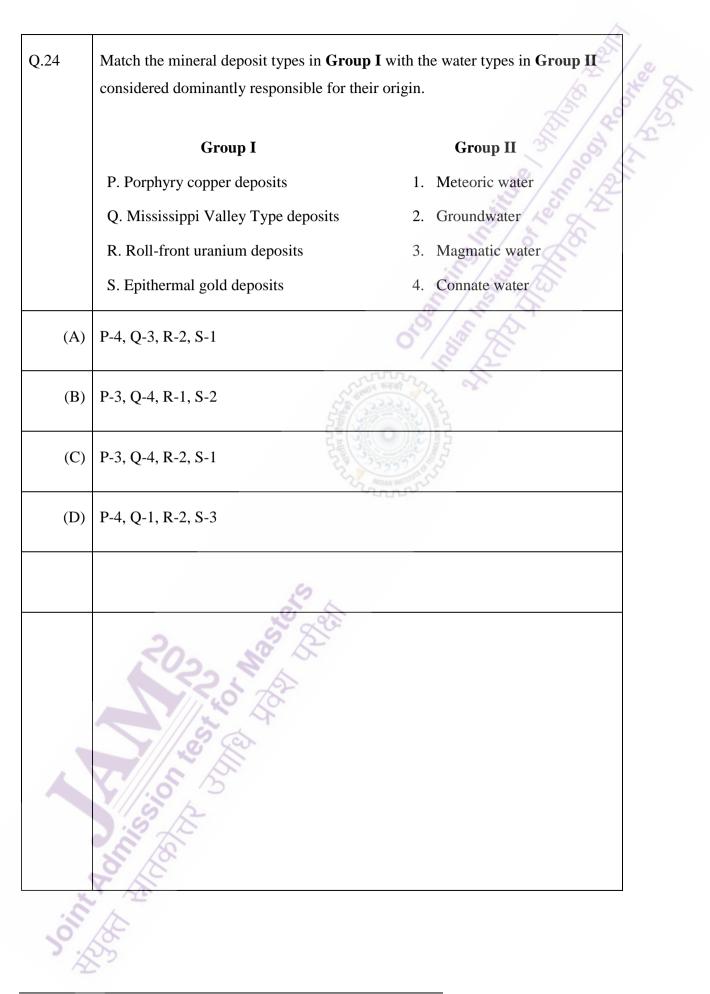






Q.23	Match the rock types in Group I with their characteristic mineral assemblages	
	in Group II .	1º
	Group I	Group II
	P. Diorite	1. plagioclase – orthopyroxene \pm clinopyroxene
	Q. Tonalite	2. olivine – orthopyroxene – clinopyroxene
	R. Norite	3. plagioclase – hornblende \pm quartz
	S. Lherzolite	4. quartz – plagioclase \pm K-feldspar
(A)	P-4, Q-3, R-2, S-1	NAME OF ALL
(B)	P-2, Q-1, R-3, S-4	
(C)	P-3, Q-4, R-1, S-2	ADIAN INSTITUTE
(D)	P-1, Q-3, R-4, S-2	
		See 20
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Q.25 Match the minerals in Group I with their optical properties in Group II. Group I **Group II** P. Sodalite 1. Mottled extinction Q. Tourmaline 2. Isotropic 3. Pleochroic from blue to brown R. Calcite S. Muscovite 4. Twinkling effect (A) P-4, Q-3, R-2, S-1 (B) P-2, Q-3, R-4, S-1 (C) P-3, Q-1, R-2, S-4 (D) P-1, Q-3, R-4, S-2 Q.26 The contact between the Talchir Formation and the underlying Precambrian basement is an angular unconformity (A) (B) a disconformity a paraconformity (C) a nonconformity (D)



Q.27	Increased diversity of siphonate bivalves occurred in response to
(A)	the Cambrian explosion in the Paleozoic
(B)	increased temperature in the Cenozoic
(C)	increased predation pressure in the Mesozoic
(D)	increased oxygen level in the Proterozoic
	NAME OF ALL ALL
Q.28	An index fossil should have
(A)	large geographic range and small temporal range
(B)	small geographic range and large temporal range
(C)	small geographic range and small temporal range
(D)	large geographic range and large temporal range
	5/10/2
nr.	Manie Marine
5.5	



Q.29	Match the formations in Group I with corresponding stratigraphic periods in Group II .	
	Group I	Group II
	P. Syringothyris Limestone	1. Permian
	Q. Karai Shale	2. Jurassic
	R. Chari	3. Carboniferous
	S. Barren Measures	4. Cretaceous
(A)	P-1, Q-2, R-3, S-4	Conic Conic
(B)	P-2, Q-4, R-1, S-3	A LE
(C)	P-3, Q-4, R-2, S-1	
(D)	P-4, Q-1, R-2, S-3	23532 Star
	and	
2.30	Which one of the given statements is corre	ect?
(A)	van der Waal's bonding is absent in silica	te minerals
(B)	Sulfide minerals form by covalent bondin	g between metal and sulfur
(C)	Silicate minerals have a significant compo	onent of metallic bonding
(D)	Metal-sulfide formation does not involve	splitting of d-orbitals



Section B	: Q.31 – Q.40 Carry TWO marks each.
Q.31	Which of the following structures form in marine environment?
(A)	Lateral accretionary surfaces
(B)	Hummocky cross stratification
(C)	Herringbone cross stratification
(D)	Barchanoids
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Q.32	Identify the correct stratigraphic successions ordered from oldest to youngest.
(A)	Papaghni Group - Kurnool Group - Nallamalai Group - Chitravati Group
(B)	Semri Group - Kaimur Group - Rewa Group - Bhander Group
(C)	Papaghni Group - Chitravati Group - Nallamalai Group - Kurnool Group
(D)	Semri Group - Rewa Group - Bhander Group - Kaimur Group
-	E C



Q.33 Which of the following stratigraphic units contain coal seams? (A) **Barakar** Formation (B) Lakadong Formation Pachmarhi Formation (C) (D) **Panchet Formation** Which of the following statements are CORRECT? Q.34 (A) Mytilus represents byssally attached bivalves (B) Nautilus is the only living cephalopod genus with a coiled external shell (C) The cidaroids are the only echinoid group still living Trilobites did not moult (D)



2.35	Which of the following genera are stem fossils?	1
2.33	which of the following genera are stern rossils:	001
(A)	Dadoxylon	12 s
(B)	Dicroidium	
(C)	Vertebraria	
(D)	Ptilophyllum	
	States and a second	
2.36	Which of the following statements are correct?	
(A)	Abutments are the sides of the valley supporting the dam structure	
(B)	Spillways can control the release of water from the reservoir	
(C)	The toe of the dam is the upstream edge of the base of the dam structure	
(D)	Galleries serve as passages through the dam	
~	5//5 B	
	A chris	
012	A C	
5.4	55	

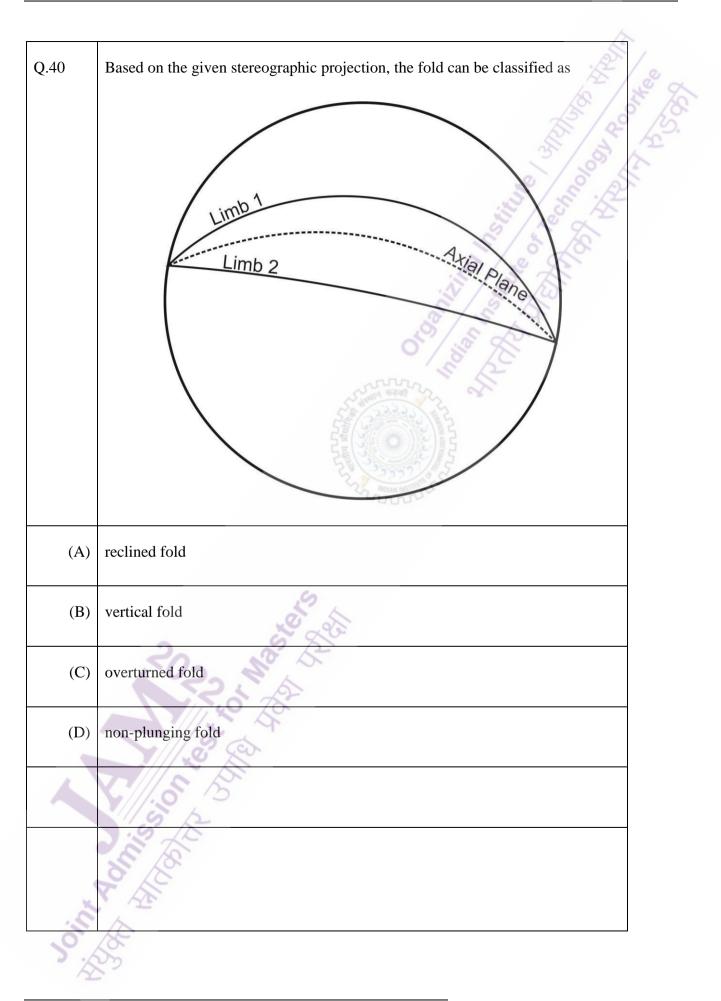


Q.37	The acceleration due to gravity on the Earth's surface depends on
(A)	latitude
(B)	longitude
(C)	elevation
(D)	topography of the surrounding terrain
	The second secon
Q.38	A metamorphosed basaltic assemblage can include the minerals
(A)	garnet-omphacite
(B)	hornblende-plagioclase
(C)	garnet-staurolite
(D)	glaucophane-lawsonite
	5/05
75	Hanis
SA	

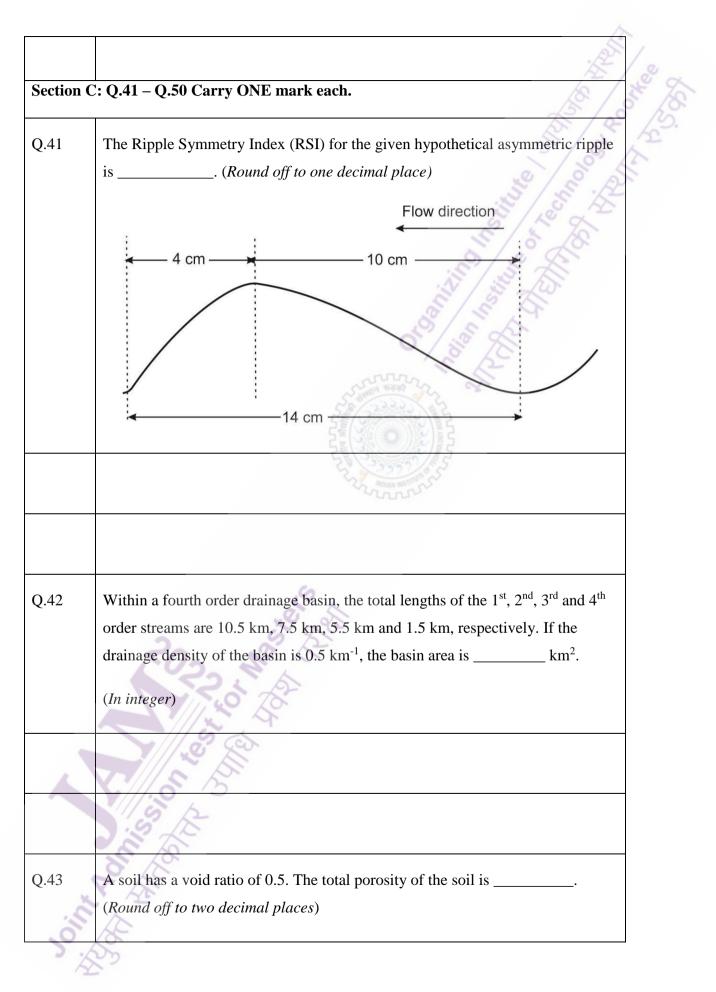


2.39	Which of the following pairs represent correct plutonic – volcanic equivalents?
(A)	Granodiorite – dacite
(B)	Norite – basalt
(C)	Dunite – komatiite
(D)	Nepheline syenite – phonolite
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Q.44	The average unit weight of the uppermost part of the crust is 25000 N/m ³ . The
	vertical stress at a depth of 1 km would be MPa. (In integer)
	000
	A. C.
	5 5 8
2.45	The radius of the Earth's circular orbit round the Sun is 149×10^6 km. The Earth
	takes 365 days to orbit the Sun. The tangential velocity of the Earth is
	km/hour. (π = 3.14) (<i>Round off to one decimal place</i>)
	and the second second
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.46	A borehole inclined at 60° to the horizontal pierces a vertical basaltic dyke of
	uniform thickness. If the length of the basaltic drill core along the core axis is
	12 m, the thickness of the dyke is m. (<i>In integer</i>)
	2
	S Solo
	500 50
	20 78
0.47	A P-ray arrives at the mantle-core boundary at an angle 25° with respect to the
	normal. At what angle to the normal does it enter the core? (P-wave velocity in
	the lower mantle is 13.7 km/s and outer core is 8.1 km/s)
	(Round off to two decimal places)
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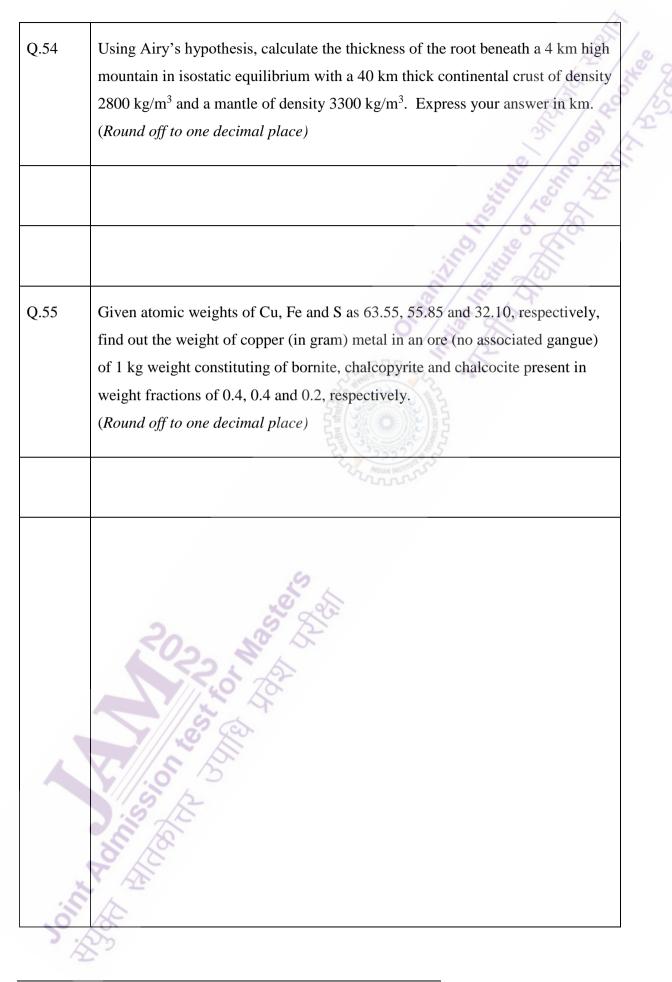


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	15/2
Q.48	The mass of the Earth is 80 times that of the Moon while the radius of the Earth
	is four times that of the Moon. The surface gravity of the Earth is times
	that of the Moon? (In integer)
	Same Can
	0/378
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	2
Q.49	A hypothetical rock contains the assemblage kyanite, sillimanite and quartz.
	The variance (degree of freedom) of the assemblage is (<i>In integer</i>)
	POLAN BOAT
	5
0.50	The cut off grade of copper is 0.45 wt%. A mine has 1 million toppe of waste
Q.50	The cut-off grade of copper is 0.45 wt%. A mine has 1 million tonne of waste with a grade of 0.25 wt%. The mine also has stock of high grade ore with a
	grade of 1.8 wt%. How much of this high grade ore (in million tonne) must be
	blended with the waste to sell the blended ore at a grade of 0.5 wt%?
	(Round off to three decimal places)
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	2 /C
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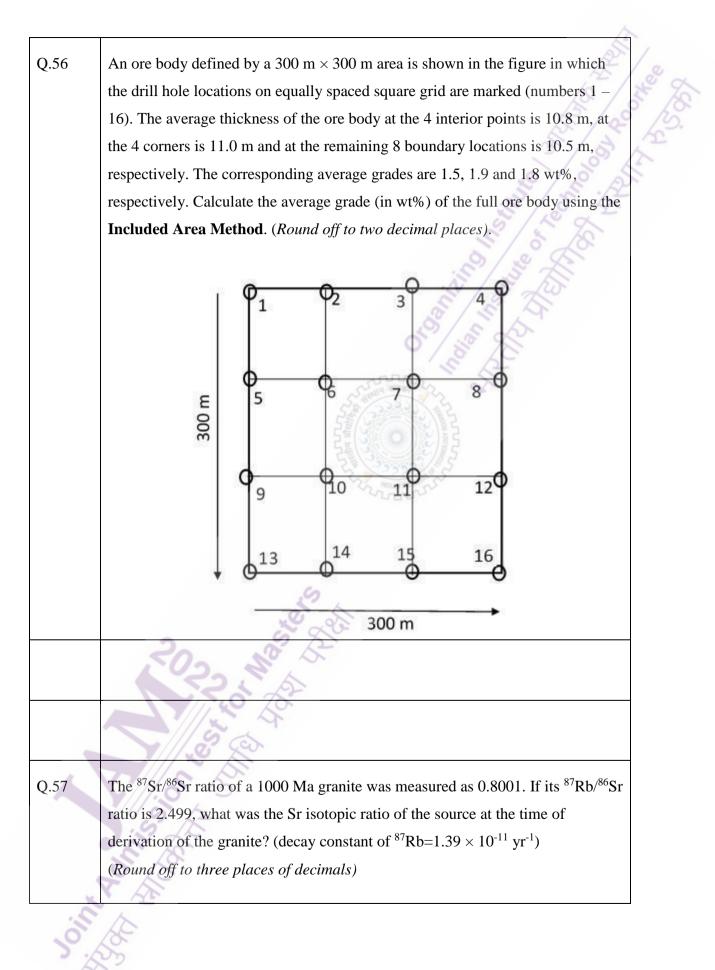


Section C: Q.51 – Q.60 Carry TWO marks each.		
	15 00	
Q.51	The maximum and minimum principal stresses in a zone of active normal	
	faulting are 28 MPa and 8 MPa, respectively. The fault plane strikes N30°E and	
	dips 60° towards SE. Considering Anderson's theory of faulting, the normal stress on the fault plane is MPa. (<i>In integer</i>)	
	Contraction of the second seco	
	States of the states	
Q.52	A granite block starts sliding on a slope (inclination of 30° with the horizontal)	
	under the effect of gravity only, along the true direction of inclination of the	
	slope and hits the ground in 4 seconds. Considering zero friction and zero	
	cohesion during sliding, the vertical height of the point (with respect to the	
	ground) from where the block was dislodged is m. $(g = 10 \text{ m/s}^2)$	
	(In integer)	
	2	
	Real and a second secon	
Q.53	A cylindrical soil sample is encased in an open-ended inclined tube with a	
	diameter of 100 mm. There is a constant supply of water from the upper end of	
	the sample and the outflow from the other end is collected in a beaker. The	
	average amount of water collected is 1000 mm ³ every 10 sec. The average	
	outflow velocity is mm/sec. ($\pi = 3.14$)	
	(Round off to three decimal places)	
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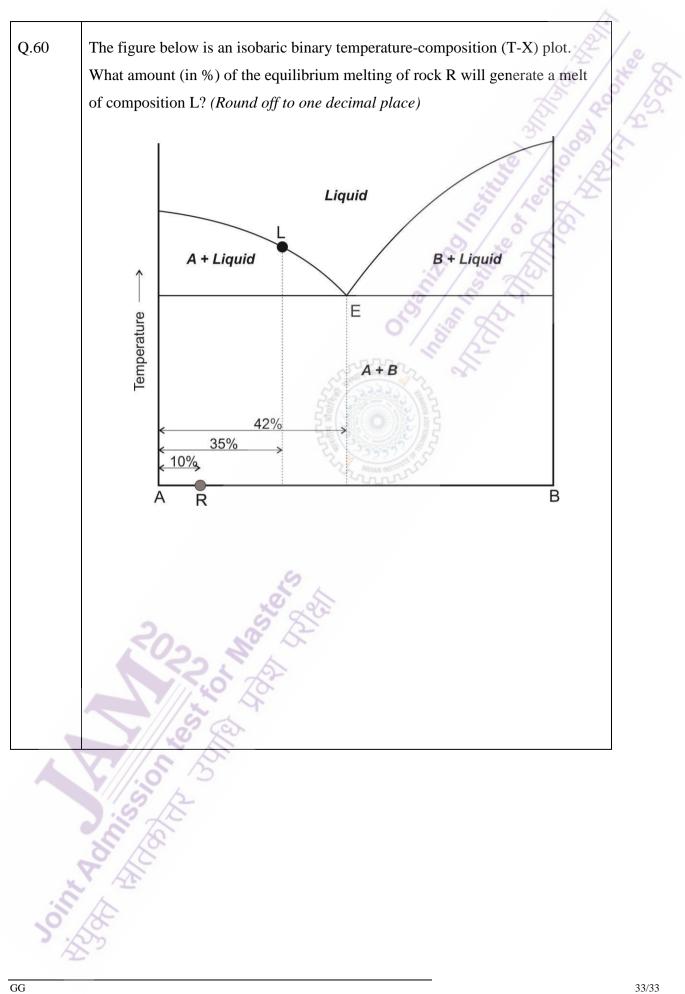






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	Special Instructions / Useful Data
	Special Instructions / Useful Data
\mathbb{R}	The set of real numbers
\mathbb{R}^{n}	$\{(x_1, x_2, \dots, x_n) : x_i \in \mathbb{R}, i = 1, 2, \dots, n\}, n = 2, 3, \dots$
$\ln x$	Natural logarithm of $x, x > 0$
det(M)	Determinant of a square matrix M
In	$n \times n$ identity matrix, $n = 2, 3, 4,$
E^{c}	Complement of a set <i>E</i>
P(E)	Probability of an event <i>E</i>
$P(E \mid F)$	Conditional probability of an event E given the occurrence of the event F
E(X)	Expectation of a random variable X
Var(X)	Variance of a random variable X
U(a,b)	Continuous uniform distribution on the interval $(a, b), -\infty < a < b < \infty$
$Exp(\lambda)$	Exponential distribution with the probability density function, for $\lambda > 0$,
	$f(x) = \begin{cases} \lambda e^{-\lambda x}, & x > 0\\ 0, & \text{otherwise} \end{cases}$
$N(\mu, \sigma^2)$	Normal distribution with mean μ and variance $\sigma^2, \mu \in \mathbb{R}, \sigma > 0$
$\Phi(\cdot)$	The cumulative distribution function of $N(0, 1)$ distributed random variable
χ^2_n	Central chi-square distribution with n degrees of freedom, $n = 1, 2,$
$F_{m,n}$	Snedecor's central F -distribution with (m, n) degrees of freedom,
	$m, n = 1, 2, \dots$
$t_{n,\alpha}$	A constant such that $P(X > t_{n,\alpha}) = \alpha$, where X has central Student's
	<i>t</i> -distribution with <i>n</i> degrees of freedom, $n = 1, 2,; \alpha \in (0, 1)$
	$\Phi(1.645) = 0.95, \qquad \Phi(0.355) = 0.6387$
	$t_{8,0.0185} = 2.5$
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Section A	: Q.1 – Q.10 Carry ONE mark each.
Q.1	Let $\{a_n\}_{n\geq 1}$ be a sequence of non-zero real numbers. Then which one of the following statements is true?
(A)	If $\left\{\frac{a_{n+1}}{a_n}\right\}_{n\geq 1}$ is a convergent sequence, then $\{a_n\}_{n\geq 1}$ is also a convergent sequence
(B)	If $\{a_n\}_{n\geq 1}$ is a bounded sequence, then $\{a_n\}_{n\geq 1}$ is a convergent sequence
(C)	If $ a_{n+2} - a_{n+1} \le \frac{3}{4} a_{n+1} - a_n $ for all $n \ge 1$, then $\{a_n\}_{n\ge 1}$ is a Cauchy sequence
(D)	If $\{ a_n \}_{n\geq 1}$ is a Cauchy sequence, then $\{a_n\}_{n\geq 1}$ is also a Cauchy sequence

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Q.2	Let $f: \mathbb{R} \to \mathbb{R}$ be the function defined by	000
	$f(x) = \begin{cases} \lim_{h \to 0} \frac{(x+h)\sin(\frac{1}{x}+h) - x\sin\frac{1}{x}}{h}, & x \neq 0\\ 0, & x = 0. \end{cases}$	100.5
	Then which one of the following statements is NOT true?	
(A)	$f\left(\frac{2}{\pi}\right) = 1$	
(B)	$f\left(\frac{1}{\pi}\right) = \frac{1}{\pi}$	
(C)	$f\left(-\frac{2}{\pi}\right) = -1$	
(D)	f is not continuous at $x = 0$	

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Q.3	Let $f: \mathbb{R} \to \mathbb{R}$ be the function defined by $f(x) = \det \begin{pmatrix} 1+x & 9 & 9\\ 9 & 1+x & 9\\ 9 & 9 & 1+x \end{pmatrix}.$
	Then the maximum value of f on the interval [9, 10] equals
(A)	118
(B)	112
(C)	114
(D)	116
	52 333555 Stars

Q.4	Let A and B be two events such that $0 < P(A) < 1$ and $0 < P(B) < 1$.
	Then which one of the following statements is NOT true?
(A)	If $P(A B) > P(A)$, then $P(B A) > P(B)$
(B)	If $P(A \cup B) = 1$, then A and B cannot be independent
(C)	If $P(A B) > P(A)$, then $P(A^c B) < P(A^c)$
(D)	If $P(A B) > P(A)$, then $P(A^c B^c) < P(A^c)$
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Q.5	If $M(t)$, $t \in \mathbb{R}$, is the moment generating function of a random variable, then which one of the following is NOT the moment generating function of any	The Sta
	random variable?	15. 15.
(A)	$\frac{5e^{-5t}}{1-4t^2}M(t), \ t < \frac{1}{2}$	1
(B)	$e^{-t}M(t), t \in \mathbb{R}$	
(C)	$\frac{1+e^t}{2(2-e^t)}M(t), \ t < \ln 2$	
(D)	$M(4t), t \in \mathbb{R}$	
	232322	

Q.6	Let X be a random variable having binomial distribution with parameters
	$n (> 1)$ and $p (0 . Then E \left(\frac{1}{1+X}\right) equals$
(A)	$\frac{1 - (1 - p)^{n+1}}{(n+1)p}$
(B)	$\frac{1-p^{n+1}}{(n+1)(1-p)}$
(C)	$\frac{(1-p)^{n+1}}{n(1-p)}$
(D)	$\frac{1-p^n}{(n+1)p}$
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Q.7	Let (X, Y) be a random vector having the joint probability density function $\left(\sqrt{2} - 2r - \frac{(y-x)^2}{2}\right) = 0$
	$f(x,y) = \begin{cases} \frac{\sqrt{2}}{\sqrt{\pi}} e^{-2x} e^{-\frac{(y-x)^2}{2}}, & 0 < x < \infty, -\infty < y < \infty \\ 0, & \text{otherwise.} \end{cases}$
	(0, otherwise.
	Then $E(Y)$ equals
(A)	$\frac{1}{2}$
(B)	2
(C)	
(D)	



Q.8	Let X_1 and X_2 be two independent and identically distributed discrete random variables having the probability mass function
	$f(x) = \begin{cases} \left(\frac{1}{2}\right)^{x}, & x = 1, 2, 3, \\ 0, & \text{otherwise.} \end{cases}$
	Then $P(\min\{X_1, X_2\} \ge 5)$ equals
(A)	
(B)	1 512
(C)	$\frac{1}{64}$
(D)	<u>9</u> 256

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Q.9	Let $X_1, X_2,, X_n$ $(n \ge 2)$ be a random sample from $Exp\left(\frac{1}{\theta}\right)$ distribution,
	where $\theta > 0$ is unknown. If $\overline{X} = \frac{1}{n} \sum_{i=1}^{n} X_i$, then which one of the following
	statements is NOT true?
(A)	\overline{X} is the uniformly minimum variance unbiased estimator of θ
(B)	\overline{X}^2 is the uniformly minimum variance unbiased estimator of θ^2
(C)	$\frac{n}{n+1}\overline{X}^2$ is the uniformly minimum variance unbiased estimator of θ^2
(D)	$Var\left(E\left(X_{n} \mid \overline{X}\right)\right) \leq Var(X_{n})$

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Q.10	Let $X_1, X_2,, X_n$ $(n \ge 3)$ be a random sample from a $N(\mu, \sigma^2)$ distribution, where $\mu \in \mathbb{R}$ and $\sigma > 0$ are both unknown. Then which one of the following is a simple null hypothesis?
(A)	$H_0: \mu < 5, \ \sigma^2 = 3$
(B)	$H_0: \mu = 5, \ \sigma^2 > 3$
(C)	$H_0: \mu = 5, \ \sigma^2 = 3$
(D)	$H_0: \mu = 5$

Section A: Q.11 – Q.30 Carry TWO marks each.	
Q.11	$\lim_{n \to \infty} \frac{6}{n+2} \left\{ \left(2 + \frac{1}{n}\right)^2 + \left(2 + \frac{2}{n}\right)^2 + \dots + \left(2 + \frac{n-1}{n}\right)^2 \right\} \text{ equals}$
(A)	38
(B)	36
(C)	32
(D)	30
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Q.12	Let $f: \mathbb{R}^2 \to \mathbb{R}$ be the function defined by
	$f(x,y) = \begin{cases} x^2 \sin \frac{1}{x} + y^2 \cos y, & x \neq 0\\ 0, & x = 0. \end{cases}$
	C 0, $x = 0$. Then which one of the following statements is NOT true?
(A)	f is continuous at (0,0)
(B)	The partial derivative of f with respect to x is not continuous at $(0, 0)$
(C)	The partial derivative of f with respect to y is continuous at $(0,0)$
(D)	f is not differentiable at $(0,0)$

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Q.13	Let $f: [1,2] \to \mathbb{R}$ be the function defined by $f(t) = \int_{1}^{t} \sqrt{x^{2}e^{x^{2}} - 1} dx.$
	Then the arc length of the graph of f over the interval $[1, 2]$ equals
(A)	$e^2 - \sqrt{e}$
(B)	$e - \sqrt{e}$
(C)	$e^2 - e$
(D)	$e^2 - 1$
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Q.14	Let $F: [0, 2] \to \mathbb{R}$ be the function defined by	
	$F(x) = \int_{x^2}^{x+2} e^{x [t]} dt,$	
	where $[t]$ denotes the greatest integer less than or equal to t . Then the value	
	of the derivative of F at $x = 1$ equals	
(A)	$e^3 + 2e^2 - e$	
(B)	$e^3 - e^2 + 2e$	
(C)	$e^3 - 2e^2 + e$	
(D)	$e^3 + 2e^2 + e$	

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Q.15	Let the system of equations
	x + ay + z = 1
	2x + 4y + z = -b 3x + y + 2z = b + 2
	have infinitely many solutions, where a and b are real constants. Then the
	value of $2a + 8b$ equals
(A)	-11
(B)	-10
(C)	-13
(D)	-14
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 (A) 101 (B) 103 (C) 102 (D) 100 	Q.16	Let $A = \begin{pmatrix} 0 & 1\\ 1 & 0\\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$. Then the sum of all the elements of A^{100} equals	0705
(C) 102	(A)	101	110 010 01 01 01 01 01 01 01 01 01 01 01	-
All and a second	(B)	103	9 12 00 10 10 10 10 10 10 10 10 10 10 10 10	
(D) 100	(C)	102	All all still	
	(D)	100	of the for	





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Q.17	Suppose that four persons enter a lift on the ground floor of a building. There
	are seven floors above the ground floor and each person independently chooses
	her exit floor as one of these seven floors. If each of them chooses the topmost
	floor with probability $\frac{1}{3}$ and each of the remaining floors with an equal
	probability, then the probability that no two of them exit at the same floor
	equals
(A)	200 729
(B)	220 729
(C)	240 729
(D)	$\frac{180}{729}$



Q.18	A year is chosen at random from the set of years {2012, 2013,, 2021}. From the chosen year, a month is chosen at random and from the chosen month, a day is chosen at random. Given that the chosen day is the 29 th of a month, the conditional probability that the chosen month is February equals
(A)	279 9965
(B)	289 9965
(C)	269 9965
(D)	259 9965

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Q.19	Suppose that a fair coin is tossed repeatedly and independently. Let <i>X</i> denote the number of tosses required to obtain for the first time a tail that is immediately preceded by a head. Then $E(X)$ and $P(X > 4)$, respectively,
	are
(A)	4 and $\frac{5}{16}$
(B)	4 and $\frac{11}{16}$
(C)	6 and $\frac{5}{16}$
(D)	6 and $\frac{11}{16}$

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Q.20	Let X be a random variable with the moment generating function
	$M(t) = \frac{1}{(1-4t)^5}, t < \frac{1}{4}.$
	Then the lower bounds for $P(X < 40)$, using Chebyshev's inequality and
	Markov's inequality, respectively, are
(A)	$\frac{4}{5}$ and $\frac{1}{2}$
(B)	$\frac{5}{6}$ and $\frac{1}{2}$
(C)	$\frac{4}{5}$ and $\frac{5}{6}$
(D)	$\frac{5}{6}$ and $\frac{5}{6}$

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In a store, the daily demand for milk (in litres) is a random variable having
$Exp(\lambda)$ distribution, where $\lambda > 0$. At the beginning of the day, the store
purchases $c (> 0)$ litres of milk at a fixed price $b (> 0)$ per litre. The milk
is then sold to the customers at a fixed price $s (> b)$ per litre. At the end of
the day, the unsold milk is discarded. Then the value of c that maximizes the
expected net profit for the store equals
$-\frac{1}{\lambda}\ln\left(\frac{b}{s}\right)$
$-\frac{1}{\lambda}\ln\left(\frac{b}{s+b}\right)$
$-\frac{1}{\lambda}\ln\left(\frac{s-b}{s}\right)$
$-\frac{1}{\lambda}\ln\left(\frac{s}{s+b}\right)$



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Q.22	Let X_1, X_2 and X_3 be three independent and identically distributed random
	variables having $U(0,1)$ distribution. Then $E\left[\left(\frac{\ln X_1}{\ln X_1 X_2 X_3}\right)^2\right]$ equals
	2 2 2
(A)	$\frac{1}{6}$
(B)	$\frac{1}{3}$
(C)	$\frac{1}{8}$
(D)	

Q.23	Let (X, Y) be a random vector having bivariate normal distribution with parameters $E(X) = 0$, $Var(X) = 1$, $E(Y) = -1$, $Var(Y) = 4$ and $\rho(X,Y) = -\frac{1}{2}$, where $\rho(X,Y)$ denotes the correlation coefficient between
	X and Y. Then $P(X + Y > 1 2X - Y = 1)$ equals
(A)	$\Phi\left(-\frac{1}{2}\right)$
(B)	$\Phi\left(-\frac{1}{3}\right)$
(C)	$\Phi\left(-\frac{1}{4}\right)$
(D)	$\Phi\left(-\frac{4}{3}\right)$

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Q.24	Let $\{X_n\}_{n \ge 1}$ be a sequence of independent and identically distributed random variables having the common probability density function $f(x) = \begin{cases} \frac{2}{x^3}, & x \ge 1\\ 0, & \text{otherwise.} \end{cases}$
	If $\lim_{n \to \infty} P\left(\left \frac{1}{n}\sum_{i=1}^{n} X_i - \theta\right < \epsilon\right) = 1$ for all $\epsilon > 0$, then θ equals
(A)	4
(B)	2
(C)	ln 4
(D)	ln 2

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Q.25	Let 0.2, 1.2, 1.4, 0.3, 0.9, 0.7 be the observed values of a random sample of
	size 6 from a continuous distribution with the probability density function
	$f(x) = \begin{cases} 1, & 0 < x \le \frac{1}{2} \\ \frac{1}{2\theta - 1}, & \frac{1}{2} < x \le \theta \\ 0, & \text{otherwise,} \end{cases}$
	where $\theta > \frac{1}{2}$ is unknown. Then the maximum likelihood estimate and the
	method of moments estimate of θ , respectively, are
(A)	$\frac{7}{5}$ and 2
(B)	$\frac{47}{60}$ and $\frac{32}{15}$
	$\frac{7}{5}$ and $\frac{32}{15}$
(D)	$\frac{7}{5}$ and $\frac{47}{60}$
	$\frac{7}{5}$ and $\frac{47}{60}$

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Q.26	For $n = 1, 2, 3,,$ let the joint moment generating function of (X, Y_n) be
	$M_{X,Y_n}(t_1,t_2) = e^{\frac{t_1^2}{2}}(1-2t_2)^{-\frac{n}{2}}, t_1 \in \mathbb{R}, t_2 < \frac{1}{2}.$
	If $T_n = \frac{\sqrt{n} X}{\sqrt{Y_n}}$, $n \ge 1$, then which one of the following statements is true?
(A)	The minimum value of n for which $Var(T_n)$ is finite is 2
(B)	$E(T_{10}^3) = 10$
(C)	$Var(X+Y_4) = 7$
(D)	$\lim_{n \to \infty} P(T_n > 3) = 1 - \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^3 e^{-\frac{t^2}{2}} dt$

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Q.27	Let $X_{(1)} < X_{(2)} < \cdots < X_{(9)}$ be the order statistics corresponding to a
	random sample of size 9 from $U(0, 1)$ distribution. Then which one of the
	following statements is NOT true?
(A)	$E\left(\frac{X_{(9)}}{1-X_{(9)}}\right)$ is finite
(B)	$E(X_{(5)}) = 0.5$
(C)	The median of $X_{(5)}$ is 0.5
(D)	The mode of $X_{(5)}$ is 0.5
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Q.28	Let $X_1, X_2,, X_{16}$ be a random sample from a $N(4\mu, 1)$ distribution and
	Y_1, Y_2, \dots, Y_8 be a random sample from a $N(\mu, 1)$ distribution, where
	$\mu \in \mathbb{R}$ is unknown. Assume that the two random samples are independent.
	If you are looking for a confidence interval for μ based on the statistic
	$8\overline{X} + \overline{Y}$, where $\overline{X} = \frac{1}{16} \sum_{i=1}^{16} X_i$ and $\overline{Y} = \frac{1}{8} \sum_{i=1}^{8} Y_i$, then which one of the
	following statements is true?
(A)	There exists a 90% confidence interval for μ of length less than 0.1
(B)	There exists a 90% confidence interval for μ of length greater than 0.3
(C)	$\left[\frac{8\overline{X}+\overline{Y}}{33}-\frac{1.645}{2\sqrt{66}}, \frac{8\overline{X}+\overline{Y}}{33}+\frac{1.645}{2\sqrt{66}}\right]$ is the unique 90% confidence interval for μ
(D)	μ always belongs to its 90% confidence interval

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Q .29	Let X_1, X_2, X_3, X_4 be a random sample from a distribution with the probability mass function
	$f(x) = \begin{cases} \theta^{x} (1-\theta)^{1-x}, & x = 0, 1\\ 0, & \text{otherwise,} \end{cases}$
	where $\theta \in (0, 1)$ is unknown. Let $0 < \alpha \le 1$. To test the hypothesis
	$H_0: \theta = \frac{1}{2}$ against $H_1: \theta > \frac{1}{2}$, consider the size α test that rejects H_0 if and
	only if $\sum_{i=1}^{4} X_i \ge k_{\alpha}$, for some $k_{\alpha} \in \{0, 1, 2, 3, 4\}$. Then for which one of
	the following values of α , the size α test does NOT exist?
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(A)	$\frac{1}{16}$
(B)	
(C)	$\frac{11}{16}$
(D)	5/16
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Q.30	Let X_1 , X_2 , X_3 , X_4 be a random sample from a Poisson distribution with unknown mean $\lambda > 0$. For testing the hypothesis
	$H_0: \lambda = 1$ against $H_1: \lambda = 1.5$,
	let β denote the power of the test that rejects H_0 if and only if $\sum_{i=1}^4 X_i \ge 5$.
	Then which one of the following statements is true?
(A)	$\beta > 0.80$
(B)	$0.75 < \beta \le 0.80$
(C)	$0.70 < \beta \le 0.75$
(D)	$0.65 < \beta \le 0.70$

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Section B: Q.31 – Q.40 Carry TWO marks each.	
Q.31	Let $\{a_n\}_{n \ge 1}$ be a sequence of real numbers such that $a_n = \frac{1}{3^n}$ for all $n \ge 1$. Then which of the following statements is/are true?
(A)	$\sum_{n=1}^{\infty} (-1)^{n+1} a_n$ is a convergent series
(B)	$\sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n} (a_1 + a_2 + \dots + a_n) \text{ is a convergent series}$
(C)	The radius of convergence of the power series $\sum_{n=1}^{\infty} a_n x^n$ is $\frac{1}{3}$
(D)	$\sum_{n=1}^{\infty} a_n \sin \frac{1}{a_n}$ is a convergent series



Q.32	Let $f: \mathbb{R}^2 \to \mathbb{R}$ be the function defined by $f(x, y) = 8(x^2 - y^2) - x^4 + y^4.$ Then which of the following statements is/are true?
(A)	f has 9 critical points
(B)	f has a saddle point at (2, 2)
(C)	f has a local maximum at $(-2, 0)$
(D)	f has a local minimum at $(0, -2)$

Q.33	If $n \ge 2$, then which of the following statements is/are true?
(A)	If A and B are $n \times n$ real orthogonal matrices such that
	det(A) + det(B) = 0, then $A + B$ is a singular matrix
(B)	If A is an $n \times n$ real matrix such that $I_n + A$ is non-singular, then
	$I_n + (I_n + A)^{-1}(I_n - A)$ is a singular matrix
(C)	If A is an $n \times n$ real skew-symmetric matrix, then $I_n - A^2$ is a non-
	singular matrix
(D)	If A is an $n \times n$ real orthogonal matrix, then $det(A - \lambda I_n) \neq 0$ for all
	$\lambda \in \{x \in \mathbb{R} : x \neq \pm 1\}$
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Q.34	Let $\Omega = \{1, 2, 3,\}$ be the sample space of a random experiment and suppose that all subsets of Ω are events. Further, let <i>P</i> be a probability function such that $P(\{i\}) > 0$ for all $i \in \Omega$. Then which of the following statements is/are true?
(A)	For every $\epsilon > 0$, there exists an event A such that $0 < P(A) < \epsilon$
(B)	There exists a sequence of disjoint events $\{A_k\}_{k\geq 1}$ with $P(A_k) \geq 10^{-6}$ for all $k \geq 1$
(C)	There exists $j \in \Omega$ such that $P(\{j\}) \ge P(\{i\})$ for all $i \in \Omega$
(D)	Let $\{A_k\}_{k\geq 1}$ be a sequence of events such that $\sum_{k=1}^{\infty} P(A_k) < \infty$. Then for each $i \in \Omega$ there exists $N \geq 1$ (which may depend on i) such that $i \notin \bigcup_{k=N}^{\infty} A_k$

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Q.35	A university bears the yearly medical expenses of each of its employees up to a maximum of Rs. 1000. If the yearly medical expenses of an employee exceed Rs. 1000, then the employee gets the excess amount from an insurance policy up to a maximum of Rs. 500. If the yearly medical expenses of a randomly selected employee has $U(250, 1750)$ distribution and Y denotes the amount the employee gets from the insurance policy, then which of the following statements is/are true?
(A)	$E(Y) = \frac{500}{3}$
(B)	$P(Y > 300) = \frac{3}{10}$
(C)	The median of Y is zero
(D)	The quantile of order 0.6 for Y equals 100

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Q.36	Let X and Y be two independent random variables having $N(0, \sigma_1^2)$ and
	$N(0, \sigma_2^2)$ distributions, respectively, where $0 < \sigma_1 < \sigma_2$. Then which of the following statements is/are true?
(A)	X + Y and $X - Y$ are independent
(B)	$2X + Y$ and $X - Y$ are independent if $2\sigma_1^2 = \sigma_2^2$
(C)	X + Y and $X - Y$ are identically distributed
(D)	$X + Y$ and $2X - Y$ are independent if $2\sigma_1^2 = \sigma_2^2$

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Q.37	Let (X, Y) be a discrete random vector. Then which of the following statements is/are true?
(A)	If X and Y are independent, then X^2 and $ Y $ are also independent.
(B)	If the correlation coefficient between X and Y is 1, then $P(Y = aX + b) = 1$ for some $a, b \in \mathbb{R}$
(C)	If X and Y are independent and $E[(XY)^2] = 0$, then $P(X = 0) = 1$ or $P(Y = 0) = 1$
(D)	If $Var(X) = 0$, then X and Y are independent

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Q.38	Let X_1 , X_2 and X_3 be three independent and identically distributed random
	variables having $N(0,1)$ distribution. If
	$U = \frac{2X_1^2}{(X_2 + X_3)^2}$ and $V = \frac{2(X_2 - X_3)^2}{2X_1^2 + (X_2 + X_3)^2}$,
	then which of the following statements is/are true?
(A)	U has $F_{1,1}$ distribution and V has $F_{1,2}$ distribution
(B)	U has $F_{1,1}$ distribution and V has $F_{2,1}$ distribution
(C)	U and V are independent
(D)	$\frac{1}{2}V(1+U)$ has $F_{2,3}$ distribution

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Q.39	Let X_1 , X_2 , X_3 , X_4 be a random sample from a continuous distribution with
	the probability density function $f(x) = \frac{1}{2} e^{- x-\theta }$, $x \in \mathbb{R}$, where $\theta \in \mathbb{R}$ is
	unknown. Let the corresponding order statistics be denoted by
	$X_{(1)} < X_{(2)} < X_{(3)} < X_{(4)}$. Then which of the following statements is/are true?
(A)	$\frac{1}{2}(X_{(2)} + X_{(3)})$ is the unique maximum likelihood estimator of θ
(B)	$(X_{(1)}, X_{(2)}, X_{(3)}, X_{(4)})$ is a sufficient statistic for θ
(C)	$\frac{1}{4}(X_{(2)} + X_{(3)})(X_{(2)} + X_{(3)} + 2)$ is a maximum likelihood estimator of
	$\frac{1}{4}(X_{(2)} + X_{(3)}) (X_{(2)} + X_{(3)} + 2)$ is a maximum likelihood estimator of $\theta(\theta + 1)$
(D)	$(X_1X_2X_3, X_1X_2X_4)$ is a complete statistic

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Q.40	Let $X_1, X_2,, X_n$ $(n > 1)$ be a random sample from a $N(\mu, 1)$ distribution, where $\mu \in \mathbb{R}$ is unknown. Let $0 < \alpha < 1$. To test the hypothesis $H_0: \mu = 0$ against $H_1: \mu = \delta$, where $\delta > 0$ is a constant, let β denote the power of the
	size α test that rejects H_0 if and only if $\frac{1}{n}\sum_{i=1}^n X_i > c_{\alpha}$, for some constant c_{α} . Then which of the following statements is/are true?
(A)	For a fixed value of δ , β increases as α increases
(B)	For a fixed value of α , β increases as δ increases
(C)	For a fixed value of δ , β decreases as α increases
(D)	For a fixed value of α , β decreases as δ increases

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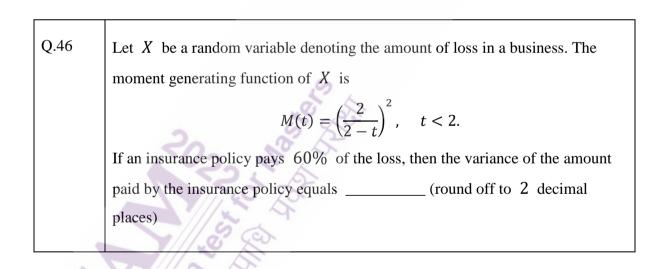
Section C: Q.41 - Q.50 Carry ONE mark each.Q.41Let $\{a_n\}_{n\geq 1}$ be a sequence of real numbers such that $a_{1+5m} = 2$,
 $a_{2+5m} = 3$, $a_{3+5m} = 4$, $a_{4+5m} = 5$, $a_{5+5m} = 6$, m = 0, 1, 2, ... Then
limsup $_{n\to\infty} a_n + \liminf_{n\to\infty} a_n$ equals _____Q.42Let $f: \mathbb{R} \to \mathbb{R}$ be a function such that
 $20(x - y) \leq f(x) - f(y) \leq 20(x - y) + 2(x - y)^2$
for all $x, y \in \mathbb{R}$ and f(0) = 2. Then f(101) equals _____</t>

Q.43	Let A be a 3×3 real matrix such that $det(A) = 6$ and $adj A = \begin{pmatrix} 1 & -1 & 2 \\ 5 & 7 & 1 \\ -1 & 1 & 1 \end{pmatrix}$, where $adj A$ denotes the adjoint of A.
	Then the trace of A equals (round off to 2 decimal places)
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Q.44	Let X and Y be two independent and identically distributed r	andom variables
	having $U(0,1)$ distribution. Then $P(X^2 < Y < X)$ equals	A A
	(round off to 2 decimal places)	000

Q.45	Consider a sequence of independent Bernoulli trials, where $\frac{3}{4}$ is the probability
	of success in each trial. Let X be a random variable defined as follows: If the
	first trial is a success, then X counts the number of failures before the next
	success. If the first trial is a failure, then X counts the number of successes
	before the next failure. Then $2E(X)$ equals
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Q.47	Let (X, Y) be a random vector having the joint moment generating function
	$M(t_1, t_2) = \left(\frac{1}{2} e^{-t_1} + \frac{1}{2} e^{t_1}\right)^2 \left(\frac{1}{2} + \frac{1}{2} e^{t_2}\right)^2, (t_1, t_2) \in \mathbb{R}^2.$
	Then $P(X + Y = 2)$ equals (round off to 2 decimal places)
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Q.48	Let X_1 and X_2 be two independent and identically distributed random
	variables having χ_2^2 distribution and $W = X_1 + X_2$. Then $P(W > E(W))$
	equals (round off to 2 decimal places)

Q.49	Let $2.5, -1.0, 0.5, 1.5$ be the observed values of a random sample of size 4
Q.+>	Let $2.5, -1.0, 0.5, 1.5$ be the observed values of a random sample of size $+$
	from a continuous distribution with the probability density function
	$f(x) = \frac{1}{8} e^{- x-2 } + \frac{3}{4\sqrt{2\pi}} e^{-\frac{1}{2}(x-\theta)^2}, \qquad x \in \mathbb{R},$
	where $\theta \in \mathbb{R}$ is unknown. Then the method of moments estimate of θ
	equals (round off to 2 decimal places)
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Q.50 Let $X_1, X_2, ..., X_{25}$ be a random sample from a $N(\mu, 1)$ distribution, where $\mu \in \mathbb{R}$ is unknown. Consider testing of the hypothesis $H_0: \mu = 5.2$ against $H_1: \mu = 5.6$. The null hypothesis is rejected if and only if $\frac{1}{25} \sum_{i=1}^{25} X_i > k$, for some constant k. If the size of the test is 0.05, then the probability of type-II error equals ______ (round off to 2 decimal places)

Section	C: Q.51 – Q.60 Carry TWO marks each.
Q.51	Let $f : \mathbb{R}^2 \to \mathbb{R}$ be the function defined by $f(x, y) = x^2 - 12y$. If M and m be the maximum value and the minimum value, respectively, of the function f on the circle $x^2 + y^2 = 49$, then $ M + m $ equals

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Q.52	The value of $\int_0^2 \int_0^{2-x} (x+y)^2 e^{\frac{2y}{x+y}} dy dx$
	equals (round off to 2 decimal places)
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Q.53	Let $A = \begin{pmatrix} 1 & -1 & 2 \\ -1 & 0 & 1 \\ 2 & 1 & 1 \end{pmatrix}$ and let $\begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix}$ be an eigenvector corresponding to	565
	the smallest eigenvalue of A, satisfying $x_1^2 + x_2^2 + x_3^2 = 1$. Then the value of	
	$ x_1 + x_2 + x_3 $ equals (round off to 2 decimal places)	
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Q.54	Five men go to a restaurant together and each of them orders a dish that is
	different from the dishes ordered by the other members of the group. However,
	the waiter serves the dishes randomly. Then the probability that exactly one of
	them gets the dish he ordered equals (round off to 2 decimal
	places)
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Q.55	Let X be a random variable having the probability density function
	$f(x) = \begin{cases} ax^2 + b, & 0 \le x \le 3\\ 0, & \text{otherwise,} \end{cases}$
	where <i>a</i> and <i>b</i> are real constants, and $P(X \ge 2) = \frac{2}{3}$.
	Then $E(X)$ equals (round off to 2 decimal places)
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Q.56	A vaccine, when it is administered to an individual, produces no side effects
	with probability $\frac{4}{5}$, mild side effects with probability $\frac{2}{15}$ and severe side effects
	with probability $\frac{1}{15}$. Assume that the development of side effects is independent
	across individuals. The vaccine was administered to 1000 randomly selected
	individuals. If X_1 denotes the number of individuals who developed mild side
	effects and X_2 denotes the number of individuals who developed severe side
	effects, then the coefficient of variation of $X_1 + X_2$ equals
	(round off to 2 decimal places)

Q.57 Let $\{X_n\}_{n \ge 1}$ be a sequence of independent and identically distributed random variables having U(0, 1) distribution. Let $Y_n = n \min\{X_1, X_2, ..., X_n\}$, $n \ge 1$. If Y_n converges to Y in distribution, then the median of Y equals ______ (round off to 2 decimal places)

Q.58	Let $X_{(1)} < X_{(2)} < X_{(3)} < X_{(4)} < X_{(5)}$ be the order statistics based on a
	random sample of size 5 from a continuous distribution with the probability
	density function
	$f(x) = \begin{cases} \frac{1}{x^2}, & 1 < x < \infty \\ 0, & \text{otherwise.} \end{cases}$
	Then the sum of all possible values of $r \in \{1, 2, 3, 4, 5\}$ for which $E(X_{(r)})$
	is finite equals
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.59	Consider the linear regression model $y_i = \beta_0 + \beta_1 x_i + \epsilon_i$, $i = 1, 2,, 6$,								
	where β_0 and	d β_1	are un	nknowr	n paran	neters ar	nd ϵ_i 's	are inde	ependent and
	identically distr	ribute	d rando	om varia	ables ha	ving N	(0,1)	distribut	tion. The data
	on (x_i, y_i) are	e give	en in the	e follow	ving tab	le.		itus	chinole
		x _i	1.0	2.0	2.5	3.0	3.5	4.5	1 del
		y _i	2.0	3.0	3.5	4.2	5.0	5.4	13
	If $\widehat{\beta_0}$ and $\widehat{\beta_1}$	are t	he least	t square	es estim	ates of μ	\mathcal{B}_0 and	β_1 , res	spectively,
	based on the above data, then $\widehat{\beta_0} + \widehat{\beta_1}$ equals (round off to 2								
	decimal places))							

Q.60	Let $X_1, X_2,, X_9$ be a random sample from a $N(\mu, \sigma^2)$ distribution, where $\mu \in \mathbb{R}$ and $\sigma > 0$ are unknown. Let the observed values of $\overline{X} = \frac{1}{9} \sum_{i=1}^{9} X_i$ and $S^2 = \frac{1}{8} \sum_{i=1}^{9} (X_i - \overline{X})^2$ be 9.8 and 1.44, respectively. If the likelihood
	ratio test is used to test the hypothesis $H_0: \mu = 8.8$ against $H_1: \mu > 8.8$, then
	the p -value of the test equals (round off to 3 decimal places)
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Notation and Terminology

- \mathbb{N} = the set of all positive integers.
- \mathbb{Z} = the set of all integers.
- \mathbb{Q} = the set of all rational numbers.
- \mathbb{R} = the set of all real numbers.
- \mathbb{R}^n = the *n*-dimensional Euclidean space.
- \mathbb{C} = the set of all complex numbers.
- $M_n(\mathbb{R})$ = the real vector space of all $n \times n$ matrices with entries in \mathbb{R} .
- $M_n(\mathbb{C})$ = the complex vector space of all $n \times n$ matrices with entries in \mathbb{C} .

gcd(m, n) = the greatest common divisor of the integers *m* and *n*.

 M^{\top} = the transpose of the matrix M.

- A B = the complement of the set *B* in the set *A*, that is, $\{x \in A : x \notin B\}$.
- $\ln x$ = the natural logarithm of x (to the base e).
- |x| = the absolute value of x.

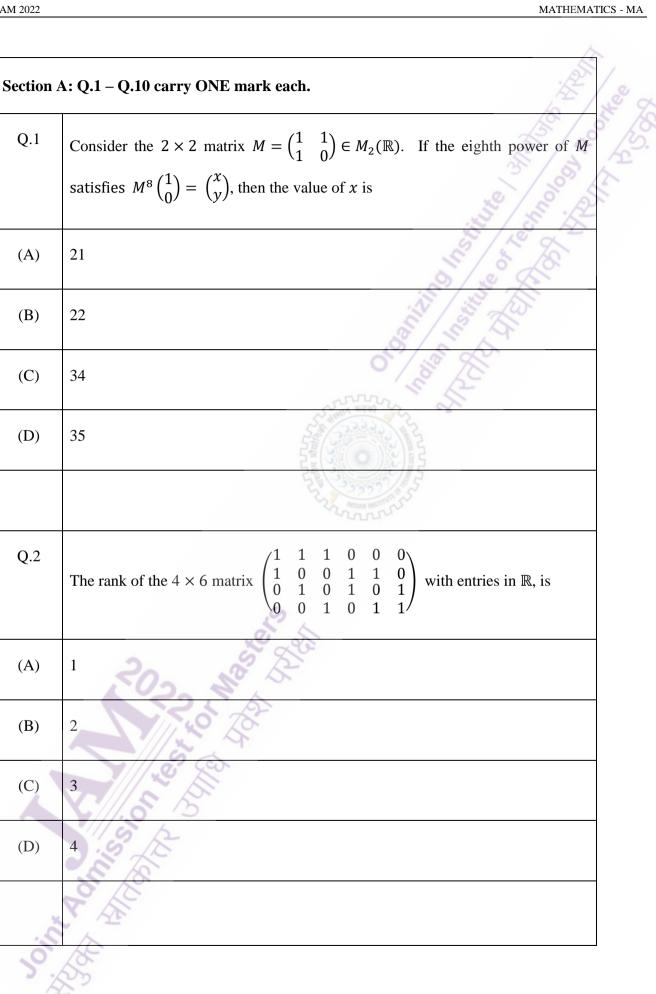
y', y'', y''' = the first, second and the third derivatives of the function *y*, respectively.

 S_n = the symmetric group consisting of all permutations of {1,2, ..., n}.

 \mathbb{Z}_n = the additive group of integers modulo n.

 $f \circ g$ is the composite function defined by $(f \circ g)(x) = f(g(x))$.

The phrase 'real vector space' refers to a vector space over \mathbb{R} .



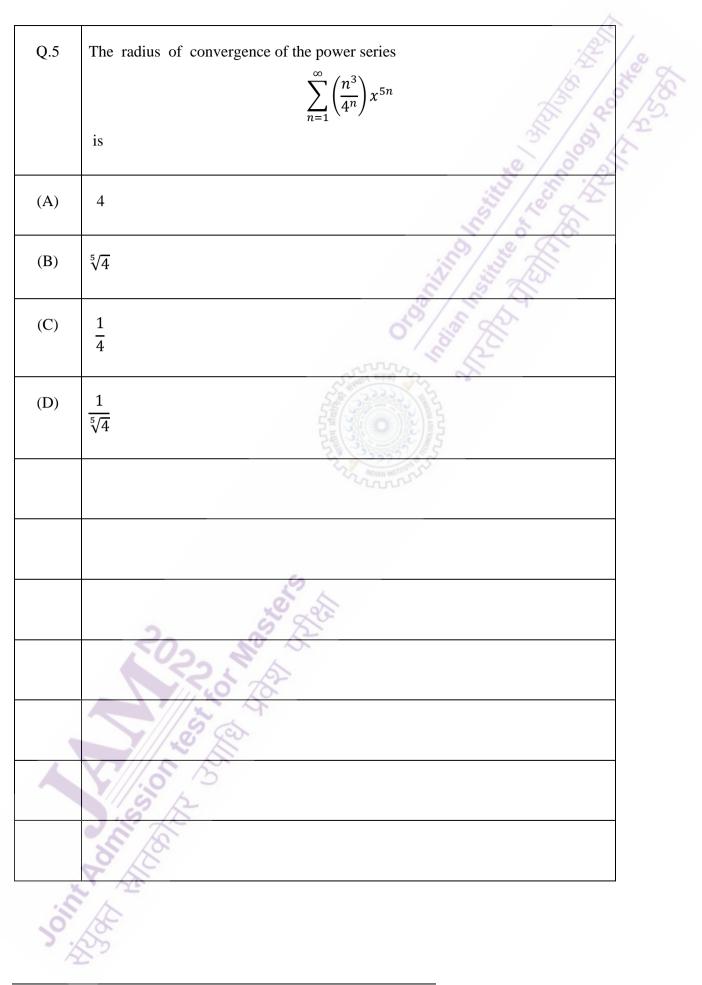
B) $\{f \in V : f(1/2) = 1\}$ is a subspace of V.C) $\{f \in V : f(1/2) = f(1)\}$ is a subspace of V.D) $\{f \in V : f'(1/2) = 1\}$ is a subspace of V.Q.4Let G be a group of order 2022. Let H and K be subgroups of G of order 337 and 674, respectively. If $H \cup K$ is also a subgroup of G, then which one of the following is FALSE?A)H is a normal subgroup of $H \cup K$.B)The order of $H \cup K$ is 1011.C)The order of $H \cup K$ is 674.	2.3	Let V be the real vector space consisting of all polynomials in one variable with
A) $\{f \in V : f(1/2) \notin \mathbb{Q}\}$ is a subspace of V.(B) $\{f \in V : f(1/2) = 1\}$ is a subspace of V.(C) $\{f \in V : f(1/2) = f(1)\}$ is a subspace of V.(D) $\{f \in V : f'(1/2) = 1\}$ is a subspace of V.(Q.4)Let G be a group of order 2022. Let H and K be subgroups of G of order 337 and 674, respectively. If $H \cup K$ is also a subgroup of G, then which one of the following is FALSE?(A)H is a normal subgroup of $H \cup K$.(B)The order of $H \cup K$ is 1011.(C)The order of $H \cup K$ is 674.		
B) $\{f \in V : f(1/2) = 1\}$ is a subspace of V.(C) $\{f \in V : f(1/2) = f(1)\}$ is a subspace of V.(D) $\{f \in V : f'(1/2) = 1\}$ is a subspace of V.(D) $\{f \in V : f'(1/2) = 1\}$ is a subspace of V.(Q.4)Let G be a group of order 2022. Let H and K be subgroups of G of order 337 and 674, respectively. If $H \cup K$ is also a subgroup of G, then which one of the following is FALSE?(A)H is a normal subgroup of $H \cup K$.(B)The order of $H \cup K$ is 1011.(C)The order of $H \cup K$ is 674.		Then which one of the following is true?
(C) $\{f \in V : f(1/2) = f(1)\}$ is a subspace of V.(D) $\{f \in V : f'(1/2) = 1\}$ is a subspace of V.(D) $\{f \in V : f'(1/2) = 1\}$ is a subspace of V.(Q.4)Let G be a group of order 2022. Let H and K be subgroups of G of order 337 and 674, respectively. If $H \cup K$ is also a subgroup of G, then which one of the following is FALSE?(A)H is a normal subgroup of $H \cup K$.(B)The order of $H \cup K$ is 1011.(C)The order of $H \cup K$ is 674.	A)	${f \in V : f(1/2) \notin \mathbb{Q}}$ is a subspace of <i>V</i> .
D) $\{f \in V : f'(1/2) = 1\}$ is a subspace of V.Q.4Let G be a group of order 2022. Let H and K be subgroups of G of order 337 and 674, respectively. If $H \cup K$ is also a subgroup of G, then which one of the following is FALSE?(A)H is a normal subgroup of $H \cup K$.(B)The order of $H \cup K$ is 1011.(C)The order of $H \cup K$ is 674.	<u>B</u>)	${f \in V : f(1/2) = 1}$ is a subspace of V.
Q.4Let G be a group of order 2022. Let H and K be subgroups of G of order 337 and 674, respectively. If $H \cup K$ is also a subgroup of G, then which one of the following is FALSE?(A)H is a normal subgroup of $H \cup K$.(B)The order of $H \cup K$ is 1011.(C)The order of $H \cup K$ is 674.	<u>(</u> C)	${f \in V : f(1/2) = f(1)}$ is a subspace of V.
674, respectively. If $H \cup K$ is also a subgroup of G , then which one of the following is FALSE?(A) H is a normal subgroup of $H \cup K$.(B)The order of $H \cup K$ is 1011.(C)The order of $H \cup K$ is 674.	D)	${f \in V : f'(1/2) = 1}$ is a subspace of <i>V</i> .
674, respectively. If $H \cup K$ is also a subgroup of G , then which one of the following is FALSE?(A) H is a normal subgroup of $H \cup K$.(B)The order of $H \cup K$ is 1011.(C)The order of $H \cup K$ is 674.		
674, respectively. If $H \cup K$ is also a subgroup of G , then which one of the following is FALSE?(A) H is a normal subgroup of $H \cup K$.(B)The order of $H \cup K$ is 1011.(C)The order of $H \cup K$ is 674.	2.4	Let G be a group of order 2022. Let H and K be subgroups of G of order 337 and
(A)H is a normal subgroup of $H \cup K$.(B)The order of $H \cup K$ is 1011.(C)The order of $H \cup K$ is 674.		674, respectively. If $H \cup K$ is also a subgroup of G, then which one of the
(B) The order of $H \cup K$ is 1011. (C) The order of $H \cup K$ is 674.		following is FALSE?
(C) The order of $H \cup K$ is 674.	(A)	<i>H</i> is a normal subgroup of $H \cup K$.
(C) The order of $H \cup K$ is 674.	B)	The order of $H \cup K$ is 1011.
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(D) K is a normal subgroup of $H \cup K$.	C)	The order of $H \cup K$ is 674.
(D) K is a normal subgroup of $H \cup K$.	-	
Sunda States	D)	K is a normal subgroup of $H \cup K$.
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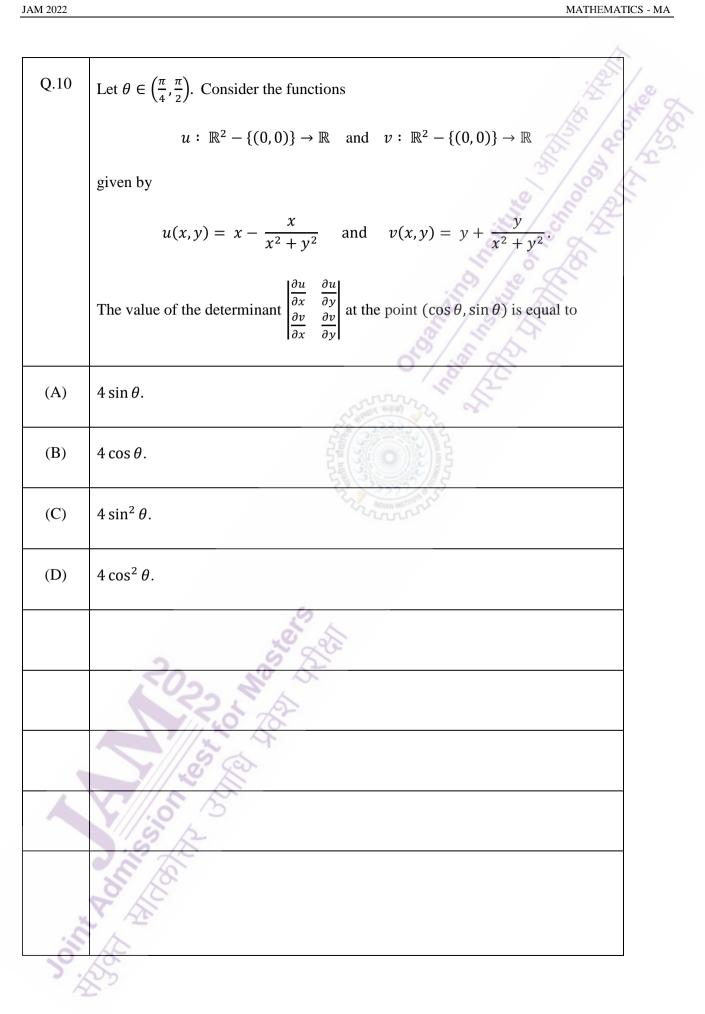
Q.6Let
$$(x_n)$$
 and (y_n) be sequences of real numbers defined by
 $x_1 = 1, \ y_1 = \frac{1}{2}, \ x_{n+1} = \frac{x_n + y_n}{2}, \ \text{and} \ y_{n+1} = \sqrt{x_n y_n} \quad \text{for all } n \in \mathbb{N},$
Then which one of the following is true?(A) (x_n) is convergent, but (y_n) is not convergent.(B) (x_n) is not convergent, but (y_n) is convergent.(C)Both (x_n) and (y_n) are convergent and $\lim_{n \to \infty} x_n > \lim_{n \to \infty} y_n$.(D)Both (x_n) and (y_n) are convergent and $\lim_{n \to \infty} x_n = \lim_{n \to \infty} y_n$.(a) $x_n = \frac{3^n + 3}{5^n - 5}$ and $b_n = \frac{1}{(1 + n^2)^{\frac{1}{3}}}$ for $n = 2,3,4,...$.(A)Both $\sum_{n=2}^{\infty} a_n$ and $\sum_{n=2}^{\infty} b_n$ are convergent.(B)Both $\sum_{n=2}^{\infty} a_n$ and $\sum_{n=2}^{\infty} b_n$ are divergent.(C) $\sum_{n=2}^{\infty} a_n$ is convergent and $\sum_{n=2}^{\infty} b_n$ is divergent.(D) $\sum_{n=2}^{\infty} a_n$ is divergent and $\sum_{n=2}^{\infty} b_n$ is convergent.

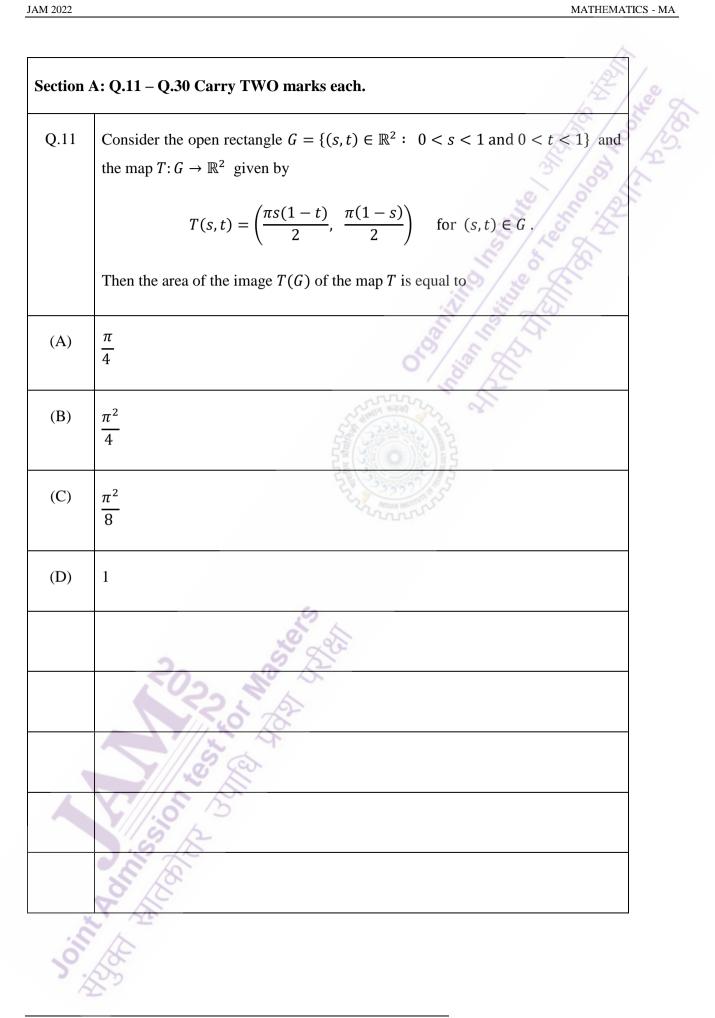


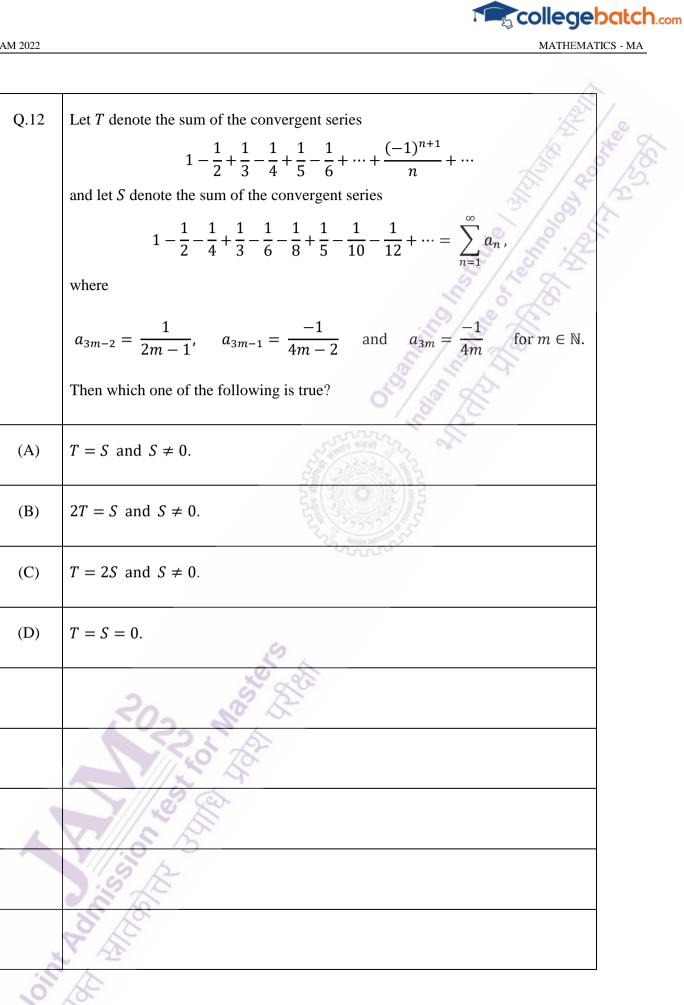
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	the set
Q.8	Consider the series
	$\sum_{n=1}^{\infty} \frac{1}{n^m \left(1 + \frac{1}{n^p}\right)}$
	where <i>m</i> and <i>p</i> are real numbers.
	Under which of the following conditions does the above series converge?
(A)	<i>m</i> > 1.
(B)	0 < m < 1 and $p > 1$.
(C)	$0 < m \le 1$ and $0 \le p \le 1$.
(D)	m = 1 and $p > 1$.
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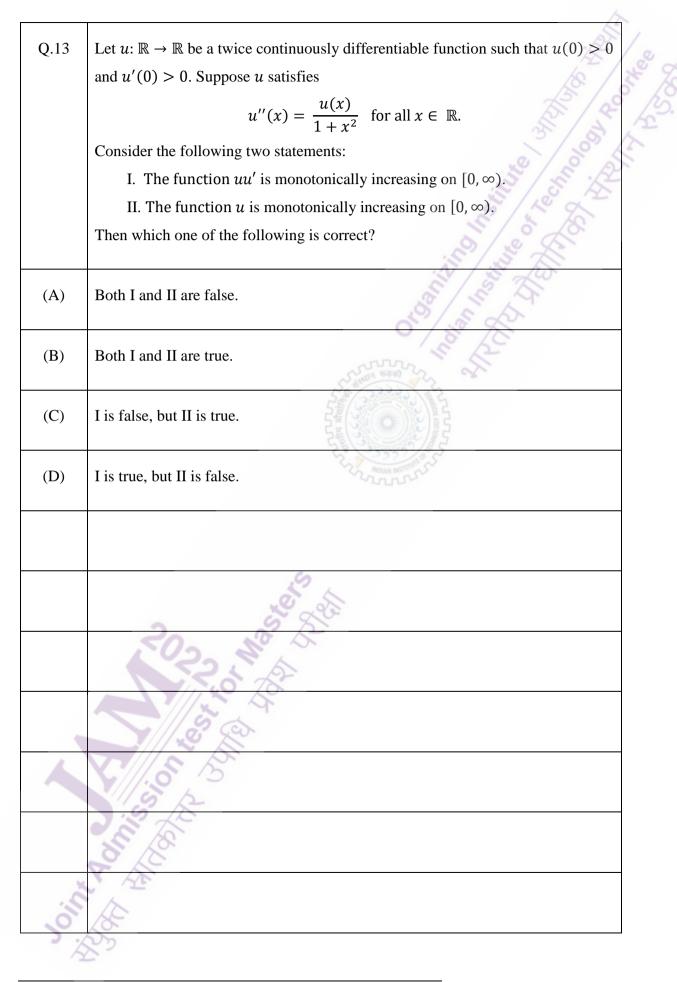


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Q.9	Let <i>c</i> be a positive real number and let $u: \mathbb{R}^2 \to \mathbb{R}$ be defined by	
	$u(x,t) = \frac{1}{\sqrt{1-\frac{x+ct}{c}}} \int \frac{1}{c} e^{s^2} ds \text{for } (x,t) \in \mathbb{R}^2$	To
	$u(x,t) = \frac{1}{2c} \int_{x-ct}^{x+ct} e^{s^2} ds \text{ for } (x,t) \in \mathbb{R}^2.$	5.
	Then which one of the following is true?	
(A)	$\frac{\partial^2 u}{\partial t^2} = c^2 \frac{\partial^2 u}{\partial x^2} \text{on } \mathbb{R}^2.$	
	$\overline{\partial t^2} = c^2 \overline{\partial x^2}$ on \mathbb{R}^2 .	
(B)	$\frac{\partial u}{\partial t} = c^2 \frac{\partial^2 u}{\partial x^2} \text{on } \mathbb{R}^2.$	
(C)	$\frac{\partial u}{\partial t}\frac{\partial u}{\partial x} = 0 \text{on } \mathbb{R}^2.$	
(D)	$\partial^2 u$	
	$\frac{\partial^2 u}{\partial t \partial x} = 0 \text{on } \mathbb{R}^2.$	
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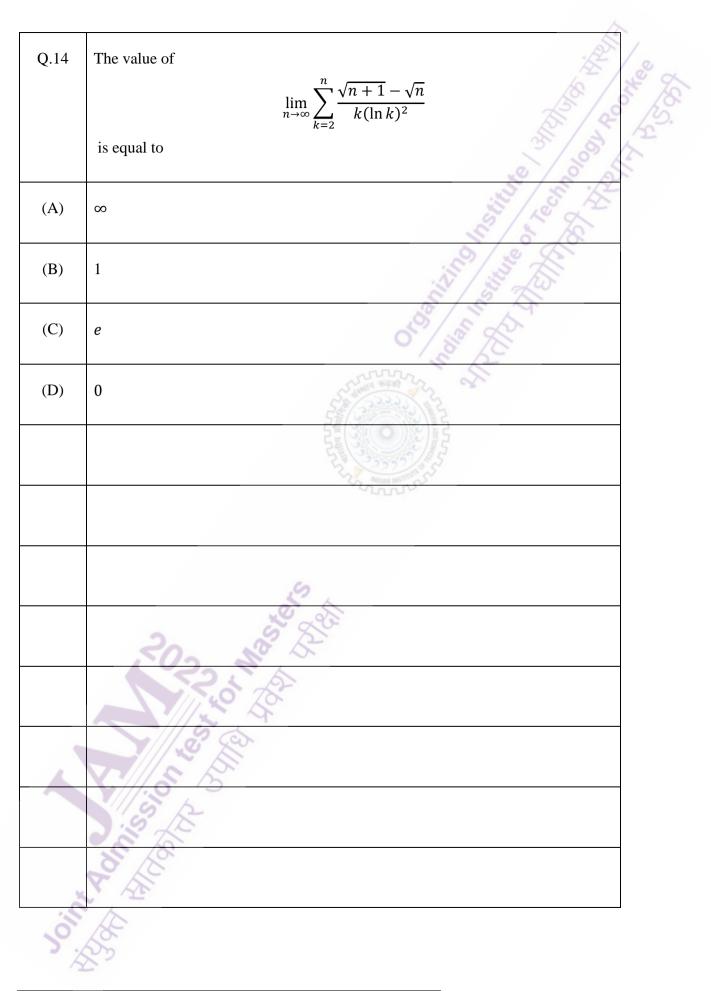




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MATHEMATICS - MA







Q.15 For $t \in \mathbb{R}$, let $[t]$ denote the greatest integer less than or equal to t . Define functions $h: \mathbb{R}^2 \to \mathbb{R}$ and $g: \mathbb{R} \to \mathbb{R}$ by $h(x, y) = \begin{cases} \frac{z^2}{x^2 - y} & \text{if } x^2 \neq y, \\ 0 & \text{if } x^2 = y \end{cases} \text{ and } g(x) = \begin{cases} \frac{\sin x}{x} & \text{if } x \neq 0, \\ 0 & \text{if } x = 0. \end{cases}$ Then which one of the following is FALSE? (A) $\lim_{(x,y) \to (\sqrt{2}, \pi)} \cos\left(\frac{x^2 y}{x^2 + 1}\right) = \frac{-1}{2}.$ (B) $\lim_{(x,y) \to (\sqrt{2}, 2)} e^{h(x, y)} = 0.$ (C) $\lim_{(x,y) \to (e, e)} \ln(x^{y-[y]}) = e - 2.$ (D) $\lim_{(x,y) \to (0, 0)} e^{2y} g(x) = 1.$		
$h(x,y) = \begin{cases} \frac{-1}{x^2 - y} & \text{if } x^2 \neq y, \\ 0 & \text{if } x^2 = y \end{cases} \text{ and } g(x) = \begin{cases} \frac{\sin x}{x} & \text{if } x \neq 0, \\ 0 & \text{if } x = 0, \end{cases}$ Then which one of the following is FALSE? $(A) \qquad \lim_{(x,y) \to (\sqrt{2}\pi)} \cos\left(\frac{x^2y}{x^2 + 1}\right) = \frac{-1}{2}.$ $(B) \qquad \lim_{(x,y) \to (\sqrt{2}2)} e^{h(x,y)} = 0.$ $(C) \qquad \lim_{(x,y) \to (e,e)} \ln(x^{y - [y]}) = e - 2.$ $(D) \qquad \lim_{(x,y) \to (0,0)} e^{2y}g(x) = 1.$	Q.15	12/0
Then which one of the following is FALSE? (A) $\lim_{(x,y)\to(\sqrt{2},\pi)} \cos\left(\frac{x^2y}{x^2+1}\right) = \frac{-1}{2}.$ (B) $\lim_{(x,y)\to(\sqrt{2},2)} e^{h(x,y)} = 0.$ (C) $\lim_{(x,y)\to(e,e)} \ln(x^{y-[y]}) = e - 2.$ (D) $\lim_{(x,y)\to(0,0)} e^{2y}g(x) = 1.$		P
Then which one of the following is FALSE? (A) $\lim_{(x,y)\to(\sqrt{2},\pi)} \cos\left(\frac{x^2y}{x^2+1}\right) = \frac{-1}{2}.$ (B) $\lim_{(x,y)\to(\sqrt{2},2)} e^{h(x,y)} = 0.$ (C) $\lim_{(x,y)\to(e,e)} \ln(x^{y-[y]}) = e - 2.$ (D) $\lim_{(x,y)\to(0,0)} e^{2y}g(x) = 1.$		$\left(\frac{-1}{x^2 - y} \text{if } x^2 \neq y, \qquad \left(\frac{\sin x}{x} \text{if } x \neq 0, \right)\right)$
Then which one of the following is FALSE? (A) $\lim_{(x,y)\to(\sqrt{2},\pi)} \cos\left(\frac{x^2y}{x^2+1}\right) = \frac{-1}{2}.$ (B) $\lim_{(x,y)\to(\sqrt{2},2)} e^{h(x,y)} = 0.$ (C) $\lim_{(x,y)\to(e,e)} \ln(x^{y-[y]}) = e - 2.$ (D) $\lim_{(x,y)\to(0,0)} e^{2y}g(x) = 1.$		$ \begin{array}{c} h(x,y) = \begin{cases} & \text{and} & g(x) = \\ 0 & \text{if } x^2 = y \end{cases} \text{of } x = 0. \end{cases} $
(A) $\lim_{(x,y)\to(\sqrt{2},\pi)} \cos\left(\frac{x^2y}{x^2+1}\right) = \frac{-1}{2}.$ (B) $\lim_{(x,y)\to(\sqrt{2},2)} e^{h(x,y)} = 0.$ (C) $\lim_{(x,y)\to(e,e)} \ln(x^{y-[y]}) = e - 2.$ (D) $\lim_{(x,y)\to(0,0)} e^{2y}g(x) = 1.$		
$\lim_{(x,y)\to(\sqrt{2},\pi)} \cos\left(\frac{x-y}{x^2+1}\right) = \frac{1}{2}.$ (B) $\lim_{(x,y)\to(\sqrt{2},2)} e^{h(x,y)} = 0.$ (C) $\lim_{(x,y)\to(e,e)} \ln(x^{y-[y]}) = e - 2.$ (D) $\lim_{(x,y)\to(0,0)} e^{2y}g(x) = 1.$		Then which one of the following is TALSE?
(B) $\lim_{(x,y)\to(\sqrt{2},2)} e^{h(x,y)} = 0.$ (C) $\lim_{(x,y)\to(e,e)} \ln(x^{y-[y]}) = e - 2.$ (D) $\lim_{(x,y)\to(0,0)} e^{2y} g(x) = 1.$	(A)	$\lim_{x \to \infty} \left(\begin{array}{c} x^2 y \end{array} \right) = -1$
(C) $\lim_{(x,y)\to(e,e)} \ln(x^{y-[y]}) = e - 2.$ (D) $\lim_{(x,y)\to(0,0)} e^{2y}g(x) = 1.$		$\lim_{(x,y)\to(\sqrt{2},\pi)}\cos\left(\frac{1}{x^2+1}\right) = \frac{1}{2}.$
(C) $\lim_{(x,y)\to(e,e)} \ln(x^{y-[y]}) = e - 2.$ (D) $\lim_{(x,y)\to(0,0)} e^{2y}g(x) = 1.$		
(D) $\lim_{(x,y)\to(0,0)} e^{2y}g(x) = 1.$	(B)	$\lim_{(x,y)\to(\sqrt{2},2)} e^{h(x,y)} = 0.$
(D) $\lim_{(x,y)\to(0,0)} e^{2y}g(x) = 1.$		
	(C)	$\lim_{(x,y)\to(e,e)} \ln(x^{y-[y]}) = e - 2.$
	(D)	$\lim_{(x,y)\to(0,0)} e^{2y} g(x) = 1.$
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Q.16	Let $P \in M_4(\mathbb{R})$ be such that P^4 is the zero matrix, but P^3 is a nonzero matrix. Then which one of the following is FALSE?
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(A)	For every nonzero vector $v \in \mathbb{R}^4$, the subset $\{v, Pv, P^2v, P^3v\}$ of the real vector
	space \mathbb{R}^4 is linearly independent.
	A. C.
(B)	The rank of P^k is $4 - k$ for every $k \in \{1,2,3,4\}$.
(C)	0 is an eigenvalue of <i>P</i> .
(D)	If $Q \in M_4(\mathbb{R})$ is such that Q^4 is the zero matrix, but Q^3 is a nonzero matrix, then
	there exists a nonsingular matrix $S \in M_4(\mathbb{R})$ such that $S^{-1}QS = P$.
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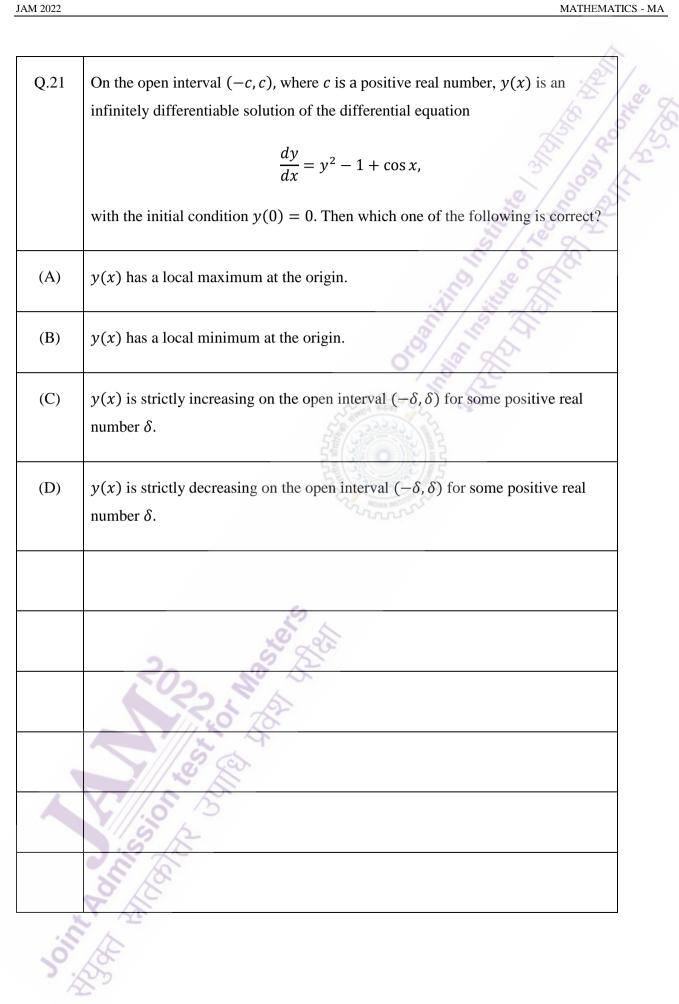
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Q.17	For $X, Y \in M_2(\mathbb{R})$, define $(X, Y) = XY - YX$. Let $0 \in M_2(\mathbb{R})$ denote the zero matrix. Consider the two statements:
	$P: (X, (Y, Z)) + (Y, (Z, X)) + (Z, (X, Y)) = 0 \text{ for all } X, Y, Z \in M_2(\mathbb{R}).$
	$Q: (X, (Y, Z)) = ((X, Y), Z) \text{ for all } X, Y, Z \in M_2(\mathbb{R}).$
	Then which one of the following is correct?
(A)	Both <i>P</i> and <i>Q</i> are true.
(B)	P is true, but Q is false.
(C)	P is false, but Q is true.
(D)	Both <i>P</i> and <i>Q</i> are false.
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Q.18	Consider the system of linear equations
	$ \begin{array}{rcl} x + y + t &=& 4, \\ 2x - 4t &=& 7, \\ x + y + z &=& 5, \\ x - 3y - z - 10t &=& \lambda, \end{array} $
	where <i>x</i> , <i>y</i> , <i>z</i> , <i>t</i> are variables and λ is a constant. Then which one of the following is true?
(A)	If $\lambda = 1$, then the system has a unique solution.
(B)	If $\lambda = 2$, then the system has infinitely many solutions.
(C)	If $\lambda = 1$, then the system has infinitely many solutions.
(D)	If $\lambda = 2$, then the system has a unique solution.
Q.19	Consider the group $(\mathbb{Q}, +)$ and its subgroup $(\mathbb{Z}, +)$.
	For the quotient group \mathbb{Q}/\mathbb{Z} , which one of the following is FALSE?
(A)	\mathbb{Q}/\mathbb{Z} contains a subgroup isomorphic to (\mathbb{Z} , +).
(B)	There is exactly one group homomorphism from \mathbb{Q}/\mathbb{Z} to (\mathbb{Q} , +).
(C)	For all $n \in \mathbb{N}$, there exists $g \in \mathbb{Q}/\mathbb{Z}$ such that the order of g is n .
(D)	\mathbb{Q}/\mathbb{Z} is not a cyclic group.
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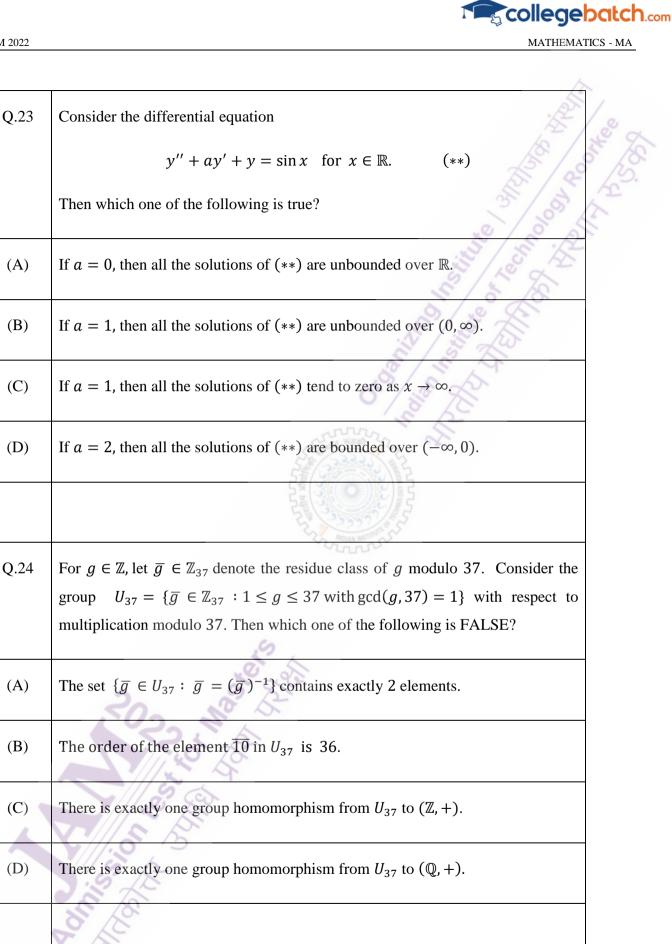
MATHEMATICS - MA

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Q.20	For $P \in M_5(\mathbb{R})$ and $i, j \in \{1, 2,, 5\}$, let p_{ij} denote the (i, j) th entry of P . Let
	$S = \{ P \in M_5(\mathbb{R}) : p_{ij} = p_{rs} \text{ for } i, j, r, s \in \{1, 2, \dots, 5\} \text{ with } i + r = j + s \}.$
	Then which one of the following is FALSE?
(A)	<i>S</i> is a subspace of the vector space over \mathbb{R} of all 5 × 5 symmetric matrices.
(B)	The dimension of S over \mathbb{R} is 5.
(C)	The dimension of S over \mathbb{R} is 11.
(D)	If $P \in S$ and all the entries of P are integers, then 5 divides the sum of all the
	diagonal entries of P.
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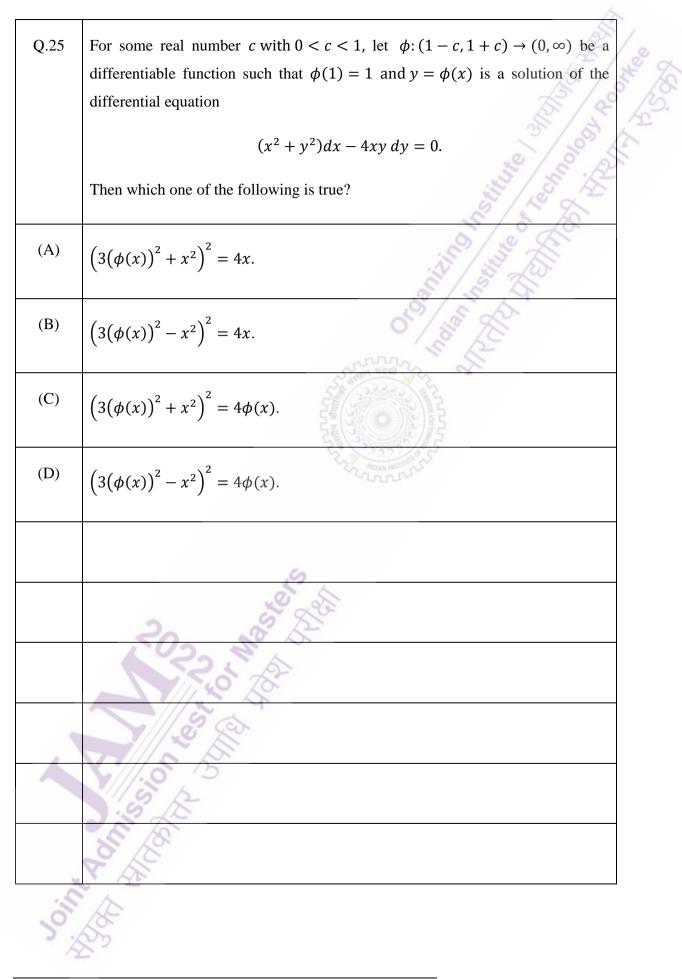




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Q.22	Let $H : \mathbb{R} \to \mathbb{R}$ be the function given by $H(x) = \frac{1}{2}(e^x + e^{-x})$ for $x \in \mathbb{R}$.	9
	Let $f : \mathbb{R} \to \mathbb{R}$ be defined by	10,5.
	$f(x) = \int_{0}^{\pi} H(x\sin\theta)d\theta \text{for } x \in \mathbb{R}.$	
	Then which one of the following is true?	
(A)	$xf''(x) + f'(x) + xf(x) = 0$ for all $x \in \mathbb{R}$.	
(B)	$xf''(x) - f'(x) + xf(x) = 0$ for all $x \in \mathbb{R}$.	
(C)	$xf''(x) + f'(x) - xf(x) = 0$ for all $x \in \mathbb{R}$.	
(D)	$xf''(x) - f'(x) - xf(x) = 0$ for all $x \in \mathbb{R}$.	
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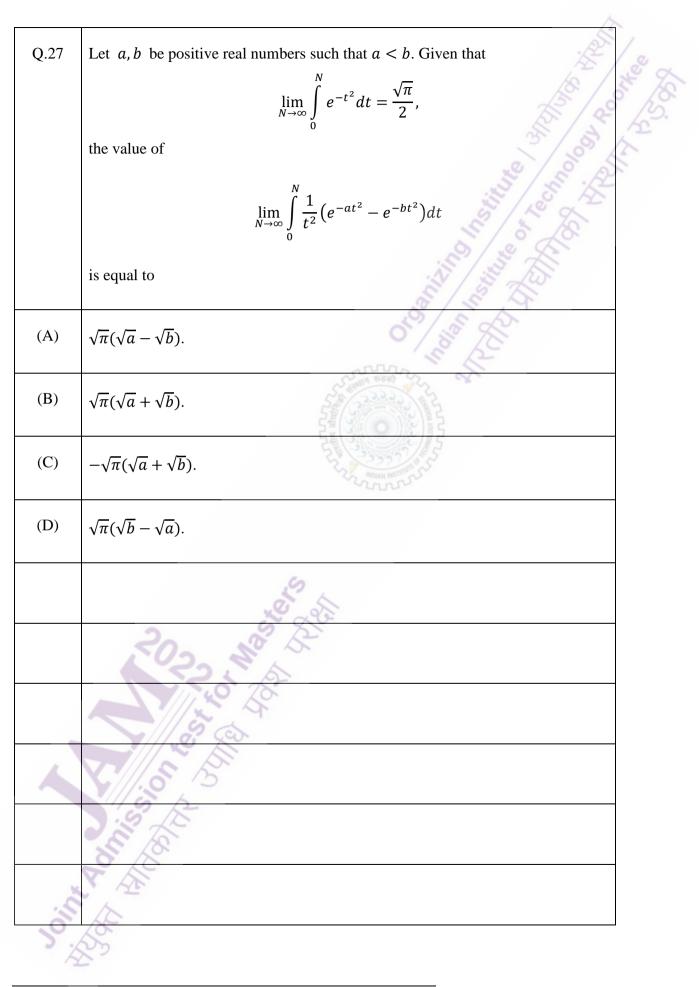




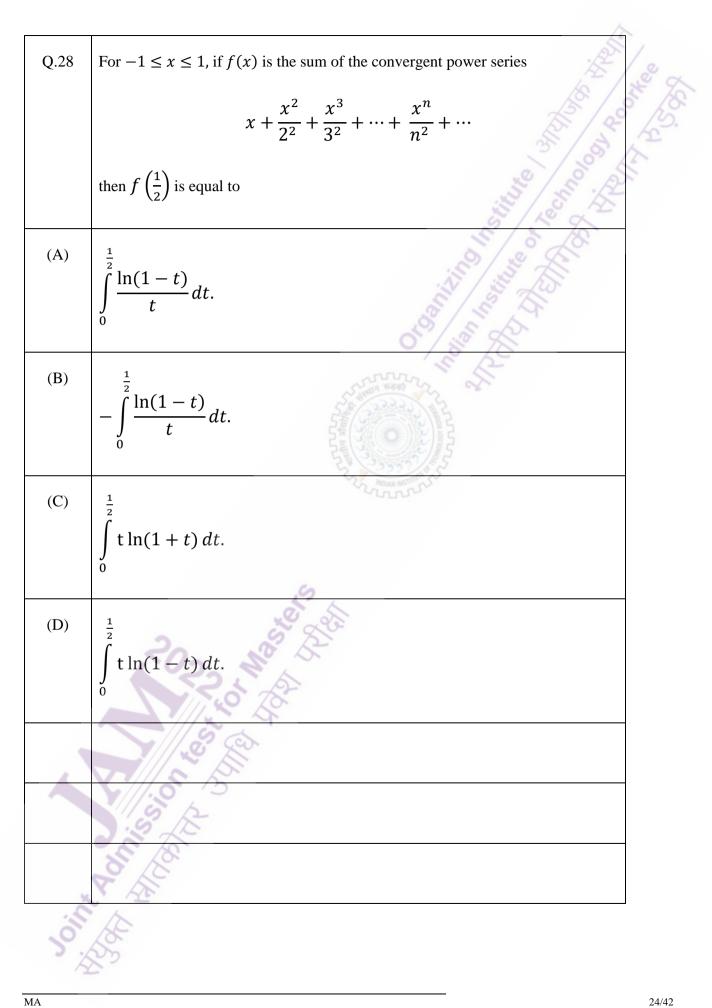


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For a 4×4 matrix $M \in M_4(\mathbb{C})$, let \overline{M} denote the matrix obtained from \overline{M} denotained from \overline{M} denotained from \overline{M}	The l
replacing each entry of M by its complex conjugate. Consider the re-	eal vector
space	E A
$H = \{ M \in M_4(\mathbb{C}) : M^\top = \overline{M} \}$	00.4
where M^{T} denotes the transpose of <i>M</i> . The dimension of <i>H</i> as a vector space	pace over
\mathbb{R} is equal to	20
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$f_{n}(x) = \int_{0}^{\pi} (x^{2} + (\cos \theta)\sqrt{x^{2} - 1})^{n} d\theta.$ Then which one of the following is true? (A) $f_{n}(x)$ is not a polynomial in x if n is odd and $n \ge 3$. (B) $f_{n}(x)$ is not a polynomial in x if n is even and $n \ge 4$. (C) $f_{n}(x)$ is a polynomial in x for all $n \in \mathbb{N}$. (D) $f_{n}(x)$ is not a polynomial in x for any $n \ge 3$. (D) $f_{n}(x)$ is not a polynomial in x for any $n \ge 3$. (D) $f_{n}(x)$ is not a polynomial in x for any $n \ge 3$. (D) $f_{n}(x)$ is not a polynomial in x for any $n \ge 3$. (A) 0 (B) 1 (C) -1		1
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Then which one of the following is true? Then which one of the following is true? (A) $f_n(x)$ is not a polynomial in x if n is odd and $n \ge 3$. (B) $f_n(x)$ is not a polynomial in x if n is even and $n \ge 4$. (C) $f_n(x)$ is a polynomial in x for all $n \in \mathbb{N}$. (D) $f_n(x)$ is not a polynomial in x for any $n \ge 3$. (D) $f_n(x)$ is not a polyn		$f_n(x) = \int_0^n \left(x^2 + (\cos \theta) \sqrt{x^2 - 1} \right)^n d\theta.$
(B) $f_n(x)$ is not a polynomial in x if n is even and $n \ge 4$. (C) $f_n(x)$ is a polynomial in x for all $n \in \mathbb{N}$. (D) $f_n(x)$ is not a polynomial in x for any $n \ge 3$. Q.30 Let P be a 3×3 real matrix having eigenvalues $\lambda_1 = 0, \lambda_2 = 1$ and $\lambda_3 = -1$. Further, $v_1 = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}, v_2 = \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix}$ and $v_3 = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}$ are eigenvectors of the matrix P corresponding to the eigenvalues λ_1, λ_2 and λ_3 , respectively. Then the entry in the first row and the third column of P is (A) 0 (B) 1 (C) -1		S A
(C) $f_n(x)$ is a polynomial in x for all $n \in \mathbb{N}$. (D) $f_n(x)$ is not a polynomial in x for any $n \ge 3$. (D) $f_n(x)$ is not a polynomial in x for any $n \ge 3$. Q.30 Let P be a 3×3 real matrix having eigenvalues $\lambda_1 = 0, \lambda_2 = 1$ and $\lambda_3 = -1$. Further, $v_1 = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}, v_2 = \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix}$ and $v_3 = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}$ are eigenvectors of the matrix P corresponding to the eigenvalues λ_1, λ_2 and λ_3 , respectively. Then the entry in the first row and the third column of P is (A) 0 (B) 1 (C) -1	(A)	$f_n(x)$ is not a polynomial in x if n is odd and $n \ge 3$.
(D) $f_n(x)$ is not a polynomial in x for any $n \ge 3$. (D) $f_n(x)$ is not a polynom	(B)	$f_n(x)$ is not a polynomial in x if n is even and $n \ge 4$.
Q.30 Let P be a 3×3 real matrix having eigenvalues $\lambda_1 = 0, \lambda_2 = 1$ and $\lambda_3 = -1$. Further, $v_1 = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}, v_2 = \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix}$ and $v_3 = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}$ are eigenvectors of the matrix P corresponding to the eigenvalues λ_1, λ_2 and λ_3 , respectively. Then the entry in the first row and the third column of P is (A) 0 (B) 1 (C) -1	(C)	$f_n(x)$ is a polynomial in x for all $n \in \mathbb{N}$.
Further, $v_1 = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$, $v_2 = \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix}$ and $v_3 = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}$ are eigenvectors of the matrix P corresponding to the eigenvalues λ_1, λ_2 and λ_3 , respectively. Then the entry in the first row and the third column of P is (A) 0 (B) 1 (C) -1	(D)	$f_n(x)$ is not a polynomial in x for any $n \ge 3$.
Further, $v_1 = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$, $v_2 = \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix}$ and $v_3 = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}$ are eigenvectors of the matrix P corresponding to the eigenvalues λ_1, λ_2 and λ_3 , respectively. Then the entry in the first row and the third column of P is (A) 0 (B) 1 (C) -1		
corresponding to the eigenvalues λ_1, λ_2 and λ_3 , respectively. Then the entry in the first row and the third column of P is (A) 0 (B) 1 (C) -1	Q.30	Let P be a 3 × 3 real matrix having eigenvalues $\lambda_1 = 0, \lambda_2 = 1$ and $\lambda_3 = -1$.
the first row and the third column of P is (A) 0 (B) 1 (C) -1		Further, $v_1 = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$, $v_2 = \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix}$ and $v_3 = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}$ are eigenvectors of the matrix <i>P</i>
(A) 0 (B) 1 (C) -1		corresponding to the eigenvalues λ_1, λ_2 and λ_3 , respectively. Then the entry in
(B) 1 (C) -1		the first row and the third column of P is
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ction]	B: Q.31 – Q.40 Carry TWO marks each.
Q.31	Let $(-c, c)$ be the largest open interval in \mathbb{R} (where <i>c</i> is either a positive real number or $c = \infty$) on which the solution $y(x)$ of the differential equation
	$\frac{dy}{dx} = x^2 + y^2 + 1$ with initial condition $y(0) = 0$
	exists and is unique. Then which of the following is/are true?
(A)	y(x) is an odd function on $(-c, c)$.
(B)	y(x) is an even function on $(-c, c)$.
(C)	$(y(x))^2$ has a local minimum at 0.
(D)	$(y(x))^2$ has a local maximum at 0.
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Q.32	Let <i>S</i> be the set of all continuous functions $f: [-1,1] \rightarrow \mathbb{R}$ satisfying the following
	three conditions:
	(i) f is infinitely differentiable on the open interval $(-1,1)$,
	(ii) the Taylor series
	$f(0) + f'(0)x + \frac{f''(0)}{2!}x^2 + \cdots$
	of <i>f</i> at 0 converges to $f(x)$ for each $x \in (-1,1)$,
	(iii) $f\left(\frac{1}{n}\right) = 0$ for all $n \in \mathbb{N}$.
	Then which of the following is/are true?
(A)	$f(0) = 0$ for every $f \in S$.
(B)	$f'\left(\frac{1}{2}\right) = 0$ for every $f \in S$.
(C)	There exists $f \in S$ such that $f'\left(\frac{1}{2}\right) \neq 0$.
	Se de
(D)	There exists $f \in S$ such that $f(x) \neq 0$ for some $x \in [-1,1]$.
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Q.33	Define $f:[0,1] \rightarrow [0,1]$ by
	$\int 1 \text{if } x = 0,$
	$f(x) = \begin{cases} 1 & \text{if } x = 0, \\ \frac{1}{n} & \text{if } x = \frac{m}{n} \text{ for some } m, n \in \mathbb{N} \text{ with } m \le n \text{ and } \gcd(m, n) = 1, \\ 0 & \text{if } x \in [0, 1] \text{ is irrational.} \end{cases}$
	0 if $x \in [0,1]$ is irrational.
	and define $g: [0,1] \rightarrow [0,1]$ by
	$g(x) = \begin{cases} 0 & \text{if } x = 0, \\ 1 & \text{if } x \in (0,1]. \end{cases}$
	Then which of the following is/are true?
(A)	<i>f</i> is Riemann integrable on [0,1].
(B)	<i>g</i> is Riemann integrable on [0,1].
(C)	The composite function $f \circ g$ is Riemann integrable on [0,1].
(D)	The composite function $g \circ f$ is Riemann integrable on [0,1].
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Q.34	Let <i>S</i> be the set of all functions $f \colon \mathbb{R} \to \mathbb{R}$ satisfying
	$ f(x) - f(y) ^2 \le x - y ^3$ for all $x, y \in \mathbb{R}$.
	Then which of the following is/are true?
(A)	Every function in <i>S</i> is differentiable.
(B)	There exists a function $f \in S$ such that f is differentiable, but f is not twice differentiable.
(C)	There exists a function $f \in S$ such that f is twice differentiable, but f is not thrice differentiable.
(D)	Every function in <i>S</i> is infinitely differentiable.
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Q.35	A real-valued function $y(x)$ defined on \mathbb{R} is said to be periodic if there exists a
	real number $T > 0$ such that $y(x + T) = y(x)$ for all $x \in \mathbb{R}$.
	Consider the differential equation
	12
	$\frac{d^2y}{dx^2} + 4y = \sin(ax), x \in \mathbb{R}, \tag{(*)}$
	where $a \in \mathbb{R}$ is a constant.
	Then which of the following is/are true?
	Then which of the following is/are true:
(A)	All solutions of (*) are periodic for every choice of a .
(B)	All solutions of (*) are periodic for every choice of $a \in \mathbb{R} - \{-2, 2\}$.
(C)	All solutions of (*) are periodic for every choice of $a \in \mathbb{Q} - \{-2, 2\}$.
	And
(D)	If $a \in \mathbb{R} - \mathbb{Q}$, then there is a unique periodic solution of (*).
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Q.36	Let <i>M</i> be a positive real number and let $u, v : \mathbb{R}^2 \to \mathbb{R}$ be continuous functions satisfying
	$\sqrt{u(x,y)^2 + v(x,y)^2} \ge M\sqrt{x^2 + y^2} \text{for all } (x,y) \in \mathbb{R}^2.$
	Let $F: \mathbb{R}^2 \to \mathbb{R}^2$ be given by
	$F(x,y) = (u(x,y),v(x,y))$ for $(x,y) \in \mathbb{R}^2$.
	Then which of the following is/are true?
(A)	F is injective.
(B)	If K is open in \mathbb{R}^2 , then $F(K)$ is open in \mathbb{R}^2 .
(C)	If <i>K</i> is closed in \mathbb{R}^2 , then <i>F</i> (<i>K</i>) is closed in \mathbb{R}^2 .
(D)	If <i>E</i> is closed and bounded in \mathbb{R}^2 , then $F^{-1}(E)$ is closed and bounded in \mathbb{R}^2 .
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Q.37	Let <i>G</i> be a finite group of order at least two and let <i>e</i> denote the identity element of <i>G</i> . Let $\sigma: G \to G$ be a bijective group homomorphism that satisfies the following
	two conditions:
	(i) If $\sigma(g) = g$ for some $g \in G$, then $g = e$,
	(ii) $(\sigma \circ \sigma)(g) = g$ for all $g \in G$.
	Then which of the following is/are correct?
(A)	For each $g \in G$, there exists $h \in G$ such that $h^{-1}\sigma(h) = g$.
(B)	There exists $x \in G$ such that $x\sigma(x) \neq e$.
(C)	The map σ satisfies $\sigma(x) = x^{-1}$ for every $x \in G$.
(D)	The order of the group G is an odd number.
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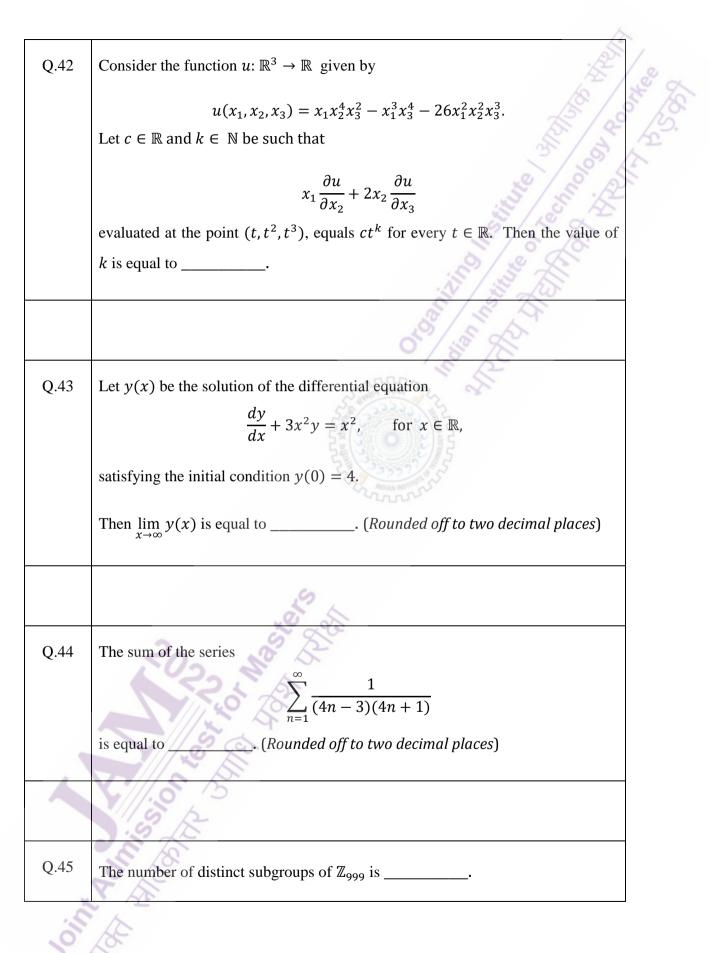
Q.38	Let (x_n) be a sequence of real numbers. Consider the set
	$P = \{n \in \mathbb{N} : x_n > x_m \text{ for all } m \in \mathbb{N} \text{ with } m > n\}.$
	Then which of the following is/are true?
(A)	If P is finite, then (x_n) has a monotonically increasing subsequence.
(B)	If P is finite, then no subsequence of (x_n) is monotonically increasing.
(C)	If P is infinite, then (x_n) has a monotonically decreasing subsequence.
(D)	If <i>P</i> is infinite, then no subsequence of (x_n) is monotonically decreasing.
Q.39	Let <i>V</i> be the real vector space consisting of all polynomials in one variable with real coefficients and having degree at most 5, together with the zero polynomial. Let $T: V \to \mathbb{R}$ be the linear map defined by $T(1) = 1$ and $T(x(x-1)\cdots(x-k+1)) = 1$ for $1 \le k \le 5$. Then which of the following is/are true?
(A)	$T(x^4) = 15.$
(B)	$T(x^3) = 5.$
(C)	$T(x^4) = 14.$
(D)	$T(x^3) = 3.$
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Q.40	Let <i>P</i> be a fixed 3×3 matrix with entries in \mathbb{R} . Which of the following maps
	from $M_3(\mathbb{R})$ to $M_3(\mathbb{R})$ is/are linear?
	2 2 2
(A)	$T_1: M_3(\mathbb{R}) \to M_3(\mathbb{R})$ given by $T_1(M) = MP - PM$ for $M \in M_3(\mathbb{R})$.
(B)	$T_2: M_3(\mathbb{R}) \to M_3(\mathbb{R})$ given by $T_2(M) = M^2 P - P^2 M$ for $M \in M_3(\mathbb{R})$.
(C)	$T_3: M_3(\mathbb{R}) \to M_3(\mathbb{R})$ given by $T_3(M) = MP^2 + P^2M$ for $M \in M_3(\mathbb{R})$.
(D)	$T_4: M_3(\mathbb{R}) \to M_3(\mathbb{R})$ given by $T_4(M) = MP^2 - PM^2$ for $M \in M_3(\mathbb{R})$.
ection	C: Q.41 – Q.50 Carry ONE mark each.
Q.41	The value of the limit
	$\lim_{n \to \infty} \left(\frac{(1^4 + 2^4 + \dots + n^4)}{n^5} + \frac{1}{\sqrt{n}} \left(\frac{1}{\sqrt{n+1}} + \frac{1}{\sqrt{n+2}} + \dots + \frac{1}{\sqrt{4n}} \right) \right)$
	is equal to (<i>Rounded off to two decimal places</i>)
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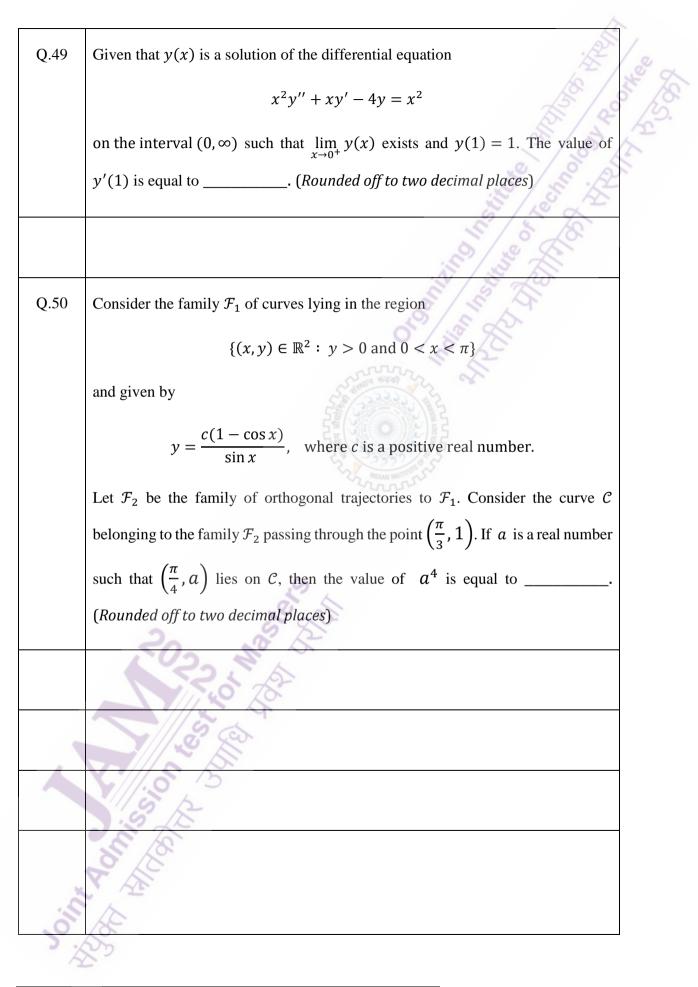






Q.47 Let $y(x)$ be the solution of the differential equation $xy^2y' + y^3 = \frac{\sin x}{x}$ for $x > 0$, satisfying $y\left(\frac{\pi}{2}\right) = 0$. Then the value of $y\left(\frac{5\pi}{2}\right)$ is equal to (Rounded off to two decimal places) Q.48 Consider the region $G = \{(x, y, z) \in \mathbb{R}^3 : 0 < z < x^2 - y^2, x^2 + y^2 < 1\}$. Then the volume of G is equal to (Rounded off to two decimal		· Land
Q.47 Let $y(x)$ be the solution of the differential equation $xy^2y' + y^3 = \frac{\sin x}{x}$ for $x > 0$, satisfying $y\left(\frac{\pi}{2}\right) = 0$. Then the value of $y\left(\frac{5\pi}{2}\right)$ is equal to (Rounded off to two decimal places) Q.48 Consider the region $G = \{(x, y, z) \in \mathbb{R}^3 : 0 < z < x^2 - y^2, x^2 + y^2 < 1\}$. Then the volume of G is equal to (Rounded off to two decimal		10-1
$xy^{2}y' + y^{3} = \frac{\sin x}{x} \text{ for } x > 0,$ satisfying $y\left(\frac{\pi}{2}\right) = 0.$ Then the value of $y\left(\frac{5\pi}{2}\right)$ is equal to (Rounded off to two decimal places) Q.48 Consider the region $G = \{(x, y, z) \in \mathbb{R}^{3} : 0 < z < x^{2} - y^{2}, x^{2} + y^{2} < 1\}.$ Then the volume of G is equal to (Rounded off to two decimal	Q.46	The number of elements of order 12 in the symmetric group S_7 is equal to
$xy^{2}y' + y^{3} = \frac{\sin x}{x} \text{ for } x > 0,$ satisfying $y\left(\frac{\pi}{2}\right) = 0.$ Then the value of $y\left(\frac{5\pi}{2}\right)$ is equal to (Rounded off to two decimal places) Q.48 Consider the region $G = \{(x, y, z) \in \mathbb{R}^{3} : 0 < z < x^{2} - y^{2}, x^{2} + y^{2} < 1\}.$ Then the volume of G is equal to (Rounded off to two decimal		3 5
$xy^{2}y' + y^{3} = \frac{\sin x}{x} \text{ for } x > 0,$ satisfying $y\left(\frac{\pi}{2}\right) = 0.$ Then the value of $y\left(\frac{5\pi}{2}\right)$ is equal to (Rounded off to two decimal places) Q.48 Consider the region $G = \{(x, y, z) \in \mathbb{R}^{3} : 0 < z < x^{2} - y^{2}, x^{2} + y^{2} < 1\}.$ Then the volume of G is equal to (Rounded off to two decimal		2 2 2
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Then the value of $y\left(\frac{5\pi}{2}\right)$ is equal to (Rounded off to two decimal places) Q.48 Consider the region $G = \{(x, y, z) \in \mathbb{R}^3 : 0 < z < x^2 - y^2, x^2 + y^2 < 1\}.$ Then the volume of G is equal to (Rounded off to two decimal		$xy^2y' + y^3 = \frac{\sin x}{x}$ for $x > 0$,
places)Q.48Consider the region $G = \{(x, y, z) \in \mathbb{R}^3 : 0 < z < x^2 - y^2, x^2 + y^2 < 1\}.$ Then the volume of G is equal to (Rounded off to two decimal		satisfying $y\left(\frac{\pi}{2}\right) = 0.$
$G = \{(x, y, z) \in \mathbb{R}^3 : 0 < z < x^2 - y^2, x^2 + y^2 < 1\}.$ Then the volume of G is equal to (Rounded off to two decimal		
$G = \{(x, y, z) \in \mathbb{R}^3 : 0 < z < x^2 - y^2, x^2 + y^2 < 1\}.$ Then the volume of G is equal to (Rounded off to two decimal		ROBAN INSTITUTE
$G = \{(x, y, z) \in \mathbb{R}^3 : 0 < z < x^2 - y^2, x^2 + y^2 < 1\}.$ Then the volume of G is equal to (Rounded off to two decimal		
$G = \{(x, y, z) \in \mathbb{R}^3 : 0 < z < x^2 - y^2, x^2 + y^2 < 1\}.$ Then the volume of G is equal to (Rounded off to two decimal		
$G = \{(x, y, z) \in \mathbb{R}^3 : 0 < z < x^2 - y^2, x^2 + y^2 < 1\}.$ Then the volume of G is equal to (Rounded off to two decimal		
$G = \{(x, y, z) \in \mathbb{R}^3 : 0 < z < x^2 - y^2, x^2 + y^2 < 1\}.$ Then the volume of G is equal to (Rounded off to two decimal	0.48	Consider the region
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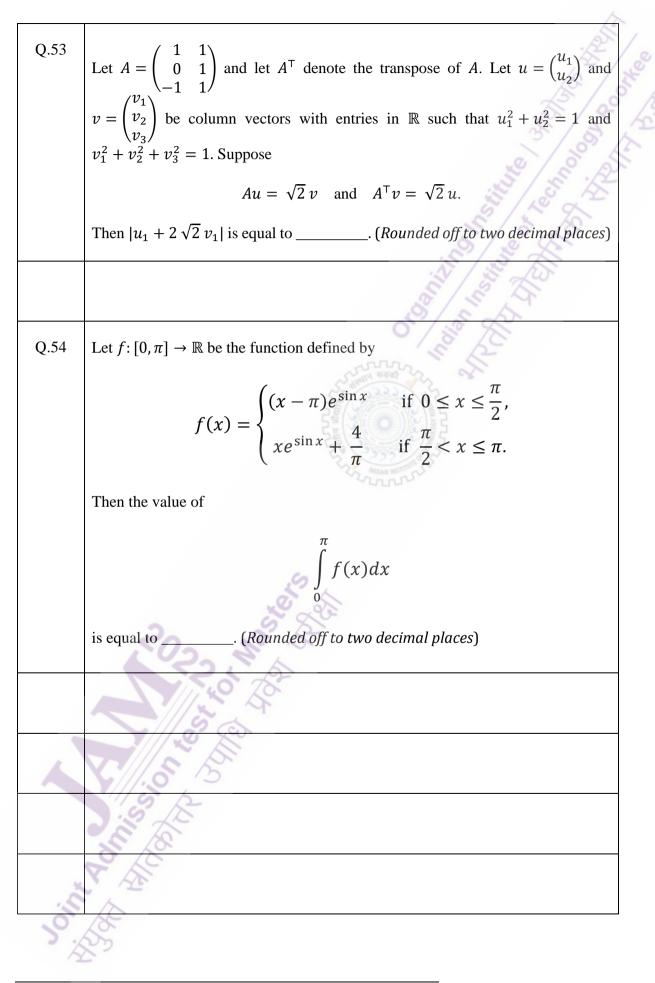






tion	C: Q.51 – Q.60 Carry TWO marks each.
Q.51	For $t \in \mathbb{R}$, let [t] denote the greatest integer less than or equal to t.
	Let $D = \{(x, y) \in \mathbb{R}^2 : x^2 + y^2 < 4\}$. Let $f: D \to \mathbb{R}$ and $g: D \to \mathbb{R}$ be defined
	by $f(0,0) = g(0,0) = 0$ and
	$f(x,y) = [x^{2} + y^{2}] \frac{x^{2}y^{2}}{x^{4} + y^{4}}, \qquad g(x,y) = [y^{2}] \frac{xy}{x^{2} + y^{2}}$
	for $(x, y) \neq (0, 0)$. Let E be the set of points of D at which both f and g are
	discontinuous. The number of elements in the set <i>E</i> is
	And the second s
Q.52	If <i>G</i> is the region in \mathbb{R}^2 given by
	$G = \left\{ (x, y) \in \mathbb{R}^2 : x^2 + y^2 < 1, \ \frac{x}{\sqrt{3}} < y < \sqrt{3}x, \ x > 0, \ y > 0 \right\}$
	then the value of
	$\frac{200}{\pi} \iint_G x^2 dx dy$
	is equal to (Rounded off to two decimal places)
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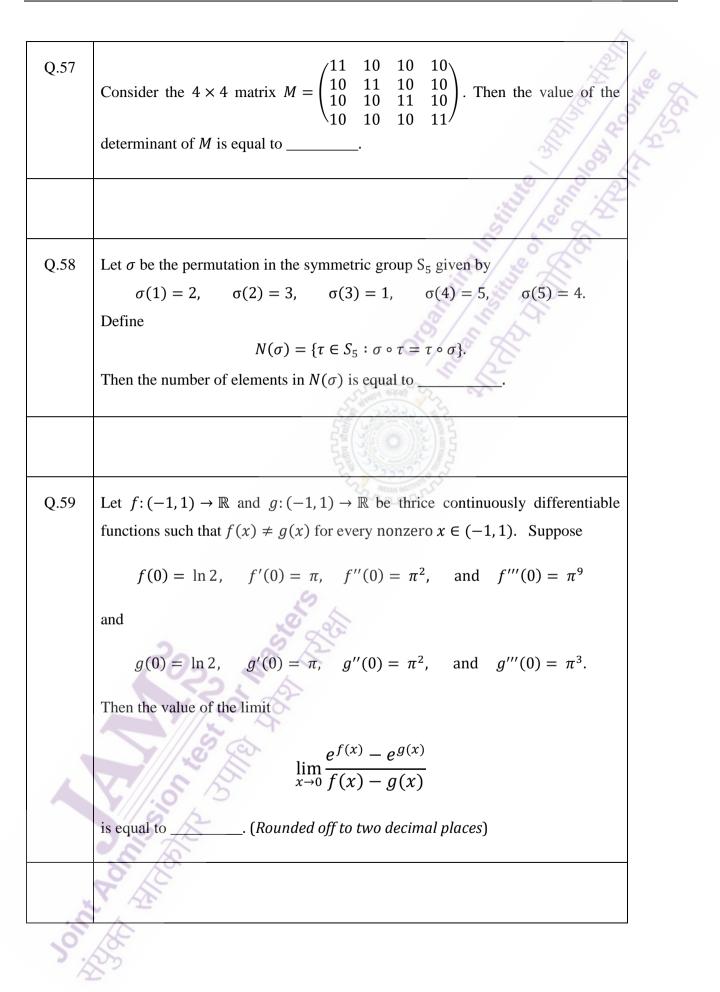






Q.55 Let r be the radius of convergence of the power series $\frac{1}{3} + \frac{x}{5} + \frac{x^2}{3^2} + \frac{x^3}{5^2} + \frac{x^4}{3^3} + \frac{x^5}{5^3} + \frac{x^6}{3^4} + \frac{x^7}{5^4} + \cdots$ Then the value of r^2 is equal to _____. (Rounded off to two decimal places) Define $f: \mathbb{R}^2 \to \mathbb{R}$ by Q.56 $f(x, y) = x^2 + 2y^2 - x$ for $(x, y) \in \mathbb{R}^2$. Let $D = \{(x, y) \in \mathbb{R}^2 : x^2 + y^2 \le 1\}$ and $E = \{(x, y) \in \mathbb{R}^2 : \frac{x^2}{4} + \frac{y^2}{9} \le 1\}.$ Consider the sets $D_{\max} = \{(a, b) \in D : f \text{ has absolute maximum on } D \text{ at } (a, b)\},\$ $D_{\min} = \{(a, b) \in D : f \text{ has absolute minimum on } D \text{ at } (a, b)\},\$ $E_{\max} = \{(c, d) \in E : f \text{ has absolute maximum on } E \text{ at } (c, d)\},\$ $E_{\min} = \{(c, d) \in E : f \text{ has absolute minimum on } E \text{ at } (c, d)\}.$ Then the total number of elements in the set $D_{\max} \cup D_{\min} \cup E_{\max} \cup E_{\min}$ is equal to







Q.60 If
$$f: [0, \infty) \to \mathbb{R}$$
 and $g: [0, \infty) \to [0, \infty)$ are continuous functions such that

$$\int_{0}^{x^{3}+x^{2}} f(t)dt = x^{2} \text{ and } \int_{0}^{g(x)} t^{2}dt = 9(x+1)^{3} \text{ for all } x \in [0, \infty),$$
then the value of
 $f(2) + g(2) + 16 f(12)$
is equal to _____. (Rounded off to two decimal places)

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Q.3	Consider a classical ideal gas of N molecules in equilibrium at temperature T .
	Each molecule has two energy levels, $-\epsilon$ and ϵ . The mean energy of the gas is
(A)	0
(B)	$N\epsilon \tanh\left(\frac{\epsilon}{k_BT}\right)$
(C)	$-N\epsilon \tanh\left(\frac{\epsilon}{k_BT}\right)$
(D)	$\frac{\epsilon}{2}$
Q.4	At a temperature T, let β and κ denote the volume expansivity and isothermal
	compressibility of a gas, respectively. Then $\frac{\beta}{\kappa}$ is equal to
(A)	$\left(\frac{\partial P}{\partial T}\right)_V$
(B)	$\left(\frac{\partial P}{\partial V}\right)_T$
(C)	$\left(\frac{\partial T}{\partial P}\right)_V$
(D)	$\left(\frac{\partial T}{\partial V}\right)_P$
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Q.5	The resultant of the binary subtraction 1110101 – 0011110 is	2
(A)	1001111	15.
(B)	1010111	
(C)	1010011	
(D)	1010001	
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Q.6	Consider a particle trapped in a three-dimensional potential well such that $U(x, y, z) = 0$ for $0 \le x \le a$, $0 \le y \le a$, $0 \le z \le a$ and $U(x, y, z) = \infty$ everywhere else. The degeneracy of the 5 th excited state is	
(A)	1	
(B)	3	
(C)	6 2023 1 1 1	
(D)	9	
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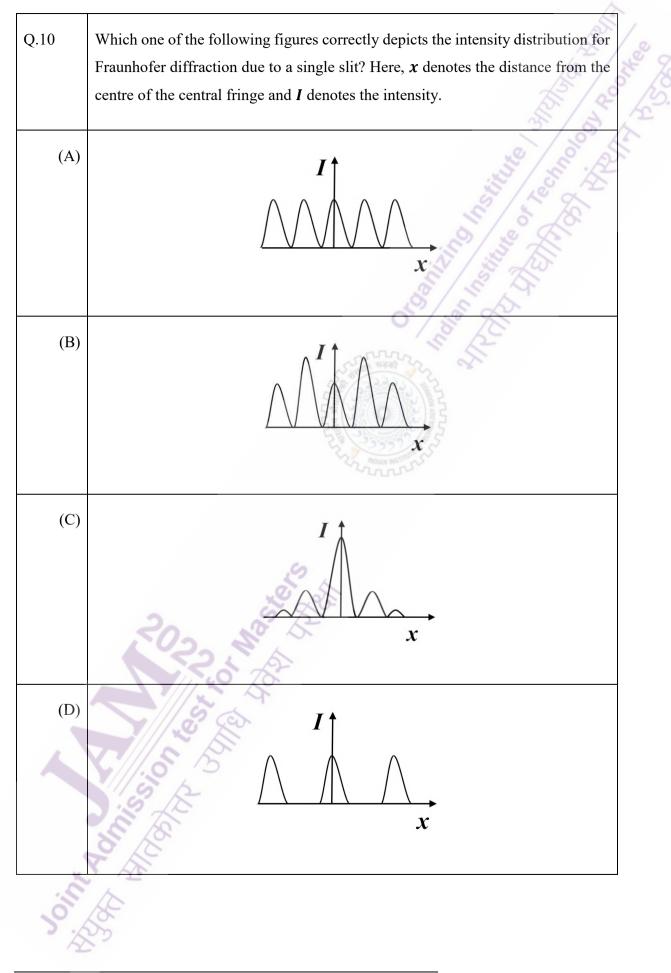


Q.7	A particle of mass m and angular momentum L moves in space where its potential energy is $U(r) = kr^2$ ($k > 0$) and r is the radial coordinate. If the particle moves in a circular orbit, then the radius of the orbit is	and brief
(A)	$\left(\frac{L^2}{mk}\right)^{\frac{1}{4}}$	
(B)	$\left(\frac{L^2}{2mk}\right)^{\frac{1}{4}}$	
(C)	$\left(\frac{2L^2}{mk}\right)^{\frac{1}{4}}$	
(D)	$\left(\frac{4L^2}{mk}\right)^{\frac{1}{4}}$	
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Q.8	Consider a two-dimensional force field
	$\vec{F}(x,y) = (5x^2 + ay^2 + bxy)\hat{x} + (4x^2 + 4xy + y^2)\hat{y}.$
	If the force field is conservative, then the values of a and b are
(A)	a = 2 and $b = 4$
(B)	a = 2 and $b = 8$
(C)	a = 4 and $b = 2$
(D)	a = 8 and $b = 2$
Q.9	Consider an electrostatic field \vec{E} in a region of space. Identify the INCORRECT statement.
(A)	The work done in moving a charge in a closed path inside the region is zero
(B)	The curl of \vec{E} is zero
(C)	The field can be expressed as the gradient of a scalar potential
(D)	The potential difference between any two points in the region is always zero
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	A: Q.11 – Q.30 Carry TWO marks each.
Q.11	The function $f(x) = e^{\sin x}$ is expanded as a Taylor series in x, around $x = 0$,
	in the form $f(x) = \sum_{n=0}^{\infty} a_n x^n$. The value of $a_0 + a_1 + a_2$ is
(A)	0
(B)	$\frac{3}{2}$
(C)	$\frac{5}{2}$
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(D)	5
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Q.12	Consider a unit circle C in the xy plane, centered at the origin. The value of the
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	integral $\oint [(\sin x - y)dx - (\sin y - x)dy]$ over the circle <i>C</i> , traversed anticlockwise, is
(A)	6
	anticlockwise, is 0
(A) (B)	anticlockwise, is
	anticlockwise, is 0
(B) (C)	anticlockwise, is 0 2π 3π
(B)	anticlockwise, is 0 2π
(B) (C)	anticlockwise, is 0 2π 3π

Q.13	The current through a series RL circuit, subjected to a constant <i>emf</i> \mathcal{E} , obeys
	$L\frac{di}{dt} + iR = \mathcal{E}$. Let $L = 1 \ mH$, $R = 1 \ k\Omega$ and $\mathcal{E} = 1 \ V$. The initial condition
	is $i(0) = 0$. At $t = 1 \mu s$, the current in mA is
(A)	$1 - 2e^{-2}$
(B)	$1 - 2e^{-1}$
(C)	$1 - e^{-1}$
(D)	$2 - 2e^{-1}$
Q.14	An ideal gas in equilibrium at temperature <i>T</i> expands isothermally to twice its initial volume. If ΔS , ΔU and ΔF denote the changes in its entropy, internal energy and Helmholtz free energy respectively, then
(A)	$\Delta S < 0, \Delta U > 0, \Delta F < 0$
(B)	$\Delta S > 0, \Delta U = 0, \Delta F < 0$
(C)	$\Delta S < 0, \Delta U = 0, \Delta F > 0$
(D)	$\Delta S > 0, \Delta U > 0, \Delta F = 0$
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Q.15	In a dilute gas, the number of molecules with free path length $\geq x$ is given by $N(x) = N_0 e^{-x/\lambda}$, where N_0 is the total number of molecules and λ is the mean
	free path. The fraction of molecules with free path lengths between λ and 2λ is
(A)	
(B)	$\frac{e}{e-1}$
(C)	$\frac{e^2}{e-1}$
(D)	$\frac{e-1}{e^2}$
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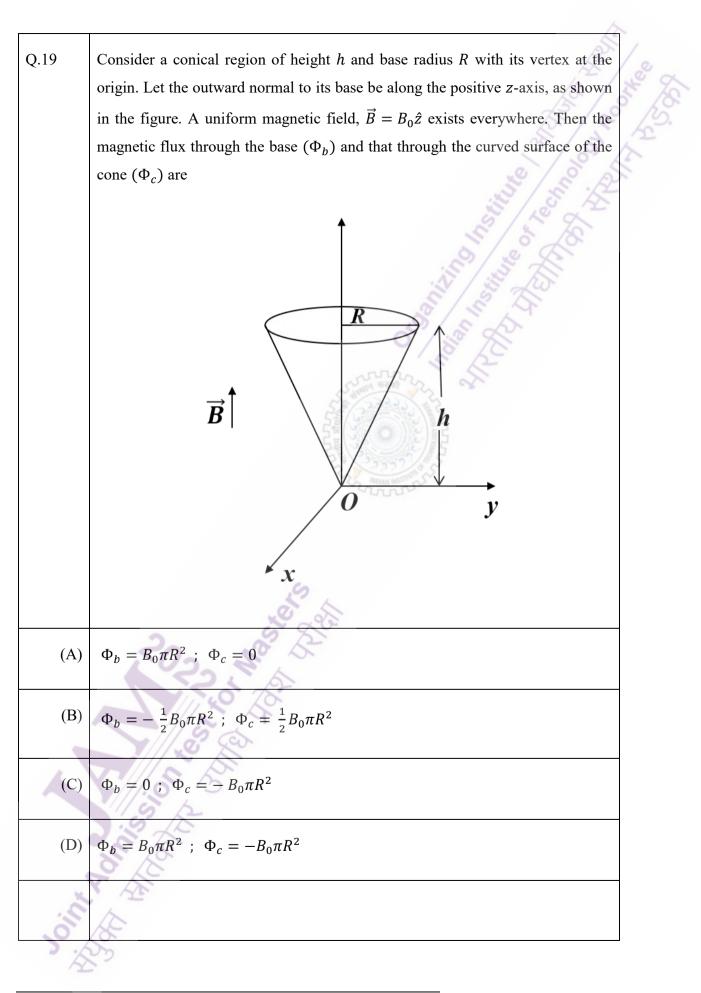
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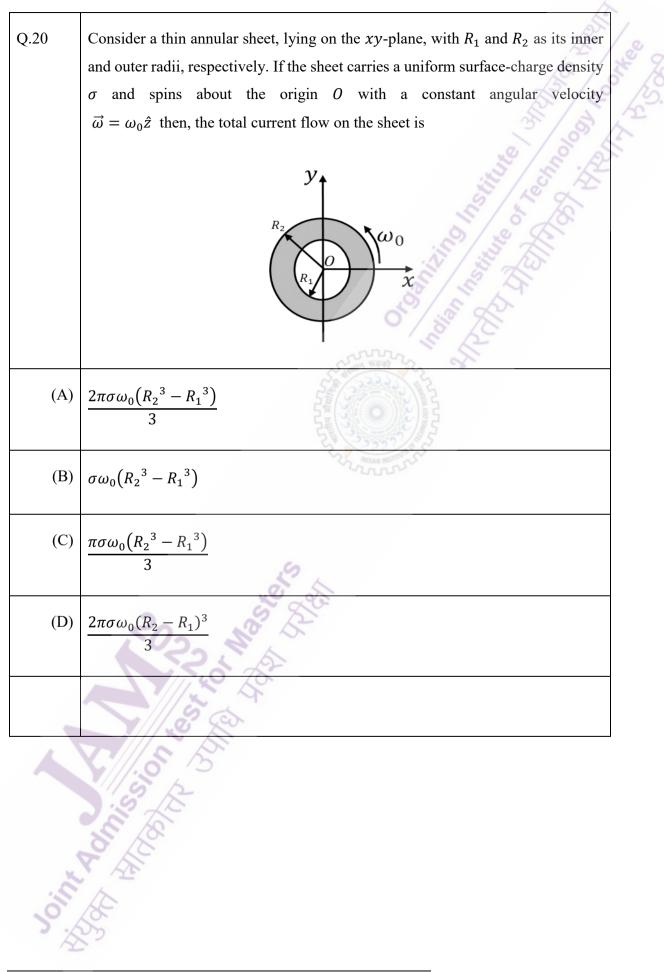
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Q.16	Consider a quantum particle trapped in a one-dimensional potential well in the
	region $[-L/2 < x < L/2]$, with infinitely high barriers at $x = -L/2$ and $x = L/2$. The stationary wave function for the ground state is $\psi(x) =$
	-
	$\sqrt{\frac{2}{L}\cos\left(\frac{\pi x}{L}\right)}$. The uncertainties in momentum and position satisfy
(A)	$\Delta p = \frac{\pi \hbar}{L}$ and $\Delta x = 0$
(B)	$\Delta p = \frac{2\pi\hbar}{L} \text{ and } 0 < \Delta x < \frac{L}{2\sqrt{3}}$
(C)	$\Delta p = \frac{\pi \hbar}{L} \text{ and } \Delta x > \frac{L}{2\sqrt{3}}$
(D)	$\Delta p = 0$ and $\Delta x = \frac{L}{2}$
Q.17	Consider a particle of mass m moving in a plane with a constant radial speed \dot{r}
	and a constant angular speed $\dot{\theta}$. The acceleration of the particle in (r, θ)
	coordinates is
(A)	$2r\dot{ heta}^2\hat{r}-\dot{r}\dot{ heta}\hat{ heta}$
(B)	$-r\dot{ heta}^2\hat{r}+2\dot{r}\dot{ heta}\hat{ heta}$
(C)	$\ddot{r}\hat{r} + r\ddot{ heta}\hat{ heta}$
(D)	$\ddot{r} heta\hat{r}+r\ddot{ heta}\hat{ heta}$
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Q.18	A planet of mass m moves in an elliptical orbit. Its maximum and minimum distances from the Sun are R and r , respectively. Let G denote the universal
	gravitational constant, and M the mass of the Sun. Assuming $M >> m$, the
	angular momentum of the planet with respect to the center of the Sun is
(A)	$m\sqrt{\frac{2GMRr}{(R+r)}}$
(B)	$m\sqrt{\frac{GMRr}{2(R+r)}}$
(C)	$m\sqrt{\frac{GMRr}{(R+r)}}$
(D)	$2m\sqrt{\frac{2GMRr}{(R+r)}}$
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Q.21	A radioactive nucleus has a decay constant λ and its radioactive daughter nucleus has a decay constant 10λ . At time $t = 0$, N_0 is the number of parent nuclei and there are no daughter nuclei present. $N_1(t)$ and $N_2(t)$ are the number of parent
	and daughter nuclei present at time t, respectively.
	The ratio $N_2(t)/N_1(t)$ is
(A)	$\frac{1}{9} \left[1 - e^{-9\lambda t} \right]$
(B)	$\frac{1}{10} \left[1 - e^{-10\lambda t} \right]$
(C)	$\left[1-e^{-10\lambda t}\right]$
(D)	$[1-e^{-9\lambda t}]$

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Q.22	A uniform magnetic field $\vec{B} = B_0 \hat{z}$, where $B_0 > 0$ exists as shown in the figure. A charged particle of mass <i>m</i> and charge q ($q > 0$) is released at the origin, in the <i>yz</i> -plane, with a velocity \vec{v} directed at an angle $\theta = 45^\circ$ with respect to the
	positive <i>z</i> -axis. Ignoring gravity, which one of the following is TRUE .
	$ \begin{array}{c} $
(A)	The initial acceleration $\vec{a} = \frac{qvB_0}{\sqrt{2}m}\hat{x}$
(B)	The initial acceleration $\vec{a} = \frac{qvB_0}{\sqrt{2}m}\hat{y}$
(C)	The particle moves in a circular path
(D)	The particle continues in a straight line with constant speed
	22.5 A
	The particle continues in a straight line with constant speed
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Q.23	For an ideal intrinsic semiconductor, the Fermi energy at 0 K	20
(A)	lies at the top of the valence band	60
(B)	lies at the bottom of the conduction band	
(C)	lies at the center of the bandgap	
(D)	lies midway between center of the bandgap and bottom of the conduction band	
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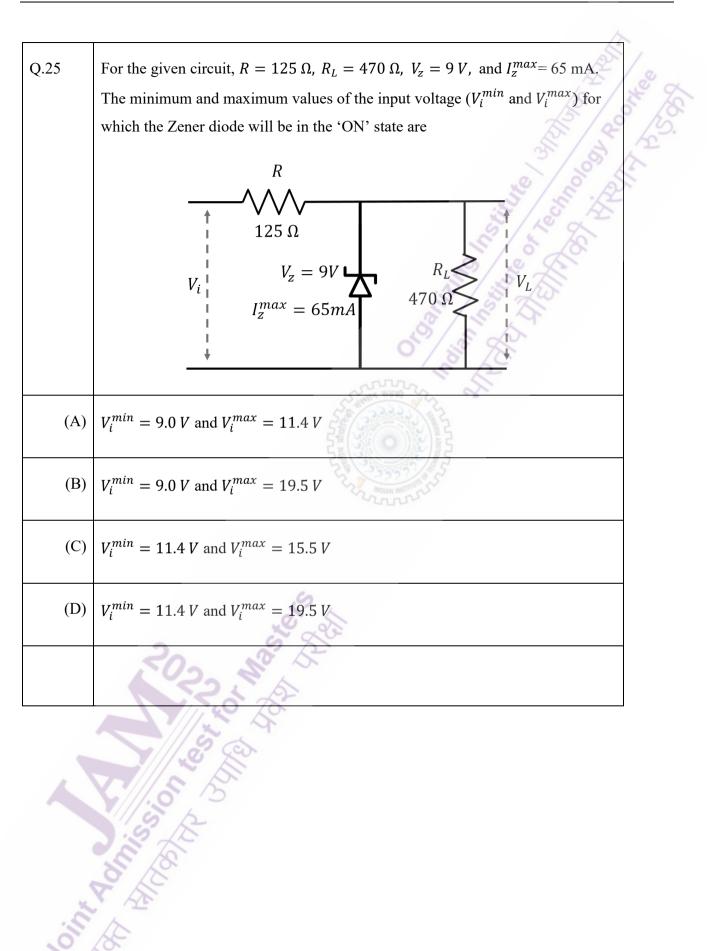


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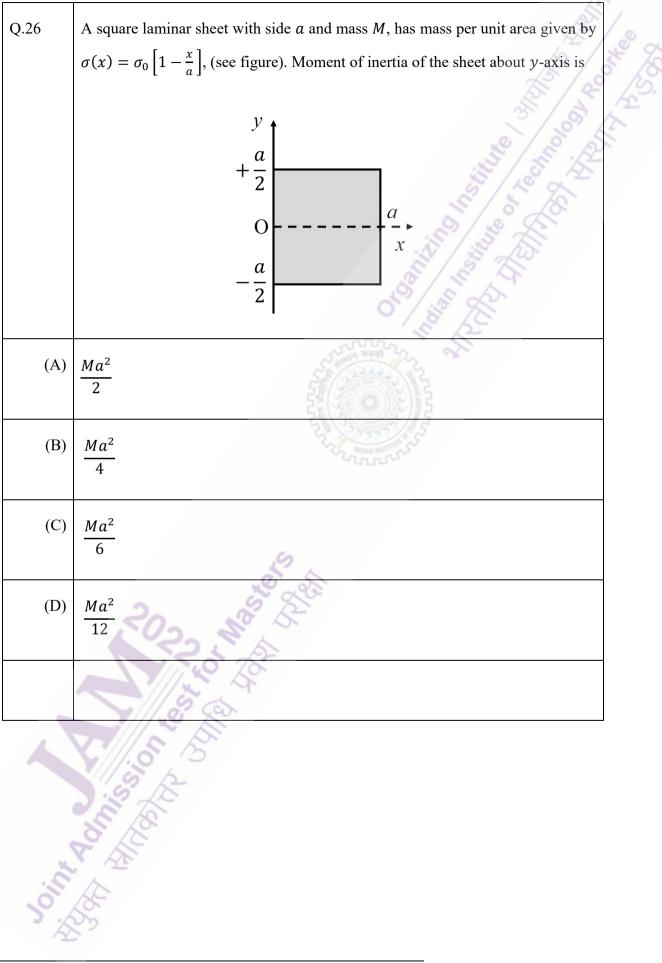
Q.24	A circular loop of wire with radius R is centered at the origin of the xy-plane. The magnetic field at a point within the loop is, $\vec{B}(\rho, \phi, z, t) = k\rho^3 t^3 \hat{z}$, where k is a positive constant of appropriate dimensions. Neglecting the effects of any
	current induced in the loop, the magnitude of the induced <i>emf</i> in the loop at time
	t is
(A)	$\frac{6\pi kt^2 R^5}{5}$
(B)	$\frac{5\pi kt^2 R^5}{6}$
(C)	$\frac{3\pi kt^2 R^5}{2}$
(D)	$\frac{\pi k t^2 R^5}{2}$
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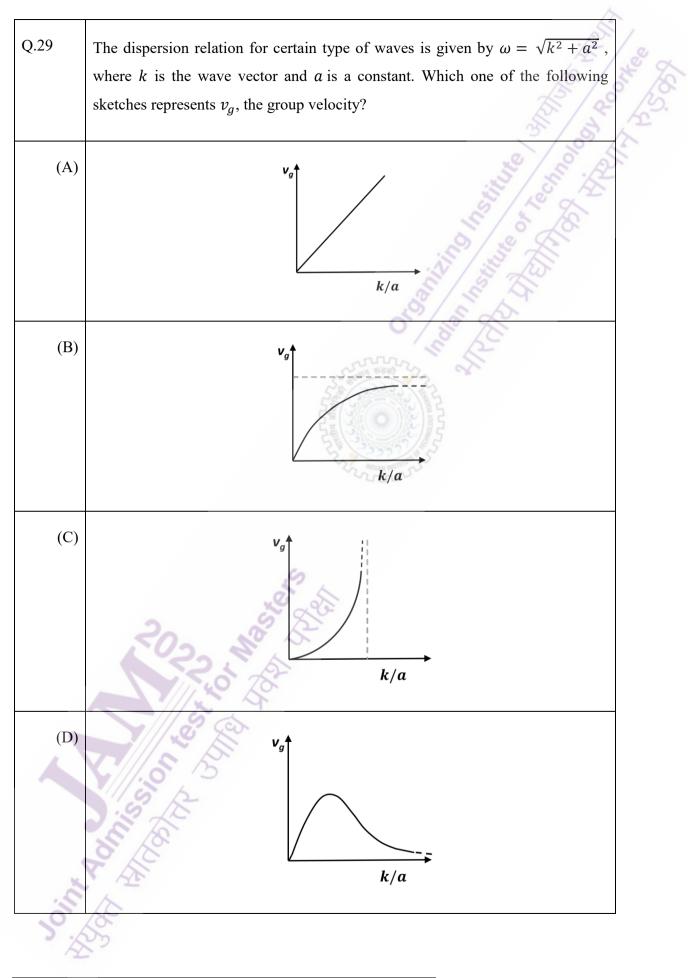
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Q.27	
X.~ /	A particle is subjected to two simple harmonic motions along the x and y axes, described by $x(t) = a \sin(2\omega t + \pi)$ and $y(t) = 2a \sin(\omega t)$. The resultant
	motion is given by
(A)	$\frac{x^2}{a^2} + \frac{y^2}{4a^2} = 1$
(B)	$x^2 + y^2 = 1$
(C)	$y^2 = x^2 \left(1 - \frac{x^2}{4a^2} \right)$
(D)	$x^2 = y^2 \left(1 - \frac{y^2}{4a^2} \right)$
	ANDLAN INSTITUTE OF A
Q.28	For a certain thermodynamic system, the internal energy $U = PV$ and P is proportional to T^2 . The entropy of the system is proportional to
Q.28 (A)	
	proportional to T^2 . The entropy of the system is proportional to
(A)	proportional to T^2 . The entropy of the system is proportional to
(B)	proportional to T^2 . The entropy of the system is proportional to







Q.30	Consider a binary number with m digits, where m is an even number. This binary number has alternating 1's and 0's, with digit 1 in the highest place value. The decimal equivalent of this binary number is
(A)	2 ^m - 1
(B)	$\frac{(2^m-1)}{3}$
(C)	$\frac{(2^{m+1}-1)}{3}$
(D)	$\frac{2}{3}(2^m-1)$
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Section B	3: Q.31 – Q.40 Carry TWO marks each.	250
Q.31	Consider the 2 × 2 matrix $M = \begin{pmatrix} 0 & a \\ a & b \end{pmatrix}$, where $a, b > 0$. Then,	15.
(A)	<i>M</i> is a real symmetric matrix	
(B)	One of the eigenvalues of <i>M</i> is greater than <i>b</i>	
(C)	One of the eigenvalues of <i>M</i> is negative	
(D)	Product of eigenvalues of M is b	
	ANDIAN INSTITUTE A	
Q.32	In the Compton scattering of electrons, by photons incident with wavelength λ ,	
(A)	$\frac{\Delta\lambda}{\lambda}$ is independent of λ	
(B)	$\frac{\Delta\lambda}{\lambda}$ increases with decreasing λ	
(C)	there is no change in photon's wavelength for all angles of deflection of the photon	
(D)	$\frac{\Delta\lambda}{\lambda}$ increases with increasing angle of deflection of the photon	
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Q.33 The figure shows a section of the phase boundary separating the vapour (1) and liquid (2) states of water in the P-T plane. Here, C is the critical point. μ_1 , ν_1 and s_1 are the chemical potential, specific volume and specific entropy of the vapour phase respectively, while μ_2 , ν_2 and s_2 respectively denote the same for the liquid phase. Then Р liquid В vapour Α 7 (A) $\mu_1 = \mu_2$ along AB $v_1 = v_2$ along AB (B) (C) $s_1 = s_2$ along AB $v_1 = v_2$ at the point C (D)



Q.34	A particle is executing simple harmonic motion with time period T . Let x , v and a denote the displacement, velocity and acceleration of the particle, respectively,
	at time t. Then,
(A)	$\frac{aT}{x}$ does not change with time
(B)	$(aT + 2\pi v)$ does not change with time
(C)	x and v are related by an equation of a straight line
(D)	v and a are related by an equation of an ellipse
Q.35	A linearly polarized light beam travels from origin to point A (1,0,0). At the point
	A, the light is reflected by a mirror towards point B $(1, -1, 0)$. A second mirror
	located at point B then reflects the light towards point C $(1, -1, 1)$. Let
	$\hat{n}(x, y, z)$ represent the direction of polarization of light at (x, y, z) .
(A)	If $\hat{n}(0, 0, 0) = \hat{y}$, then $\hat{n}(1, -1, 1) = \hat{x}$
(B)	If $\hat{n}(0, 0, 0) = \hat{z}$, then $\hat{n}(1, -1, 1) = \hat{y}$
(C)	If $\hat{n}(0, 0, 0) = \hat{y}$, then $\hat{n}(1, -1, 1) = \hat{y}$
(D)	If $\hat{n}(0, 0, 0) = \hat{z}$, then $\hat{n}(1, -1, 1) = \hat{x}$
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represent the corresponding unit vectors, then $(A) \frac{d\hat{r}}{d\theta} = \hat{\theta}$ $(B) \frac{d\hat{r}}{dr} = -\hat{\theta}$ $(C) \frac{d\hat{\theta}}{d\theta} = -\hat{r}$ $(D) \frac{d\hat{\theta}}{dr} = \hat{r}$			
represent the corresponding unit vectors, then (Λ) $\frac{d\hat{r}}{d\theta} = \hat{\theta}$ (R) $\frac{d\hat{r}}{dr} = -\hat{\theta}$ (C) $\frac{d\hat{\theta}}{d\theta} = -\hat{r}$ (D) $\frac{d\hat{\theta}}{dr} = \hat{r}$ $Q.37$ The electric field associated with an electromagnetic radiation is given by $E = a(1 + cos\omega_1 t)cos\omega_2 t$. Which of the following frequencies are present in the field? (Λ) ω_1 (B) $\omega_1 + \omega_2$ (C) $ \omega_1 - \omega_2 $	Q.36	Let (r, θ) denote the polar coordinates of a particle moving in a plane. If \hat{r} and $\hat{\theta}$	0.
(A) $\frac{d\hat{r}}{d\theta} = \hat{\theta}$ (B) $\frac{d\hat{r}}{dr} = -\hat{\theta}$ (C) $\frac{d\hat{\theta}}{d\theta} = -\hat{r}$ (D) $\frac{d\hat{\theta}}{dr} = \hat{r}$ Q.37 The electric field associated with an electromagnetic radiation is given by $E = a(1 + cos\omega_1 t)cos\omega_2 t$. Which of the following frequencies are present in the field? (A) ω_1 (B) $\omega_1 + \omega_2$ (C) $ \omega_1 - \omega_2 $			ě
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(D) $\frac{d\hat{\theta}}{dr} = \hat{r}$ Q.37 The electric field associated with an electromagnetic radiation is given by $E = a(1 + cos\omega_1 t)cos\omega_2 t$. Which of the following frequencies are present in the field? (A) ω_1 (B) $\omega_1 + \omega_2$ (C) $ \omega_1 - \omega_2 $	(C)	$\frac{d\theta}{dt} = -\hat{r}$	
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(B) $\omega_1 + \omega_2$ (C) $ \omega_1 - \omega_2 $			
(B) $\omega_1 + \omega_2$ (C) $ \omega_1 - \omega_2 $		the get	
(C) $ \omega_1 - \omega_2 $	(A)	ω_1	
(C) $ \omega_1 - \omega_2 $			
(C) $ \omega_1 - \omega_2 $	(D)	15.0 78	
1/1.0 13 5 B	(D)	$\omega_1 + \omega_2$	
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1/1.0 13 5 B	(C)	$ \omega_1 - \omega_2 $	
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	5.4	C.	
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Q.38	A string of length L is stretched between two points $x = 0$ and $x = L$ and the
	endpoints are rigidly clamped. Which of the following can represent the
	displacement of the string from the equilibrium position?
(A)	(πx)
(11)	$x\cos\left(\frac{\pi x}{L}\right)$
(P)	
(B)	$x\sin\left(\frac{\pi x}{L}\right)$
(C)	
(0)	$x\left(\frac{x}{L}-1\right)$
(D)	$(x \rightarrow)^2$
(-)	$x\left(\frac{x}{L}-1\right)^2$
	S S S S S S S S S S S S S S S S S S S
Q.39	The Boolean expression $Y = \overline{PQ}R + Q\overline{R} + \overline{P}QR + PQR$ simplifies to
(A)	$\overline{P}R + Q$
(B)	$PR + \bar{Q}$
(C)	P + R
(D)	Q + R
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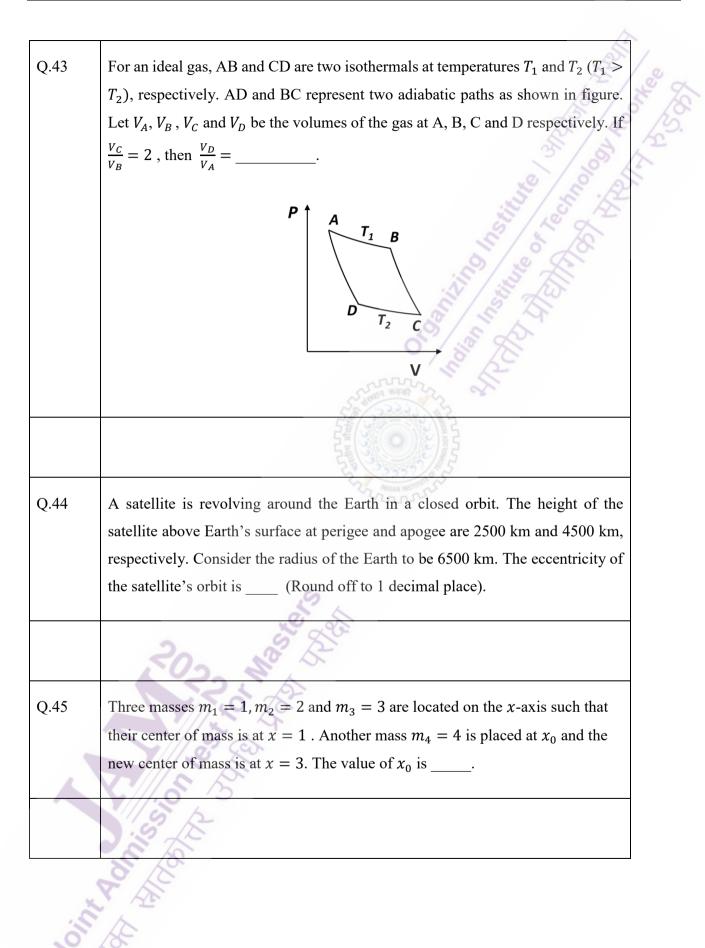


Q.40 For an *n*-type silicon, an extrinsic semiconductor, the natural logarithm of normalized conductivity (σ) is plotted as a function of inverse temperature. Temperature interval-I corresponds to the intrinsic regime, interval-II corresponds to saturation regime and interval-III corresponds to the freeze-out regime, respectively. Then ln(σ) Ι Π Ш 1 T (A) the magnitude of the slope of the curve in the temperature interval-I is proportional to the bandgap, E_a **(B)** the magnitude of the slope of the curve in the temperature interval-III is proportional to the ionization energy of the donor, E_d in the temperature interval-II, the carrier density in the conduction band is equal (C) to the density of donors in the temperature interval-III, all the donor levels are ionized (D)



Section	C: Q.41 – Q.50 Carry ONE mark each.
Q.41	The integral $\iint (x^2 + y^2) dx dy$ over the area of a disk of radius 2 in the xy plane is $\{\pi}$.
Q.42	For the given operational amplifier circuit $R_1 = 120 \ \Omega$, $R_2 = 1.5 \ k\Omega$ and $V_s = 0.6 \ V$, then the output current I_0 is mA.
	R_1
	$= V_s$







Q.46	A normal human eye can distinguish two objects separated by $0.35 m$ when viewed from a distance of $1.0 km$. The angular resolution of eye is
	seconds (Round off to the nearest integer).
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Q.47	A rod with a proper length of 3 <i>m</i> moves along <i>x</i> -axis, making an angle of 30°
	with respect to the x-axis. If its speed is $\frac{c}{2}$ m/s, where c is the speed of light, the
	change in length due to Lorentz contraction is \m (Round off to 2 decimal
	places).
	[Use $c = 3 \times 10^8 m/s$]
Q.48	Consider the Bohr model of hydrogen atom. The speed of an electron in the
	second orbit $(n-2)$ is $\times 10^6 m/s$ (Pound off to 2 desired places)
	second orbit $(n = 2)$ is × 10 ⁶ m/s (Round off to 2 decimal places).
	Second orbit $(n = 2)$ is × 10 ⁻ m/s (Round on to 2 decimal places). [Use $h = 6.63 \times 10^{-34}$ Js, $e = 1.6 \times 10^{-19}$ C, $\epsilon_0 = 8.85 \times 10^{-12}$ C ² m ² /N]
Q.49	
Q.49	[Use $h = 6.63 \times 10^{-34}$ Js, $e = 1.6 \times 10^{-19}$ C, $\epsilon_0 = 8.85 \times 10^{-12} C^2 m^2 / N$]
Q.49	[Use $h = 6.63 \times 10^{-34}$ Js, $e = 1.6 \times 10^{-19}$ C, $\epsilon_0 = 8.85 \times 10^{-12}$ C ² m ² /N] Consider a unit circle C in the xy plane with center at the origin. The line integral
Q.49	[Use $h = 6.63 \times 10^{-34}$ Js, $e = 1.6 \times 10^{-19}$ C, $\epsilon_0 = 8.85 \times 10^{-12} C^2 m^2 / N$] Consider a unit circle C in the xy plane with center at the origin. The line integral of the vector field, $\vec{F}(x, y, z) = -2y\hat{x} - 3z\hat{y} + x\hat{z}$, taken anticlockwise over C



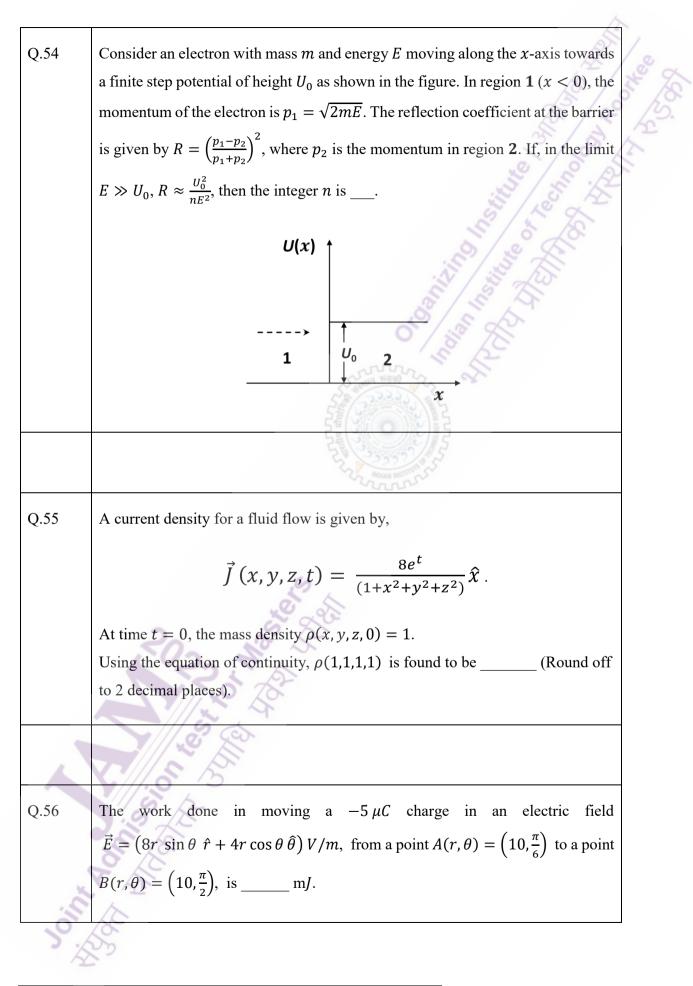
Q.50	Consider a p-n junction at $T = 300 K$. The saturation current density at reverse
	bias is $-20 \mu A/cm^2$. For this device, a current density of magnitude
	$10 \mu A/cm^2$ is realized with a forward bias voltage, V_F . The same magnitude of
	current density can also be realized with a reverse bias voltage, V_R . The value of
	$ V_F/V_R $ is (Round off to 2 decimal places).
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Section C: Q.51 – Q.60 Carry TWO marks each.	
Q.51	Consider the second order ordinary differential equation, $y'' + 4y' + 5y = 0$. If $y(0) = 0$ and $y'(0) = 1$, then the value of $y(\pi/2)$ is (Round off to 3 decimal places).
Q.52	A box contains a mixture of two different ideal monoatomic gases, 1 and 2, in equilibrium at temperature <i>T</i> . Both gases are present in equal proportions. The atomic mass for gas 1 is <i>m</i> , while the same for gas 2 is $2m$. If the <i>rms</i> speed of a gas molecule selected at random is $v_{rms} = x \sqrt{\frac{k_B T}{m}}$, then <i>x</i> is
Q.53	A hot body with constant heat capacity $800 J/K$ at temperature $925 K$ is dropped gently into a vessel containing $1 kg$ of water at temperature $300 K$ and the combined system is allowed to reach equilibrium. The change in the total entropy ΔS is J/K (Round off to 1 decimal place). [Take the specific heat capacity of water to be $4200 J/kg K$. Neglect any loss of heat to the vessel and air and change in the volume of water.]
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Q.57	A pipe of 1 <i>m</i> length is closed at one end. The air column in the pipe resonates at		
~	its fundamental frequency of 400 Hz. The number of nodes in the sound wave		
	formed in the pipe is		
	[Speed of sound = $320 m/s$]		
	20 11 Still		
Q.58	The critical angle of a crystal is 30°. Its Brewster angle is degrees (Round off to the nearest integer).		
	Superior and		
Q.59	In an LCR series circuit, a non-inductive resistor of 150 Ω , a coil of 0.2 H		
	inductance and negligible resistance, and a 30 μ <i>F</i> capacitor are connected across		
	an ac power source of 220 V , 50 Hz. The power loss across the resistor isW		
	(Round off to 2 decimal places).		
	50		
Q.60	A charge q is uniformly distributed over the volume of a dielectric sphere of		
	radius a. If the dielectric constant $\epsilon_r = 2$, then the ratio of the electrostatic energy		
	stored inside the sphere to that stored outside is (Round off to 1 decimal		
	place).		
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5.4	C.C.		

END OF THE QUESTION PAPER